

ZZS-12

Modulační syntéza

8. prosince 2014

- Amplitudová modulace**
- Frekvenční modulace**
 - Syntetické zvony**
 - Jednoduché syntetické FM nástroje**
 - Syntetické zvuky – vítr**

Kruhová modulace

$$\sin \alpha \cdot \sin \beta = \frac{1}{2} [\cos(\alpha - \beta) - \cos(\alpha + \beta)]$$

$$\cos \alpha \cdot \cos \beta = \frac{1}{2} [\cos(\alpha - \beta) + \cos(\alpha + \beta)]$$

$$\sin \alpha \cdot \cos \beta = \frac{1}{2} [\sin(\alpha - \beta) - \sin(\alpha + \beta)]$$

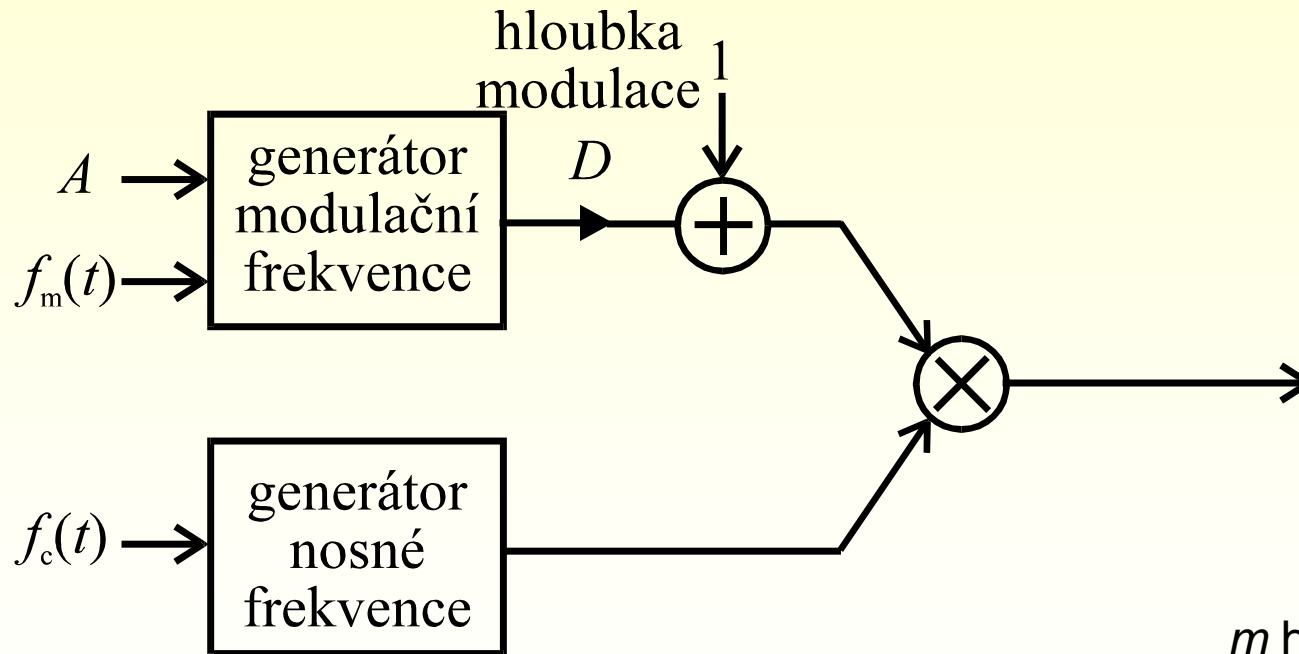
$$\cos(2\pi f_m t) \cos(2\pi f_c t) = \frac{1}{2} \cos(2\pi(f_c - f_m)t) + \frac{1}{2} \cos(2\pi(f_c + f_m)t)$$

$$x = 0.5 \cdot \cos(2 \cdot \pi \cdot 750 \cdot t) + 0.5 \cdot \cos(2 \cdot \pi \cdot 450 \cdot t)$$

$$x = \cos(2 \cdot \pi \cdot 600 \cdot t) \cdot \cos(2 \cdot \pi \cdot 150 \cdot t)$$

Amplitudová modulace

– Změna amplitudy jiným signálem



m hloubka modulace

f_c modulační frekvence

f_m nosná frekvence

$$f(t) = (1 + m \cdot \sin 2\pi f_m t) \sin 2\pi f_c t$$

Amplitudová modulace

$$\sin \alpha \cdot \sin \beta = \frac{1}{2} [\cos(\alpha - \beta) - \cos(\alpha + \beta)]$$

$$\cos \alpha \cdot \cos \beta = \frac{1}{2} [\cos(\alpha - \beta) + \cos(\alpha + \beta)]$$

$$\sin \alpha \cdot \cos \beta = \frac{1}{2} [\sin(\alpha - \beta) - \sin(\alpha + \beta)]$$

$$(1 + m \cdot \sin(2\pi f_m t)) \sin(2\pi f_c t) =$$

$$\sin(2\pi f_c t) + m_d \cdot \sin(2\pi f_m t) \sin(2\pi f_c t) =$$

$$\sin(2\pi f_c t) + \frac{m_d}{2} \cos(2\pi(f_c - f_m)t) - \frac{m_d}{2} \cos(2\pi(f_c + f_m)t)$$

Amplitudové modulace

f_c

f_m

600

150



600

170



600

50



600

70



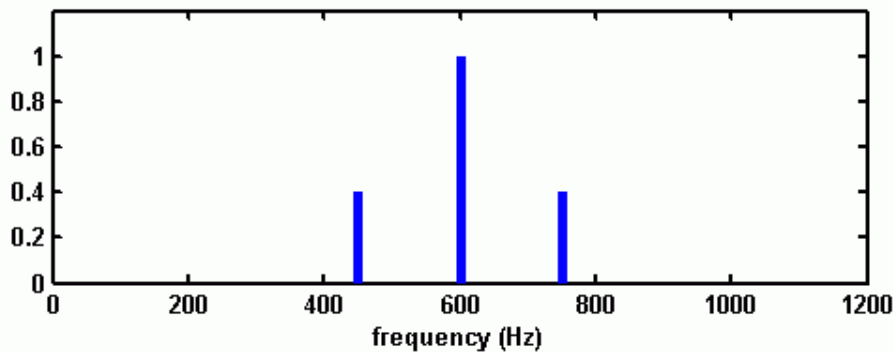
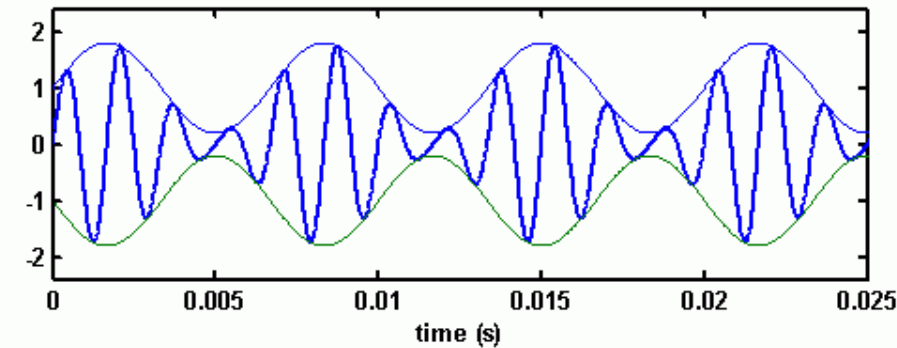
600

4

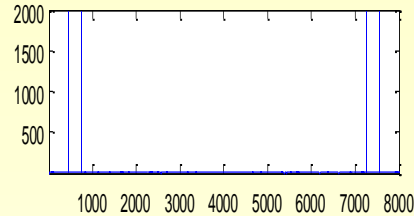
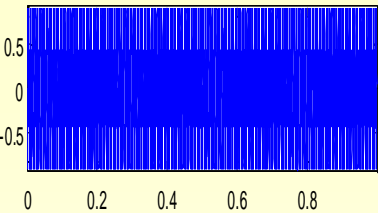


600

1

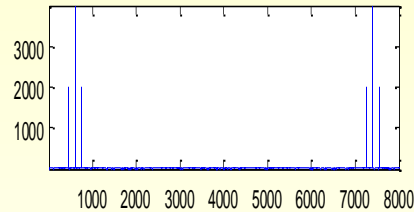
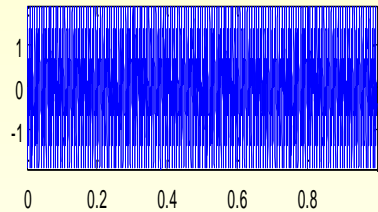


Amplitudové modulace

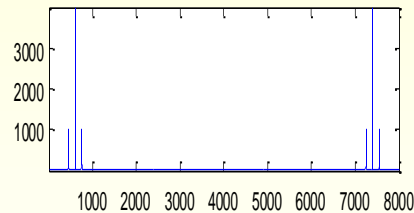
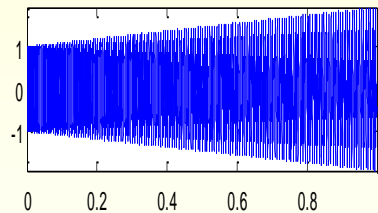


$$x = 0.5 \cdot \cos(2 \cdot \pi \cdot 750 \cdot t) + 0.5 \cdot \cos(2 \cdot \pi \cdot 450 \cdot t)$$

$$x = \cos(2 \cdot \pi \cdot 600 \cdot t) \cdot \cos(2 \cdot \pi \cdot 150 \cdot t)$$

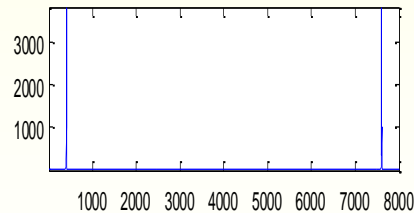
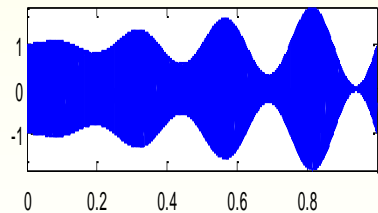


$$x = (1 + 1 \cdot \sin(2 \cdot \pi \cdot 150 \cdot t)) \cdot \sin(2 \cdot \pi \cdot 600 \cdot t)$$



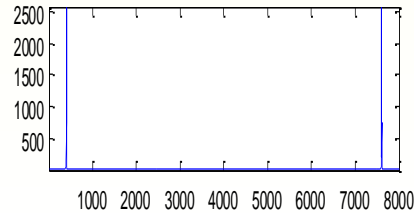
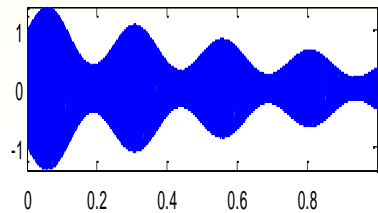
$$m_i = 0 \dots 1$$

$$x = (1 + m_i \cdot \sin(2 \cdot \pi \cdot 150 \cdot t)) \cdot \sin(2 \cdot \pi \cdot 600 \cdot t)$$



$$m_i = 0 \dots 1$$

$$x = (1 + m_i \cdot \sin(2 \cdot \pi \cdot 4 \cdot t)) \cdot \sin(2 \cdot \pi \cdot 400 \cdot t)$$



$$m_i = 0 \dots 1$$

$$x = (1 + m_i \cdot \sin(2 \cdot \pi \cdot 4 \cdot t)) \cdot \sin(2 \cdot \pi \cdot 400 \cdot t) \cdot \exp(-t)$$



Amplitudová modulace

Harmonické a neharmonické modulační frekvence, $m = 0.5$

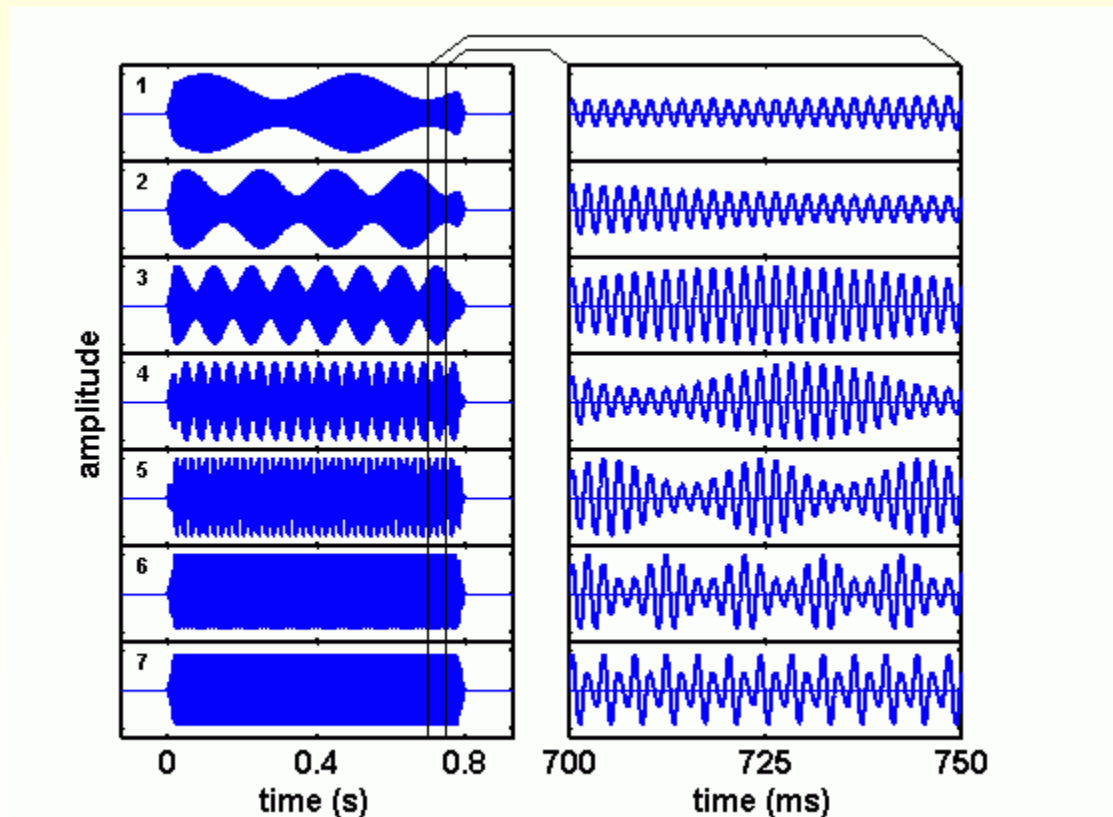
$f_c = 500\text{Hz}$

$f_c = 500\text{Hz}$

$f_m = 2.5, 5, 10, 25, 50, 100, 250\text{ Hz}$ $f_m = 4.05, 8.09, 16.2, 40.5, 80.9, 162, 405\text{ Hz}$



(.wav)



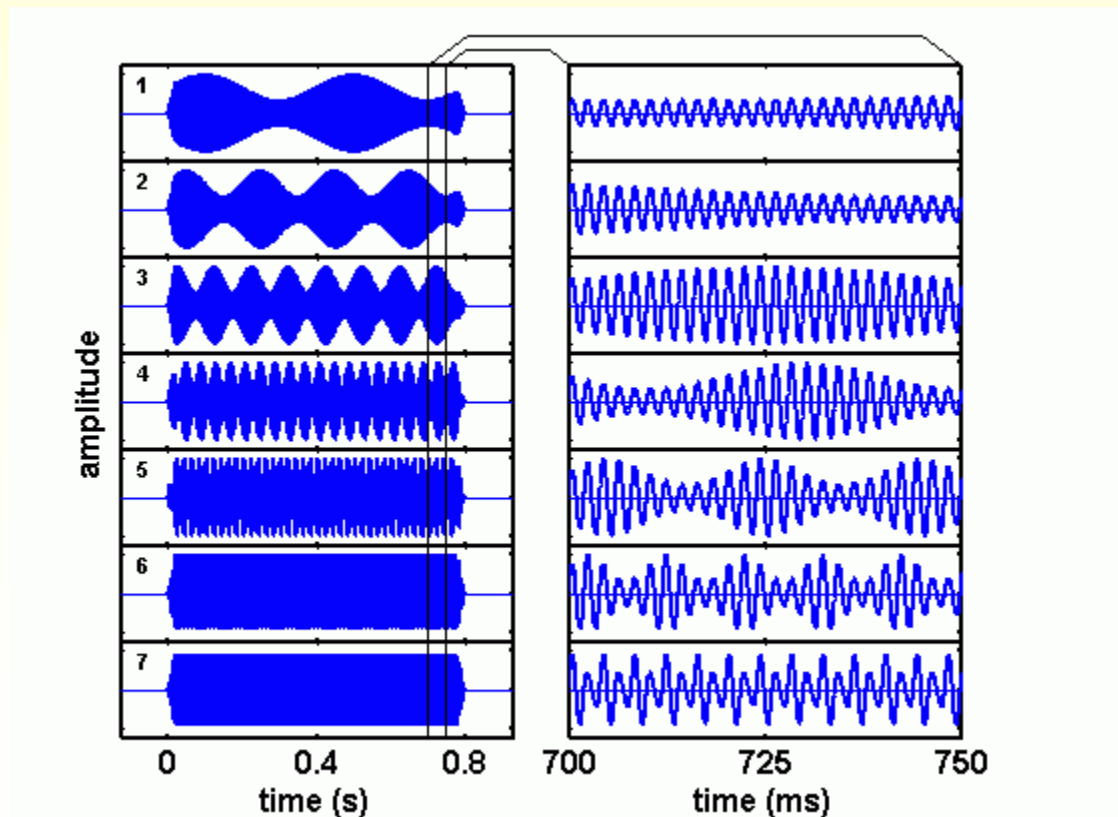
Amplitudová modulace

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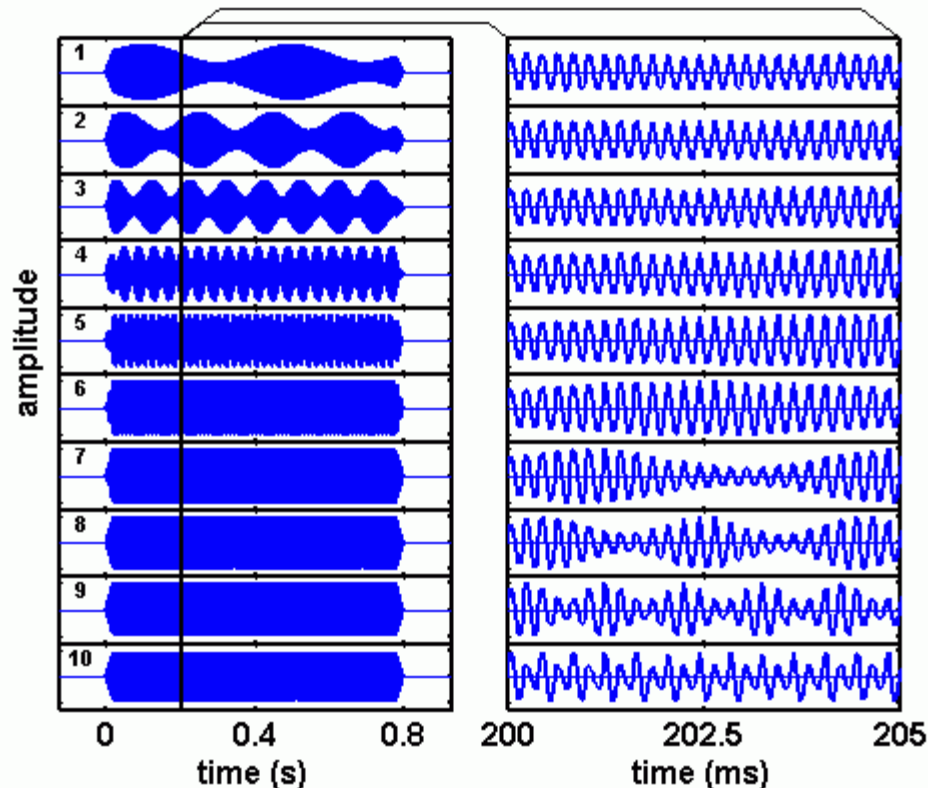


Amplitudová modulace

Harmonické a neharmonické modulační frekvence, $m = 0.5$

$f_c = 5000\text{Hz}$
 $f_m = 2.5, 5, 10, 25, 50, 100,$
 $250, 500, 1000, 2500\text{ Hz}$

$f_c = 5000\text{Hz}$
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 $162, 405, 809, 1618, 4045\text{ Hz}$

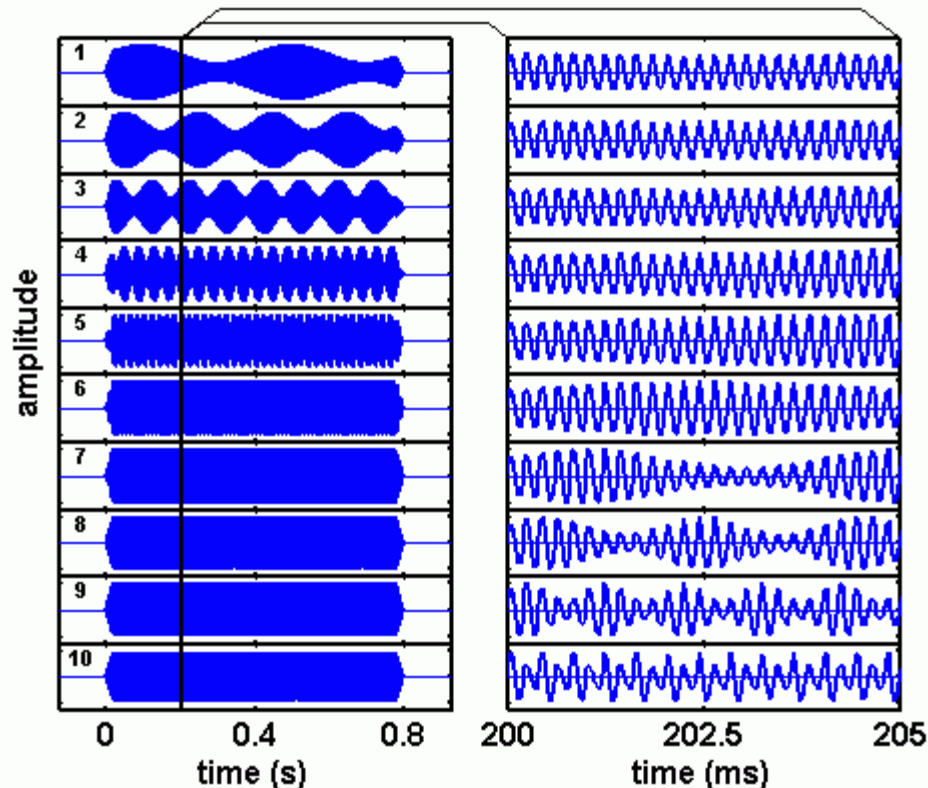


Amplitudová modulace

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(.wav)

Amplitudová modulace

Zvětšení hloubky
modulace, $m = 0 .. 1$

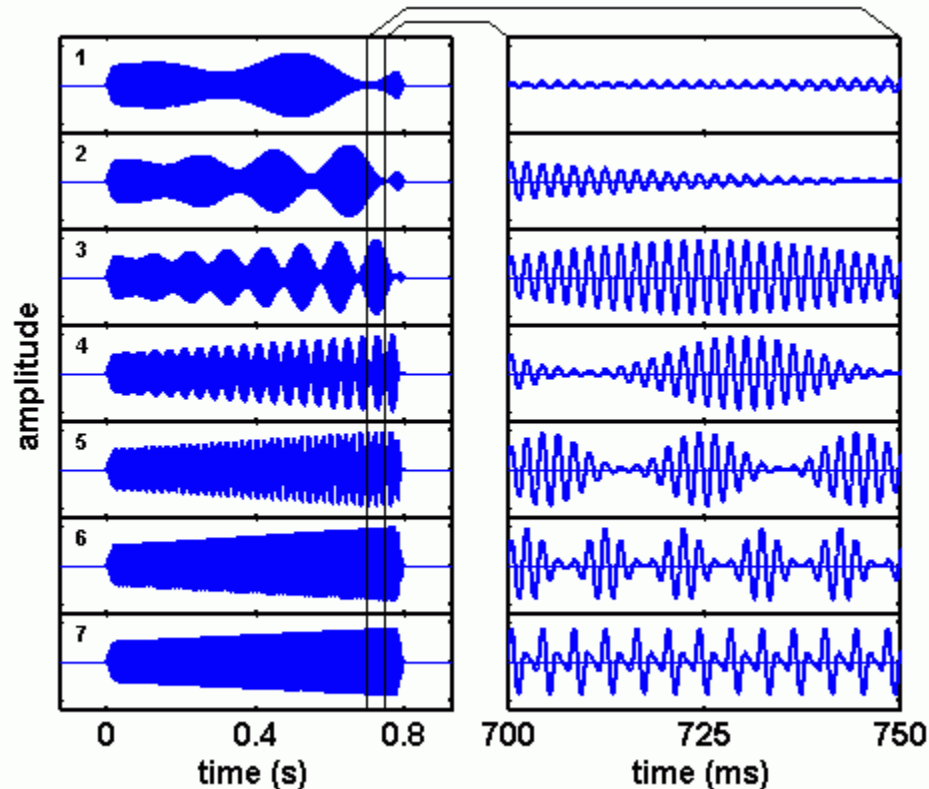
$f_c = 500\text{Hz}$

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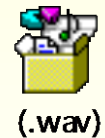
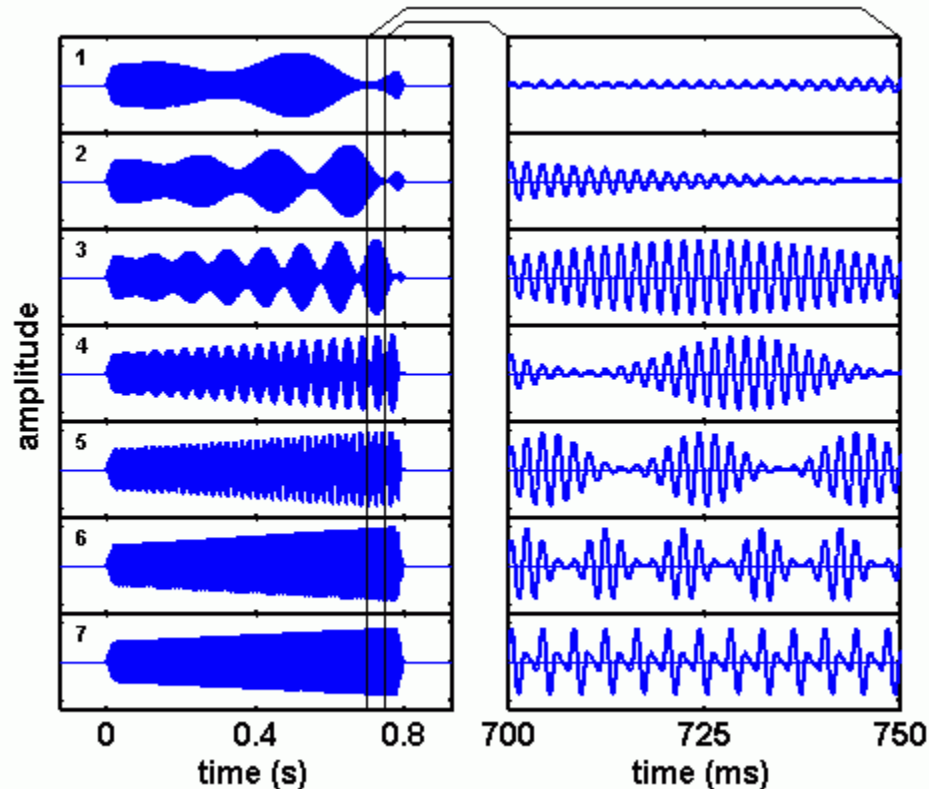
Amplitudová modulace

Zvětšení hloubky
modulace, $m = 0 .. 1$

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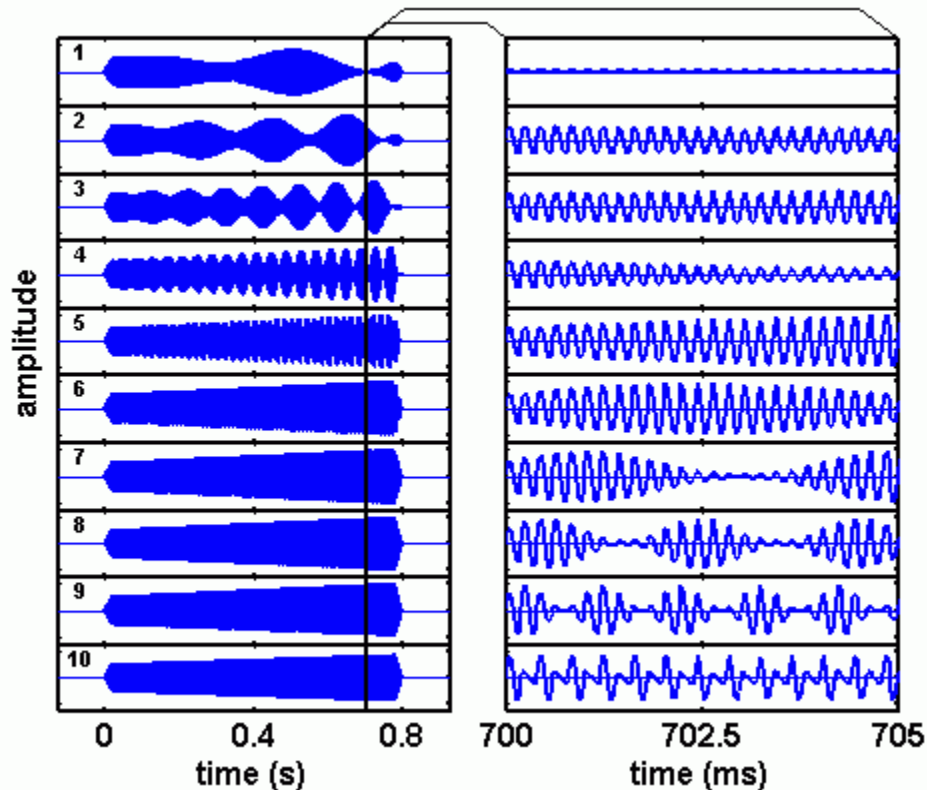


Amplitudová modulace

Zvětšení hloubky
modulace, $m = 0 .. 1$

$f_c = 5000\text{Hz}$
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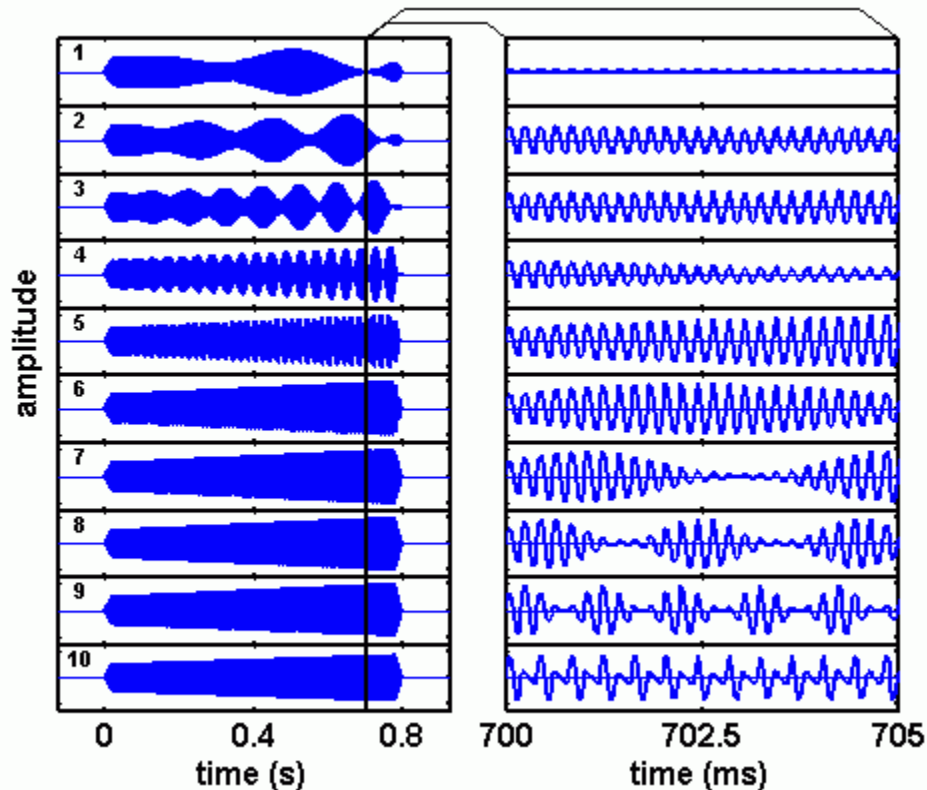


Amplitudová modulace

Zvětšení hloubky
modulace, $m = 0 .. 1$

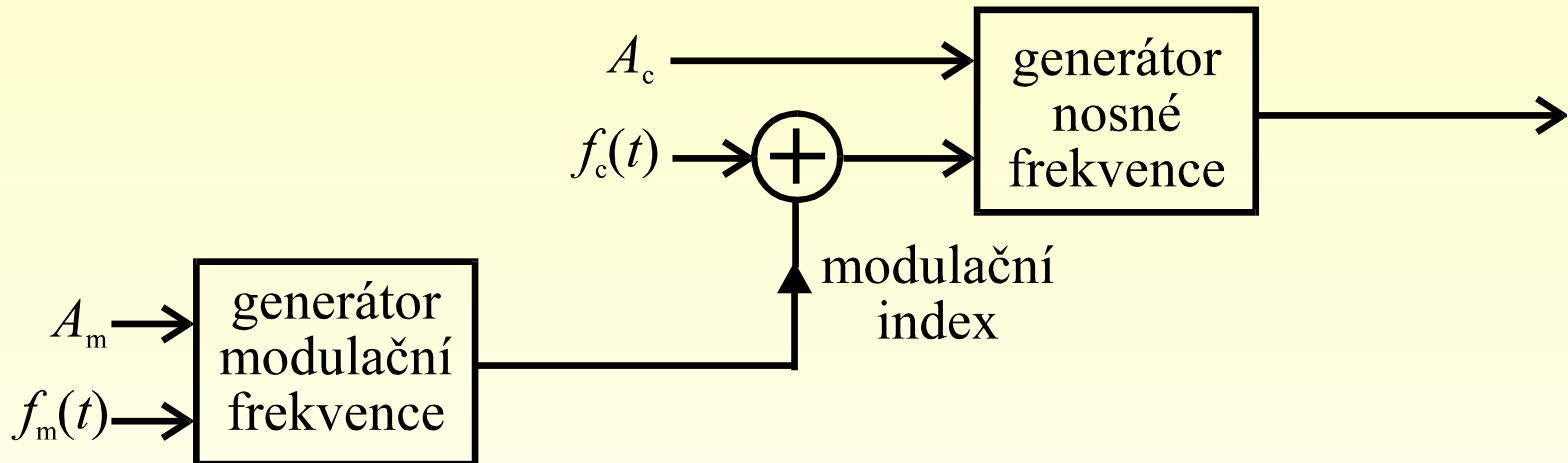
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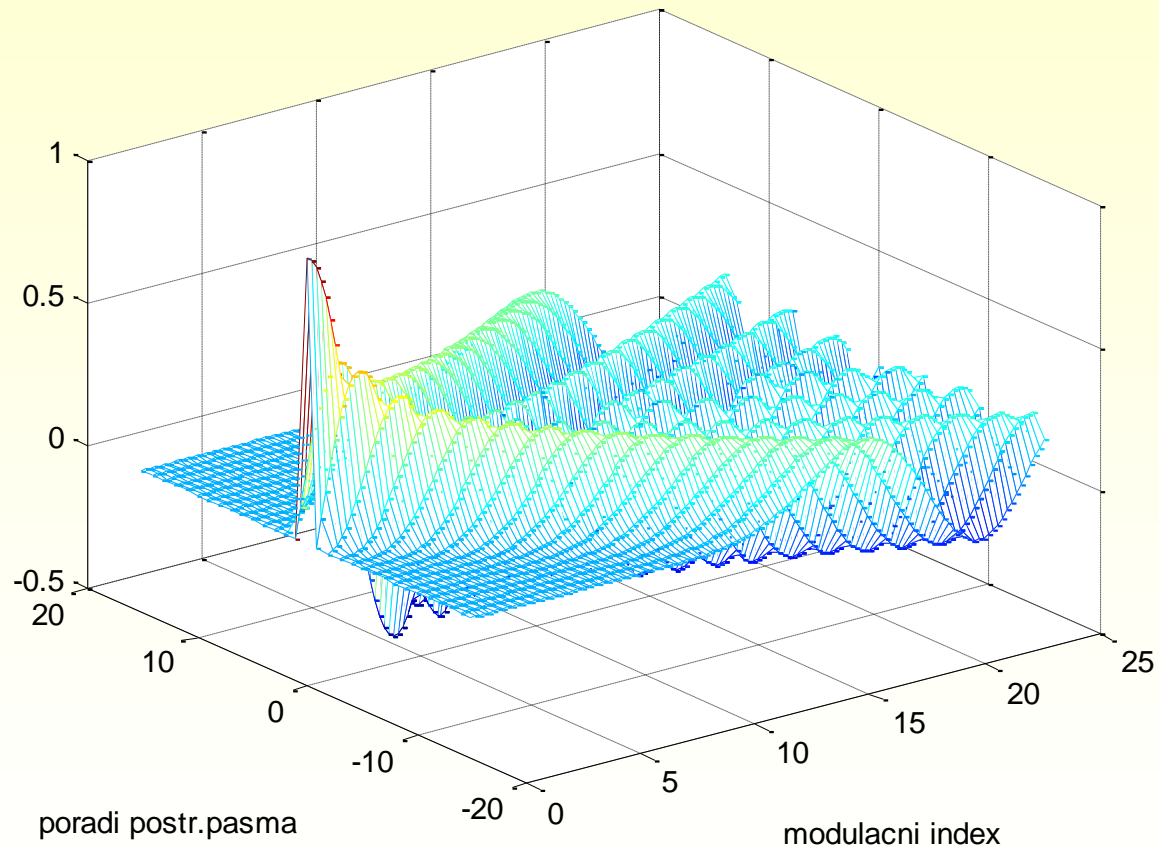
Frekvenční modulace



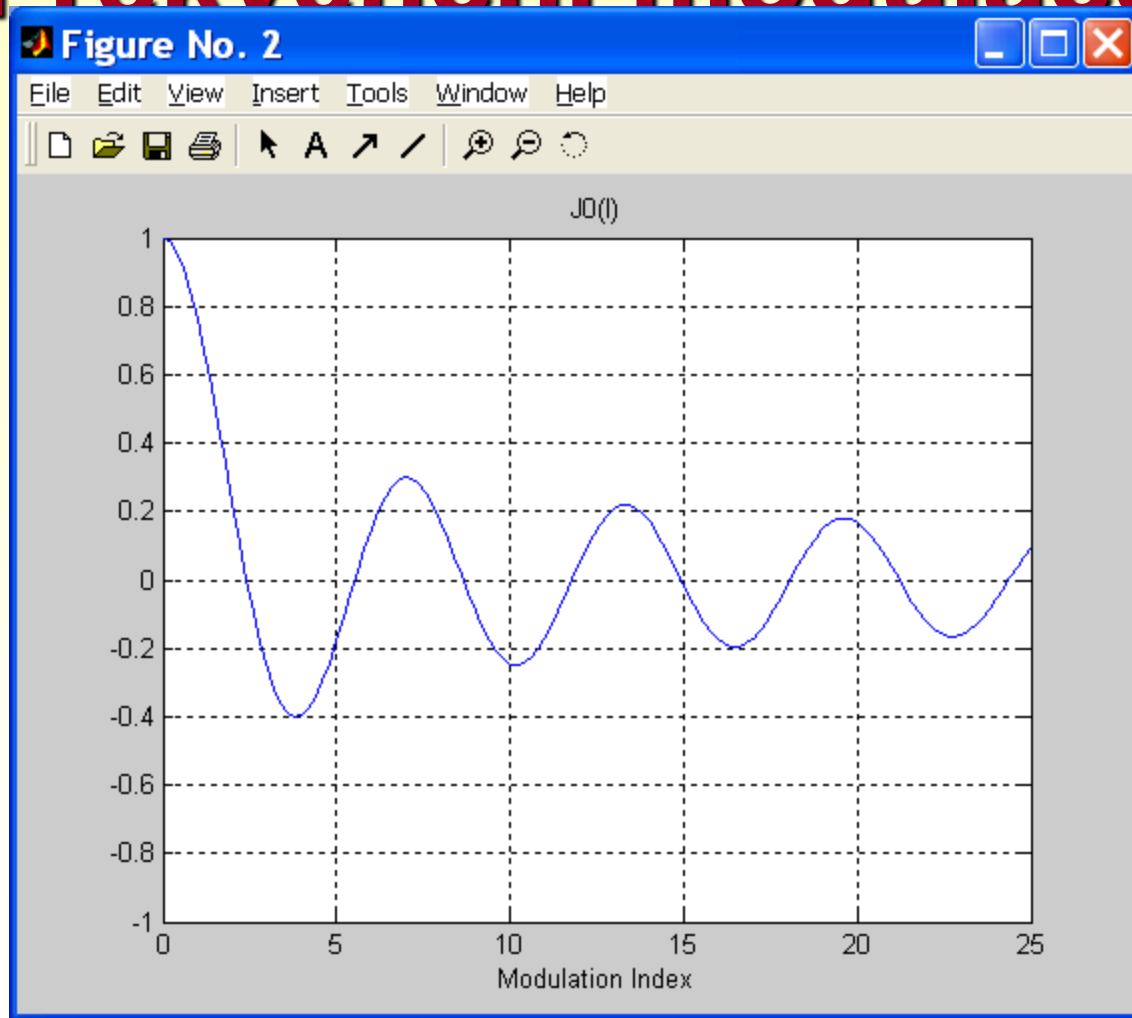
$$f(t) = \sin((2\pi f_c t) + m_i \cdot \sin(2\pi f_m t))$$

$$\sin(2\pi f_c t + m_i \sin(2\pi f_m t)) = \sum_{k=-\infty}^{\infty} I_k(m_i) \sin(2\pi(f_c + k f_m) + \phi_k)$$

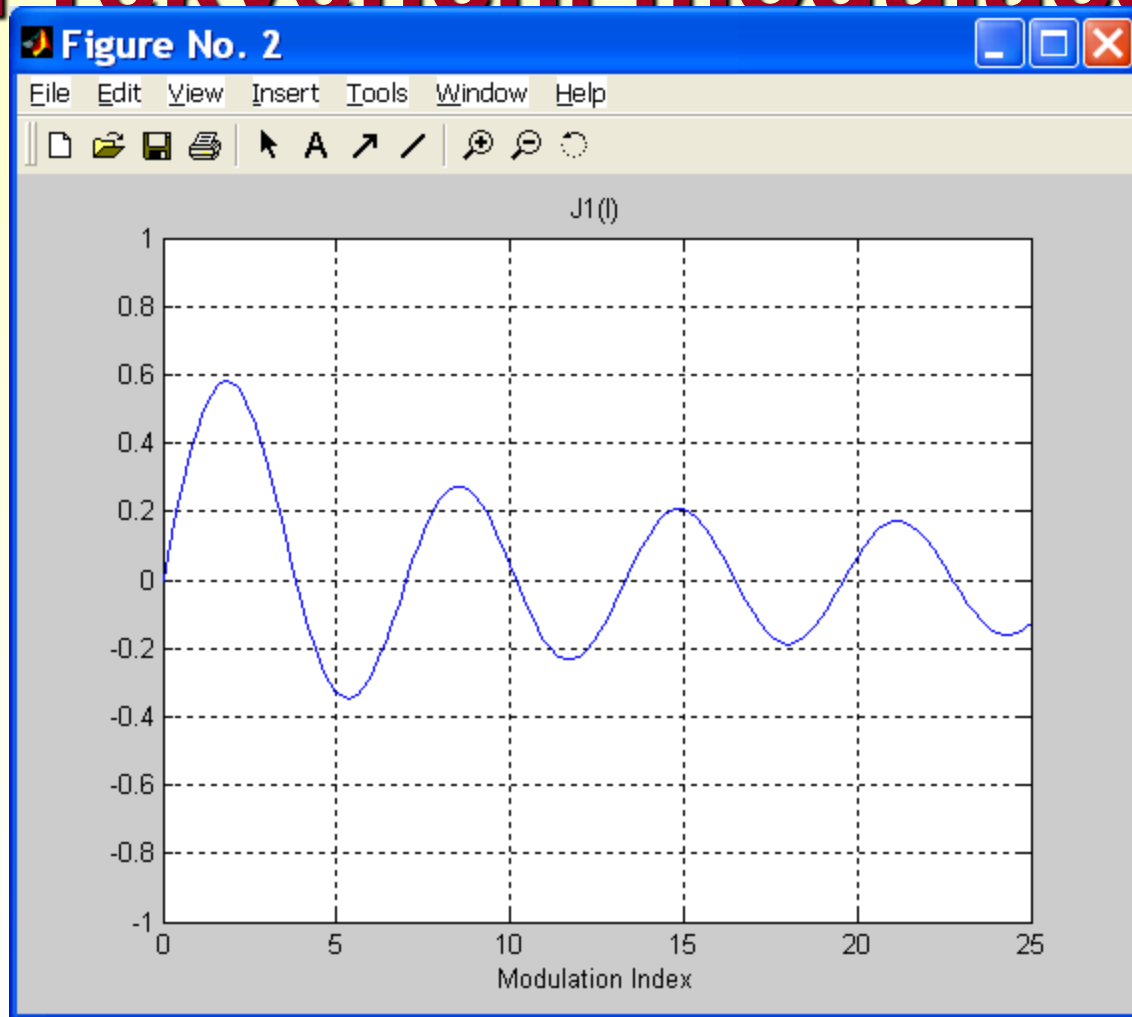
Frekvenční modulace



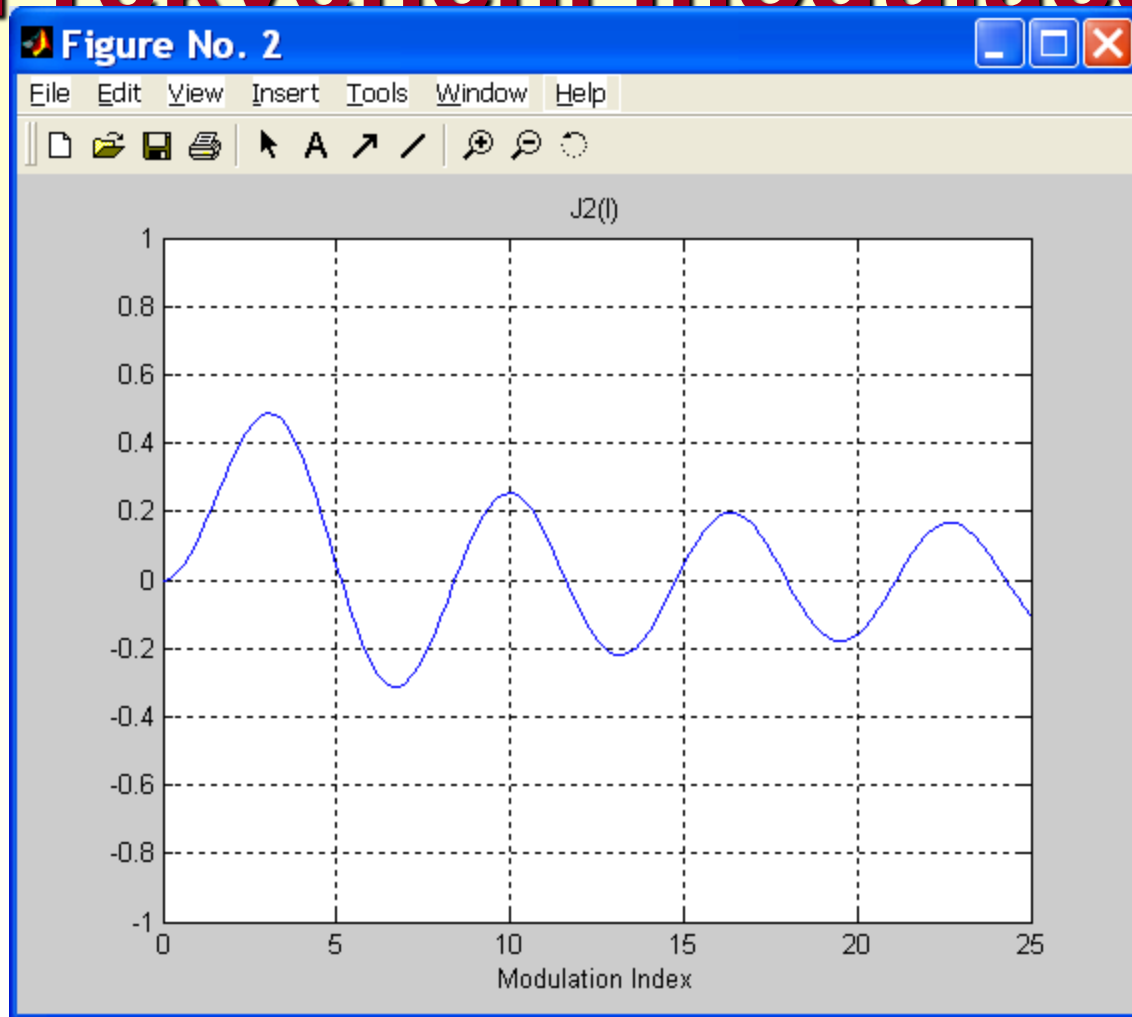
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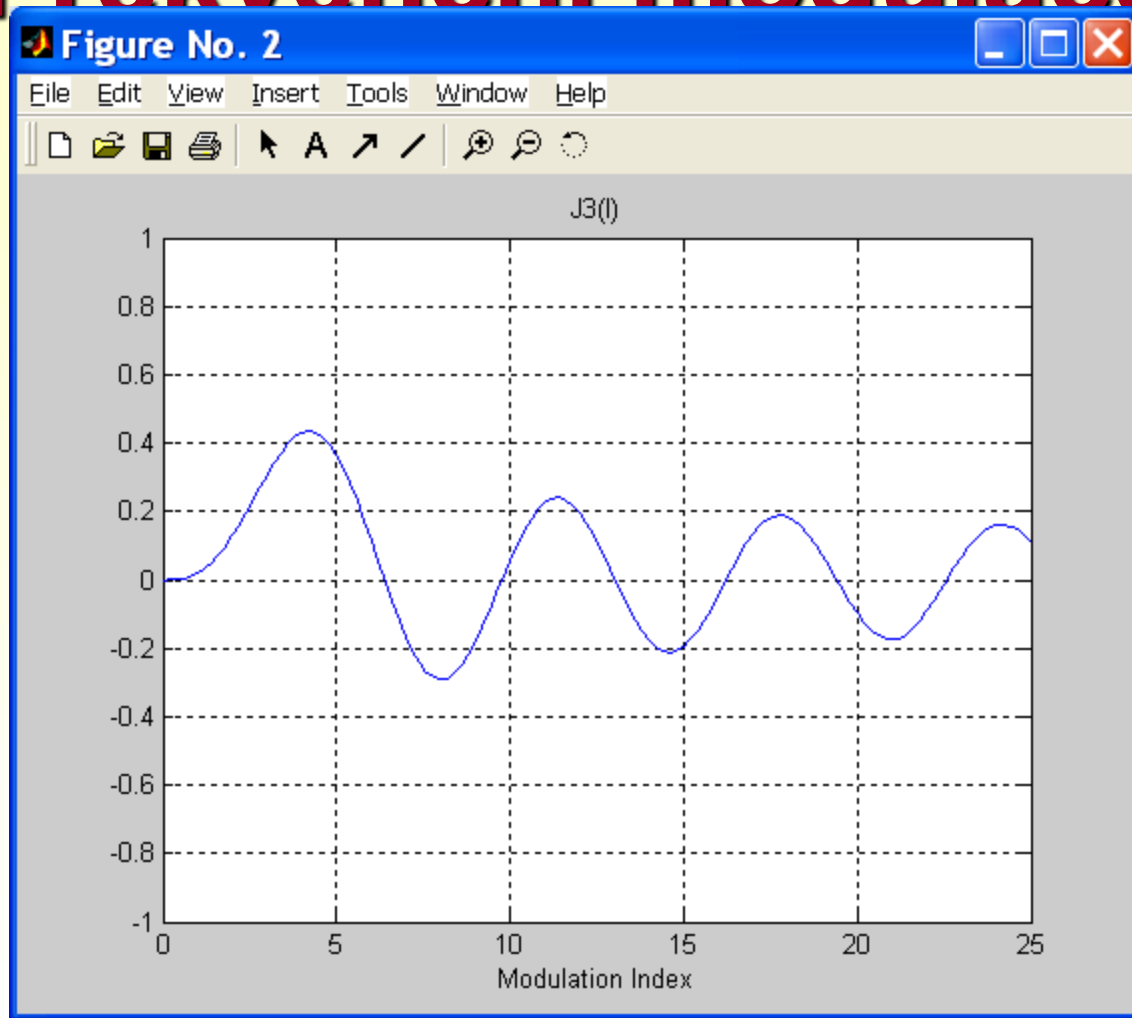
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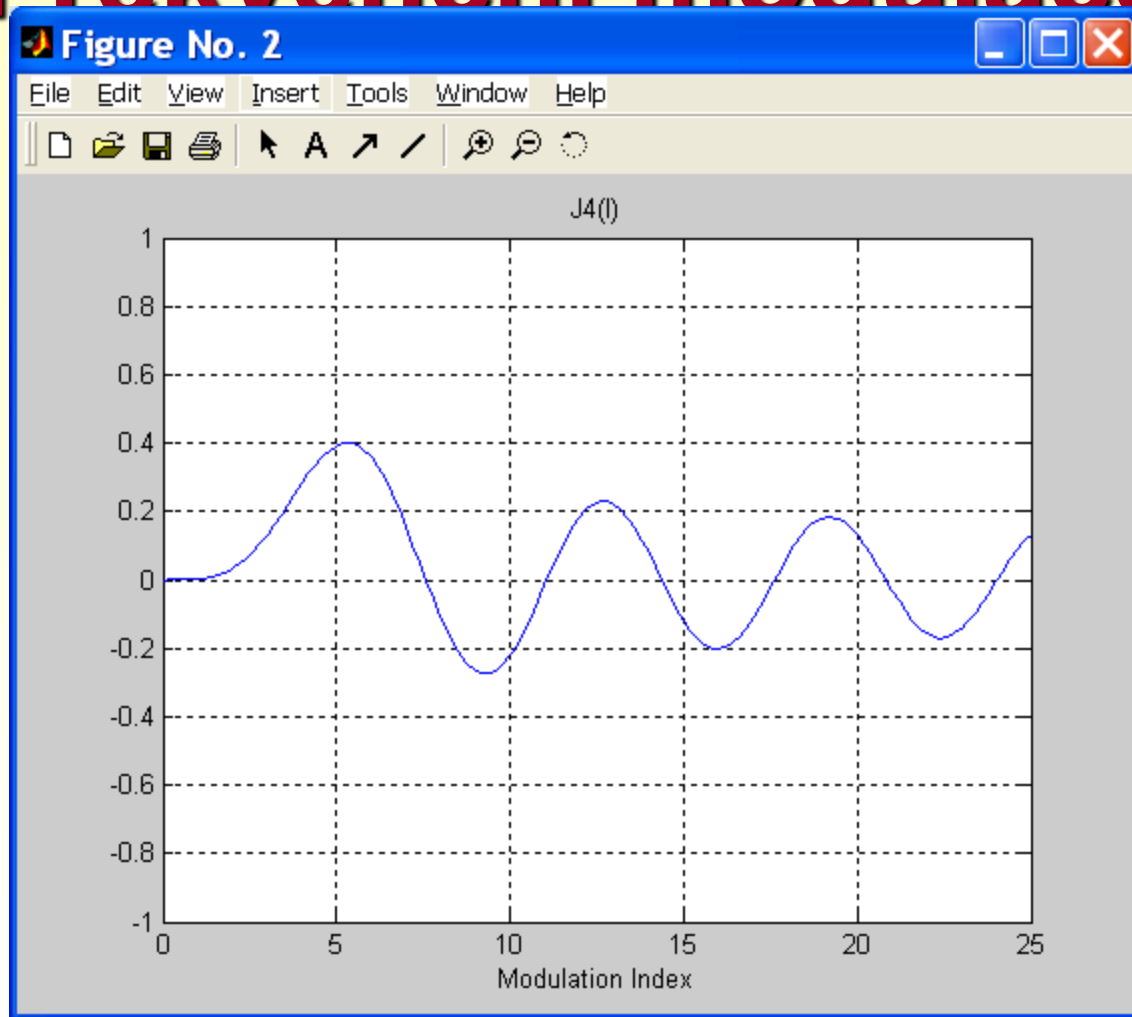
Frekvenční modulace



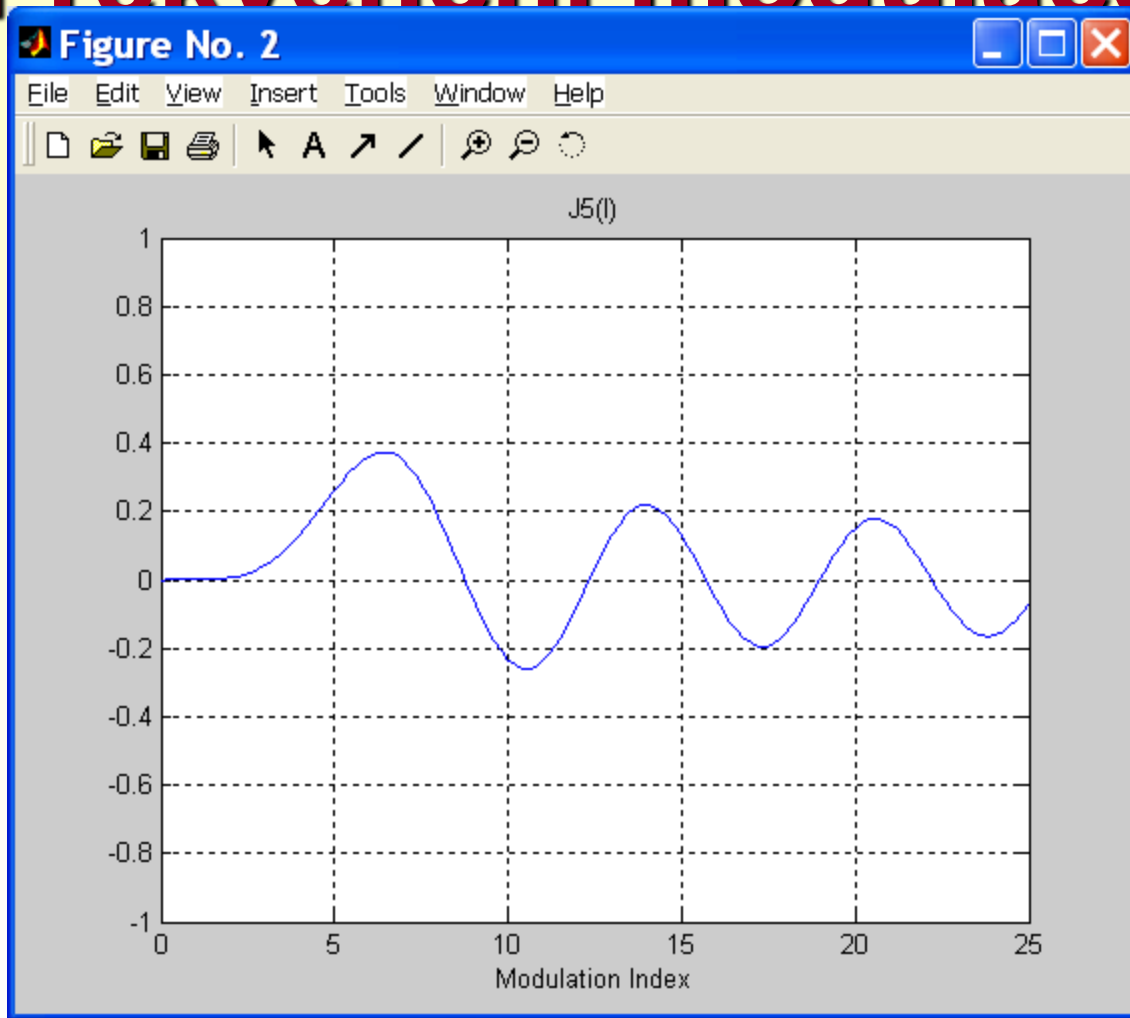
Frekvenční modulace



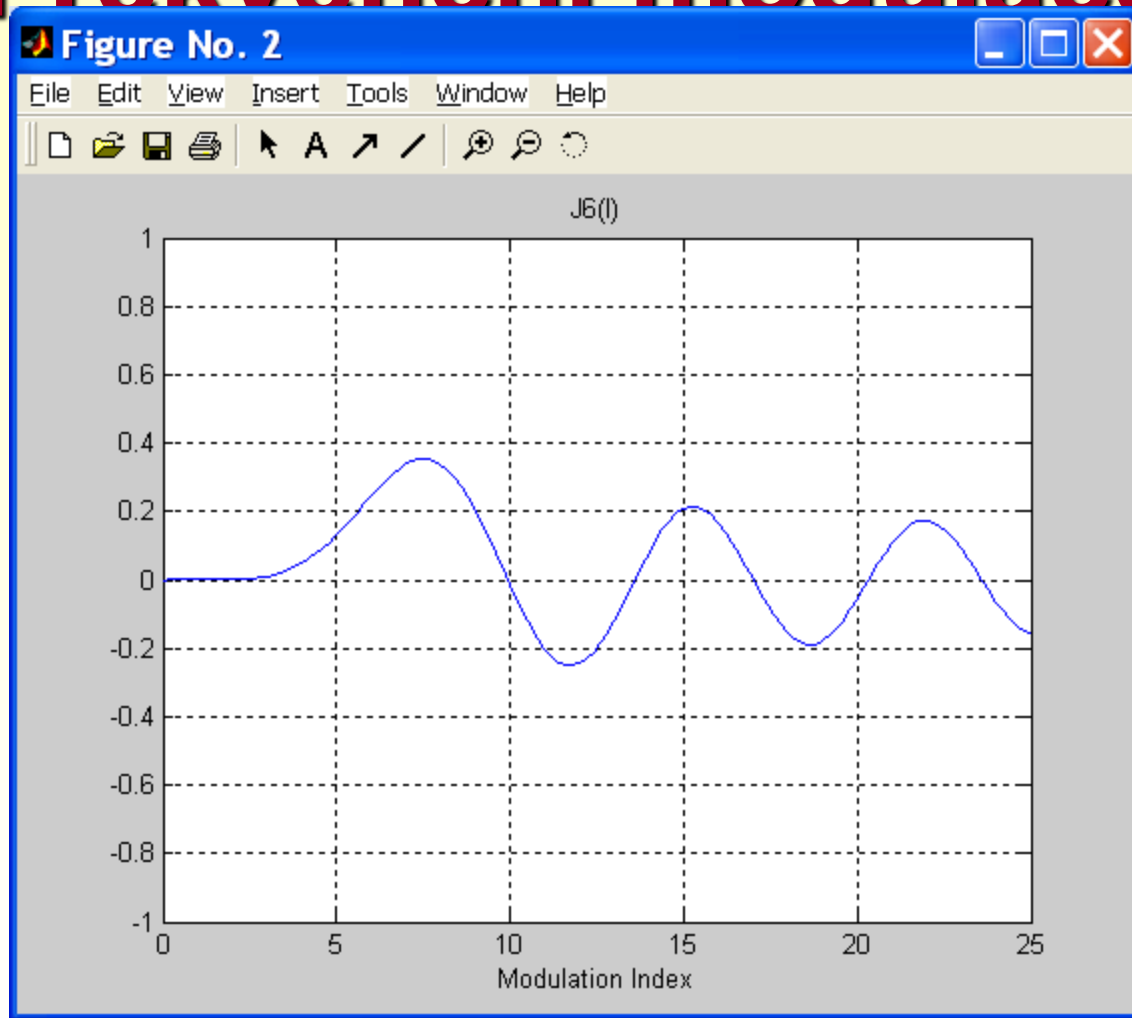
Frekvenční modulace



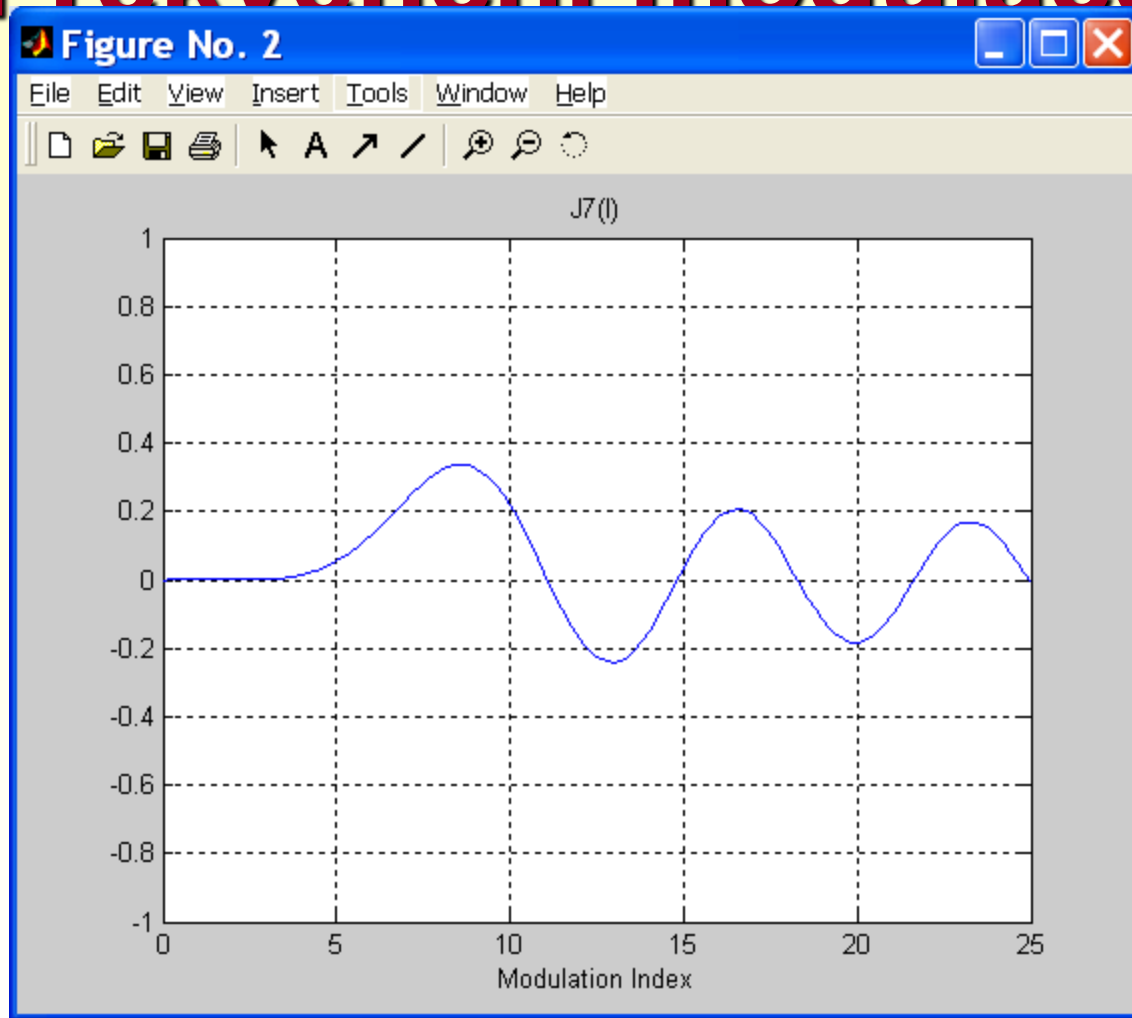
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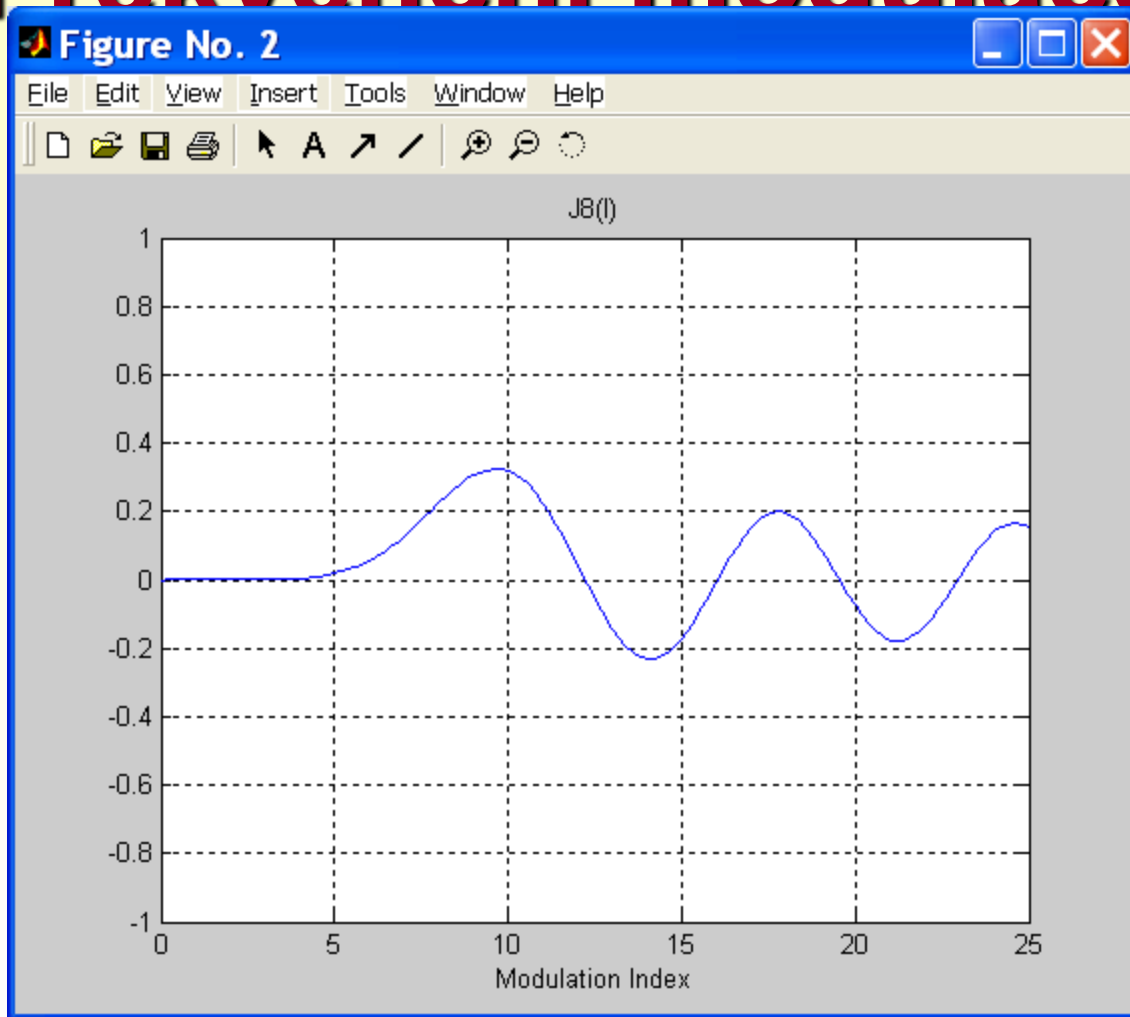
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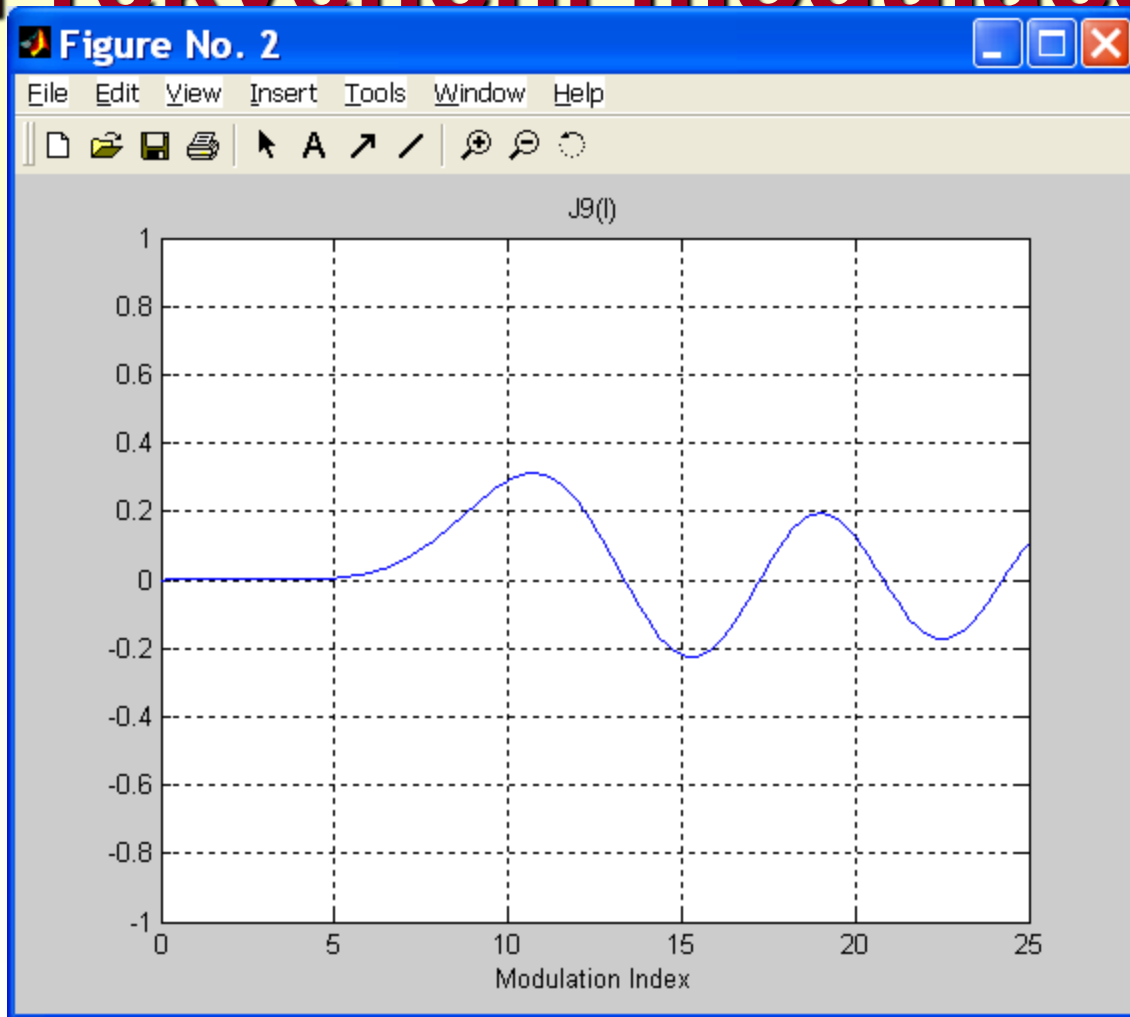
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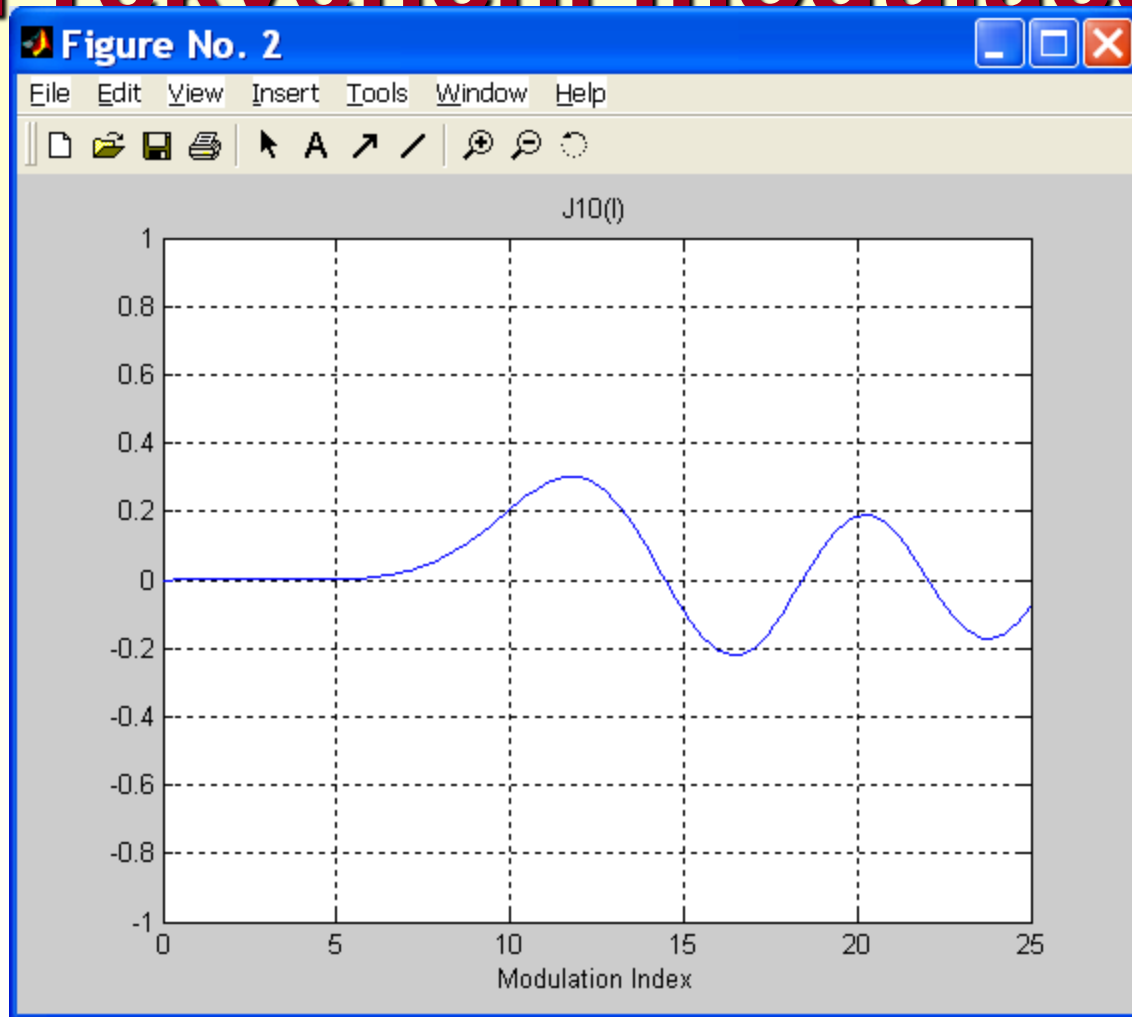
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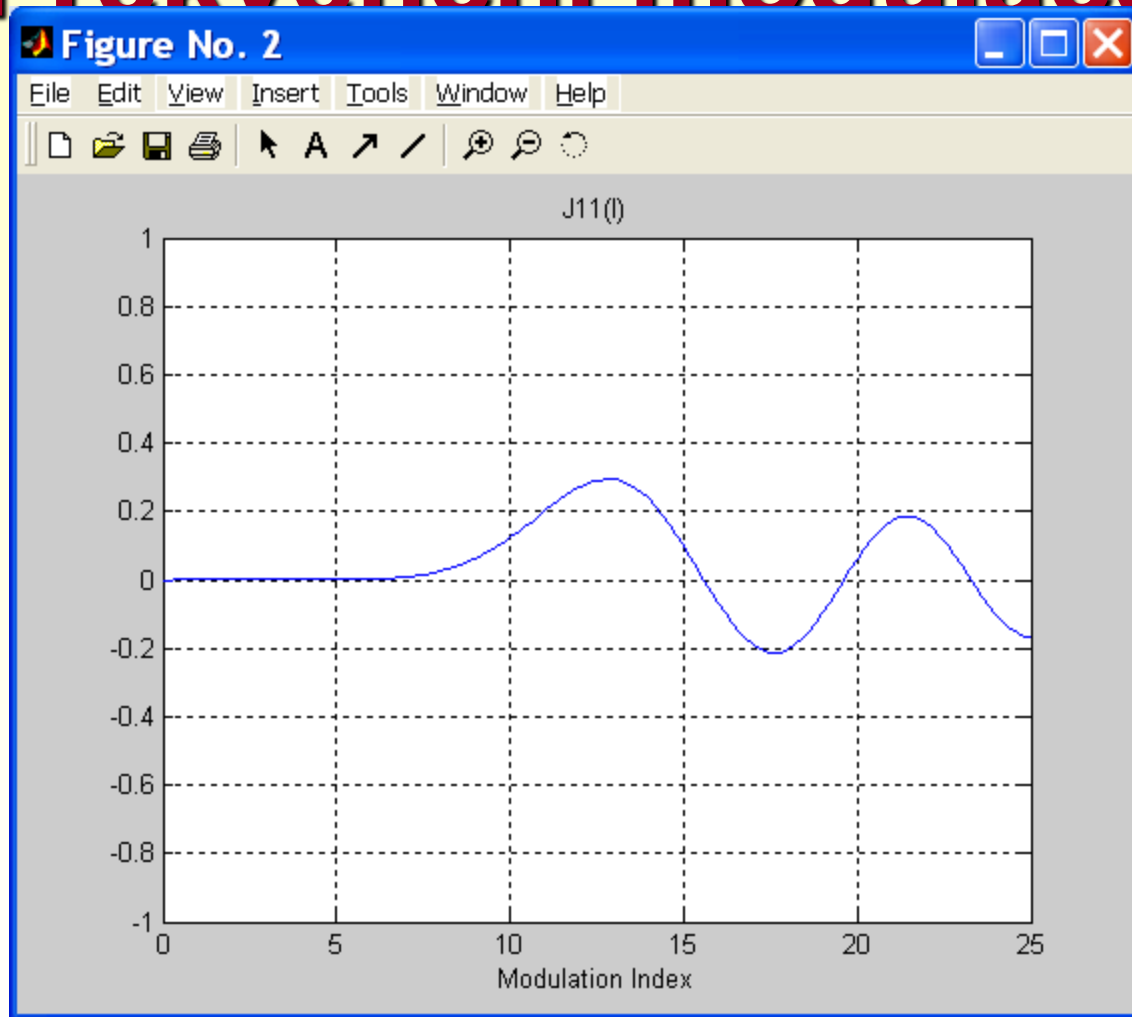
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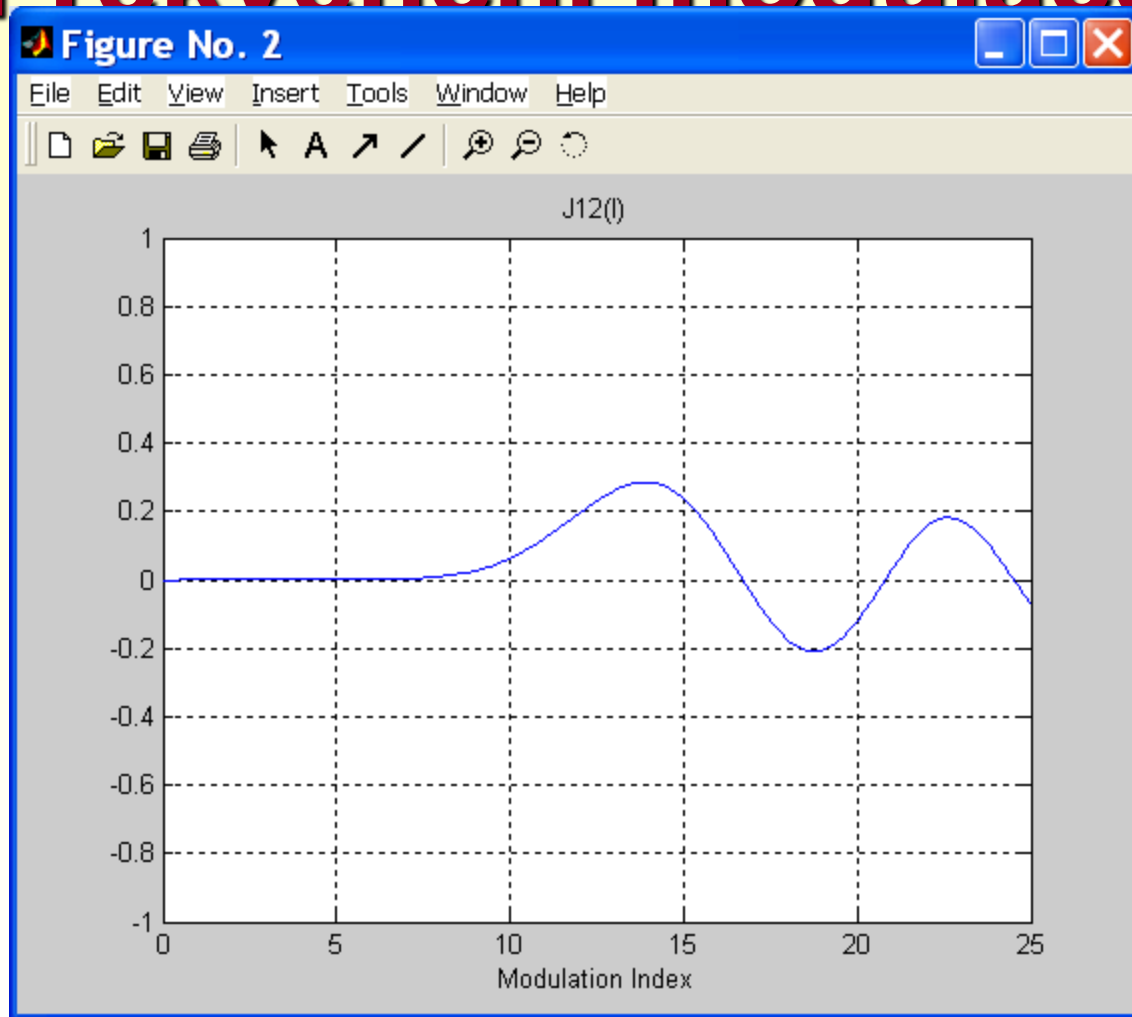
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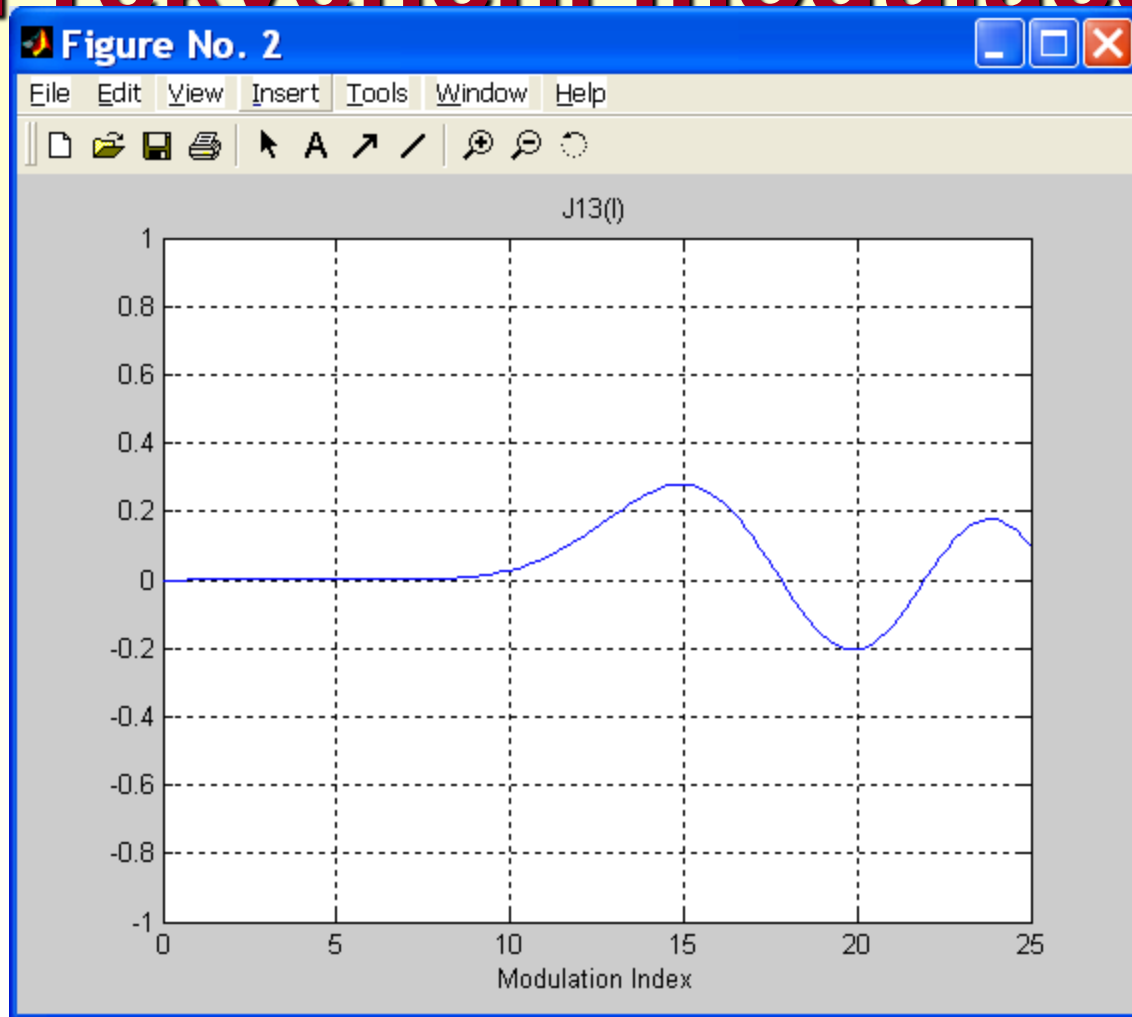
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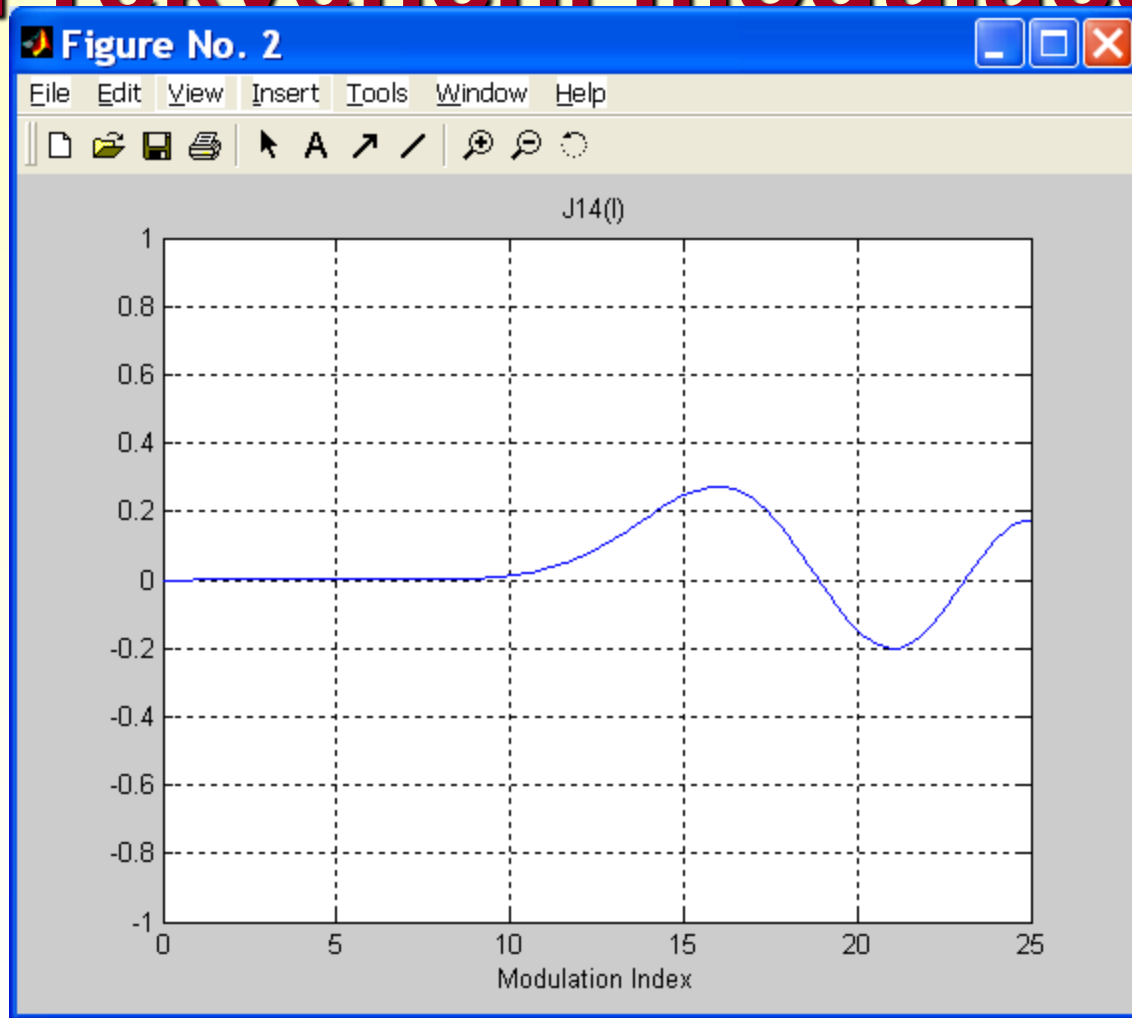
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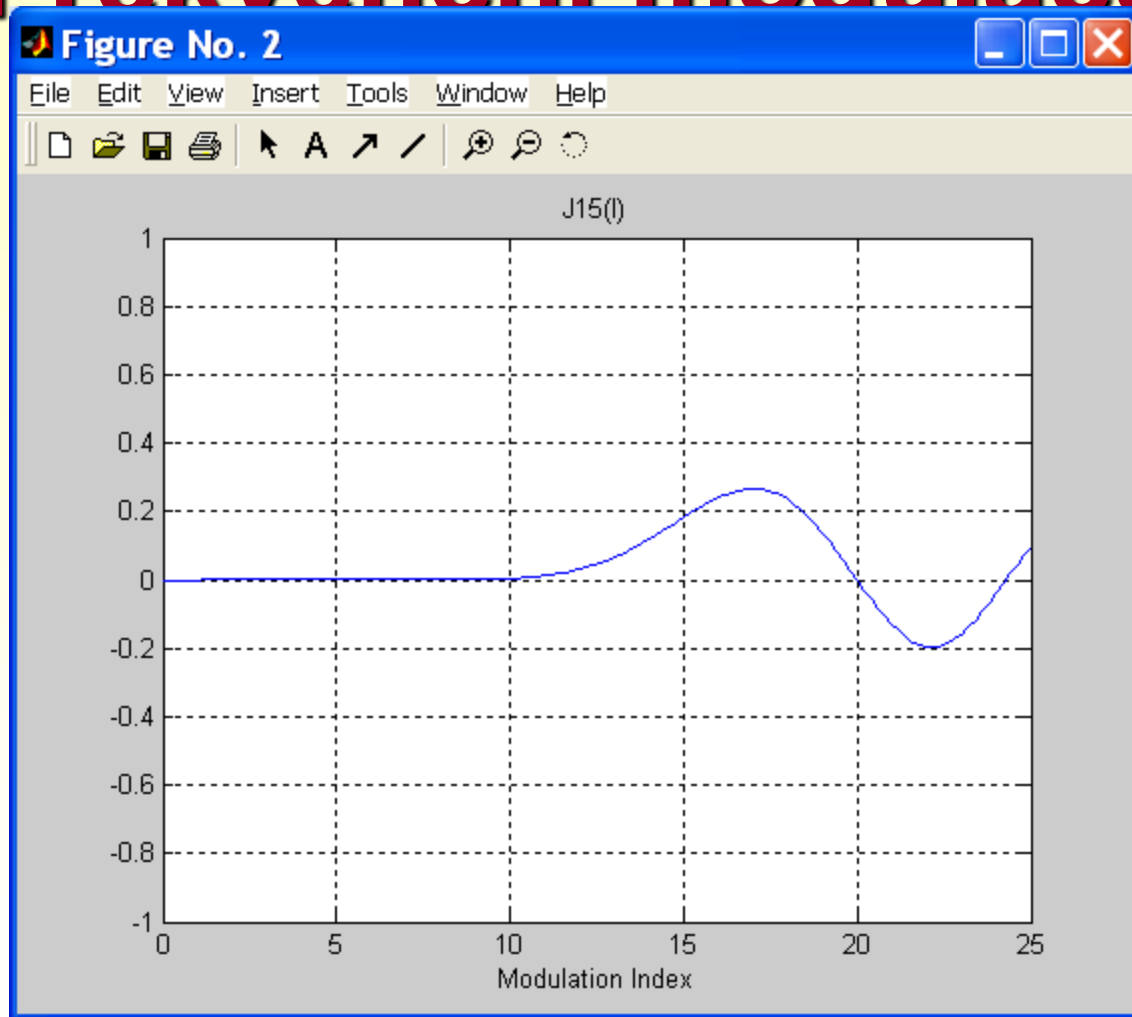
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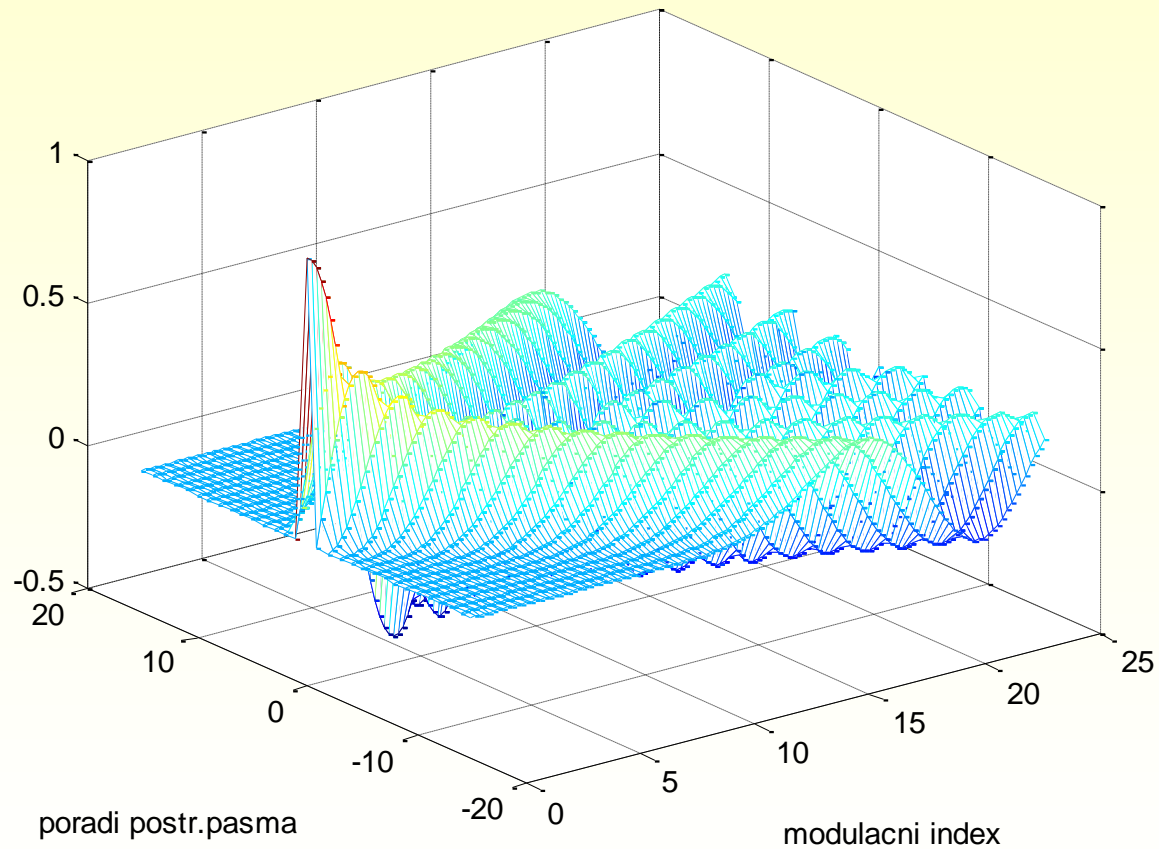
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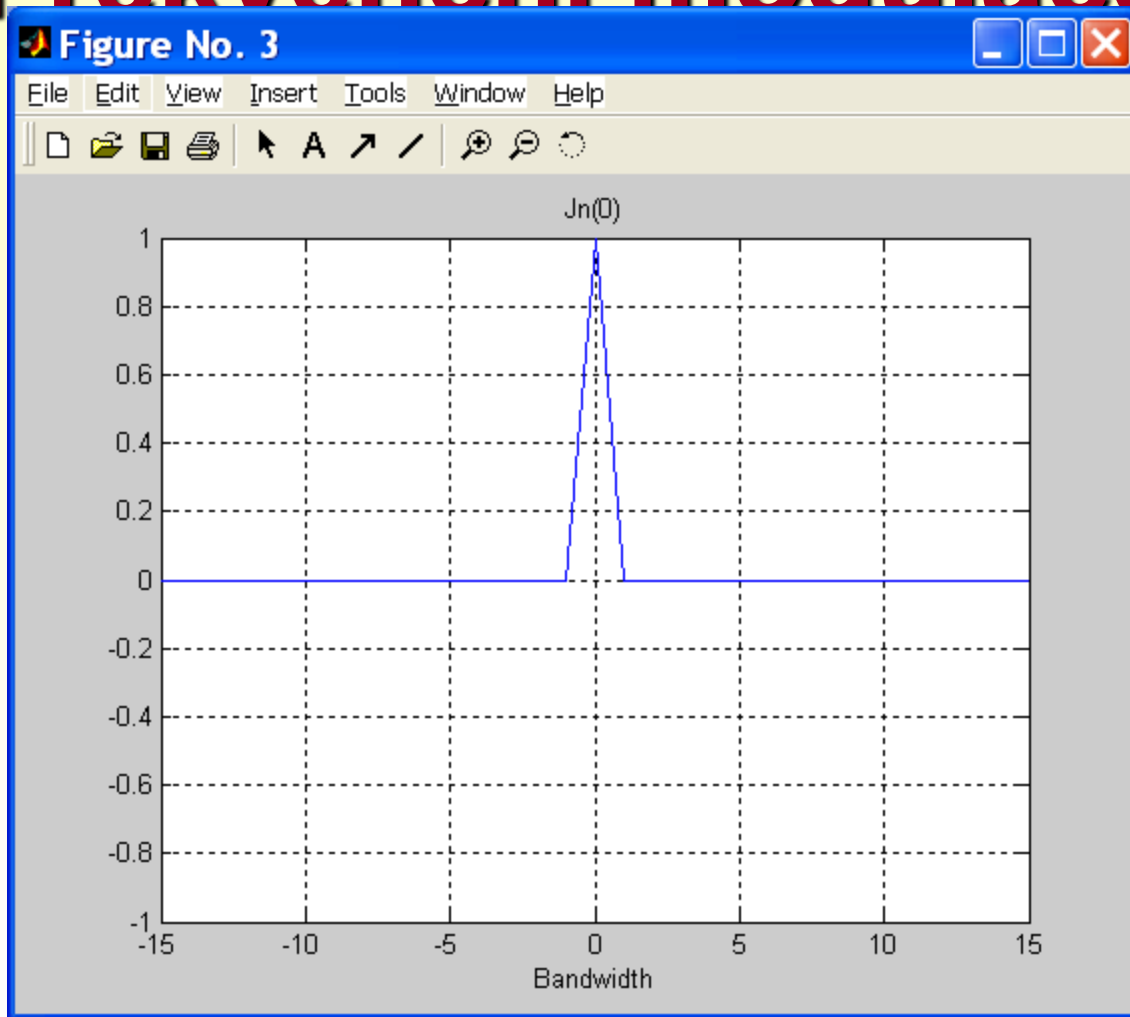
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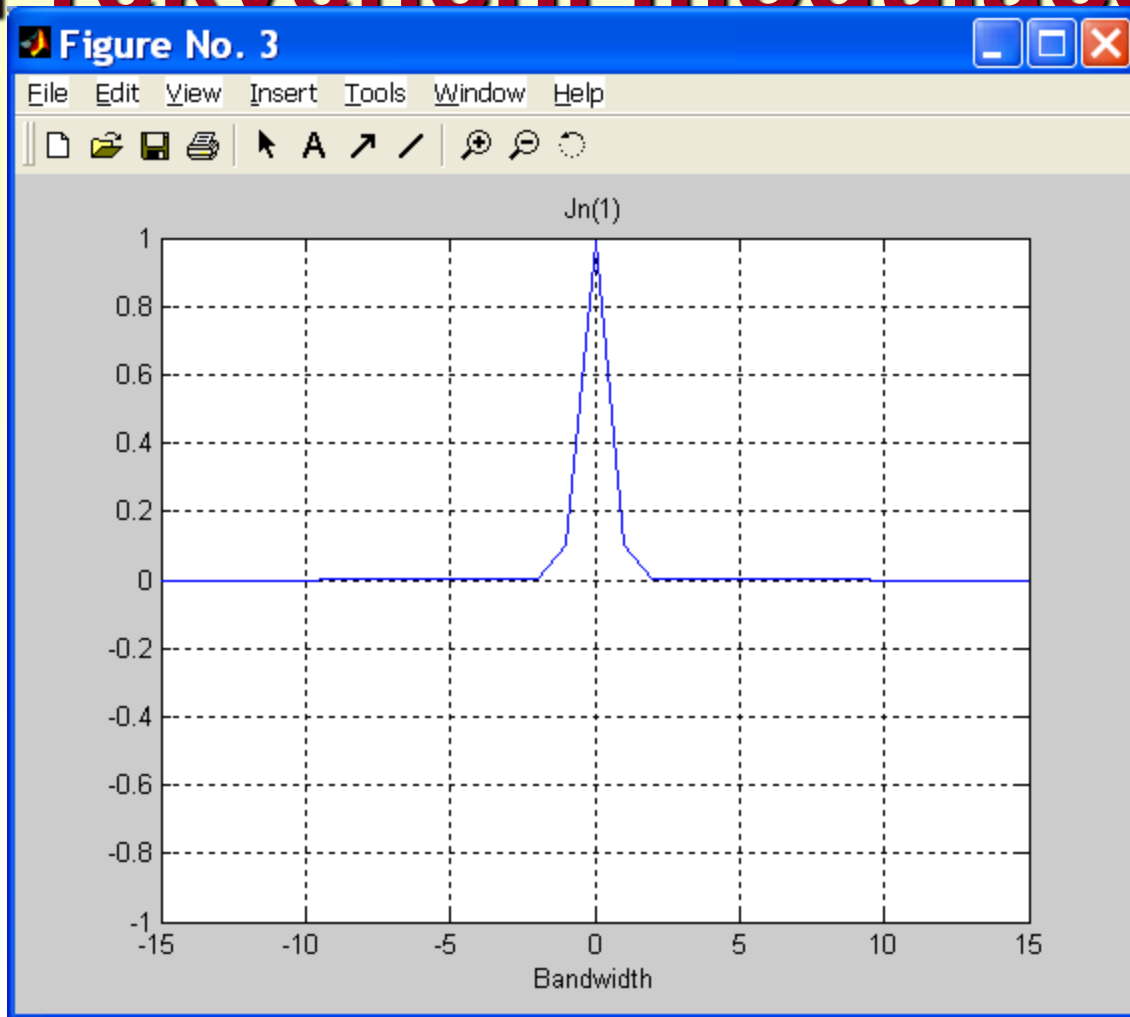
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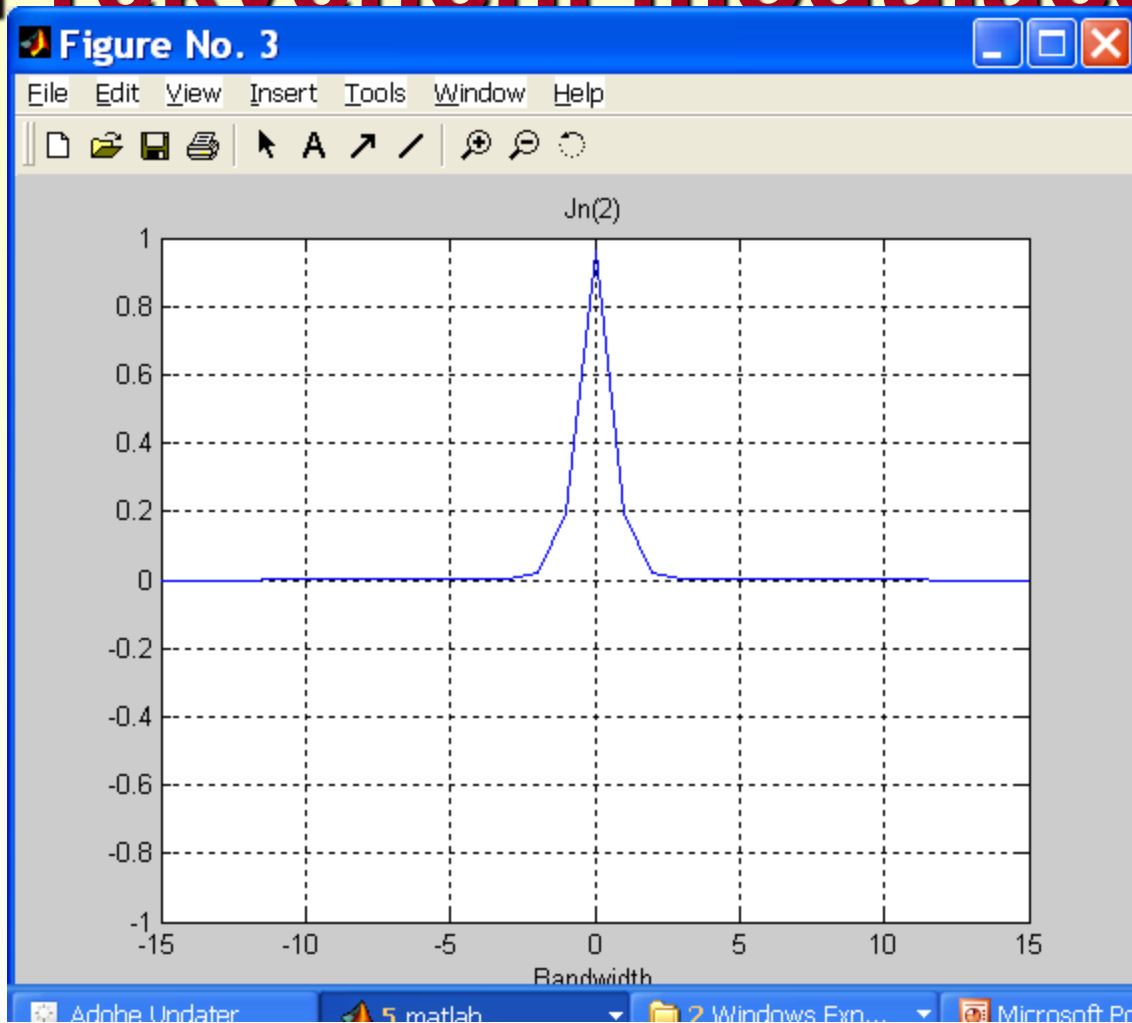
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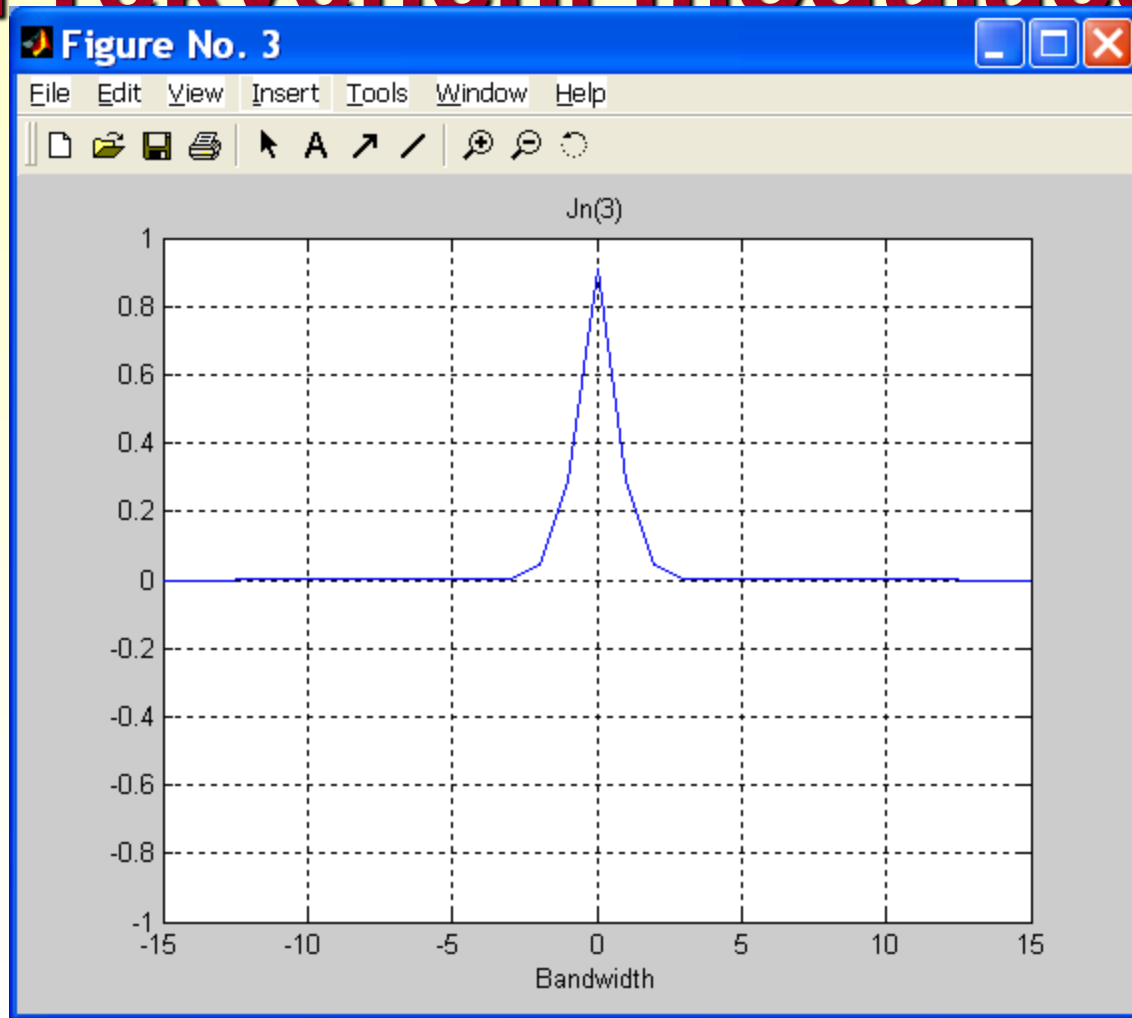
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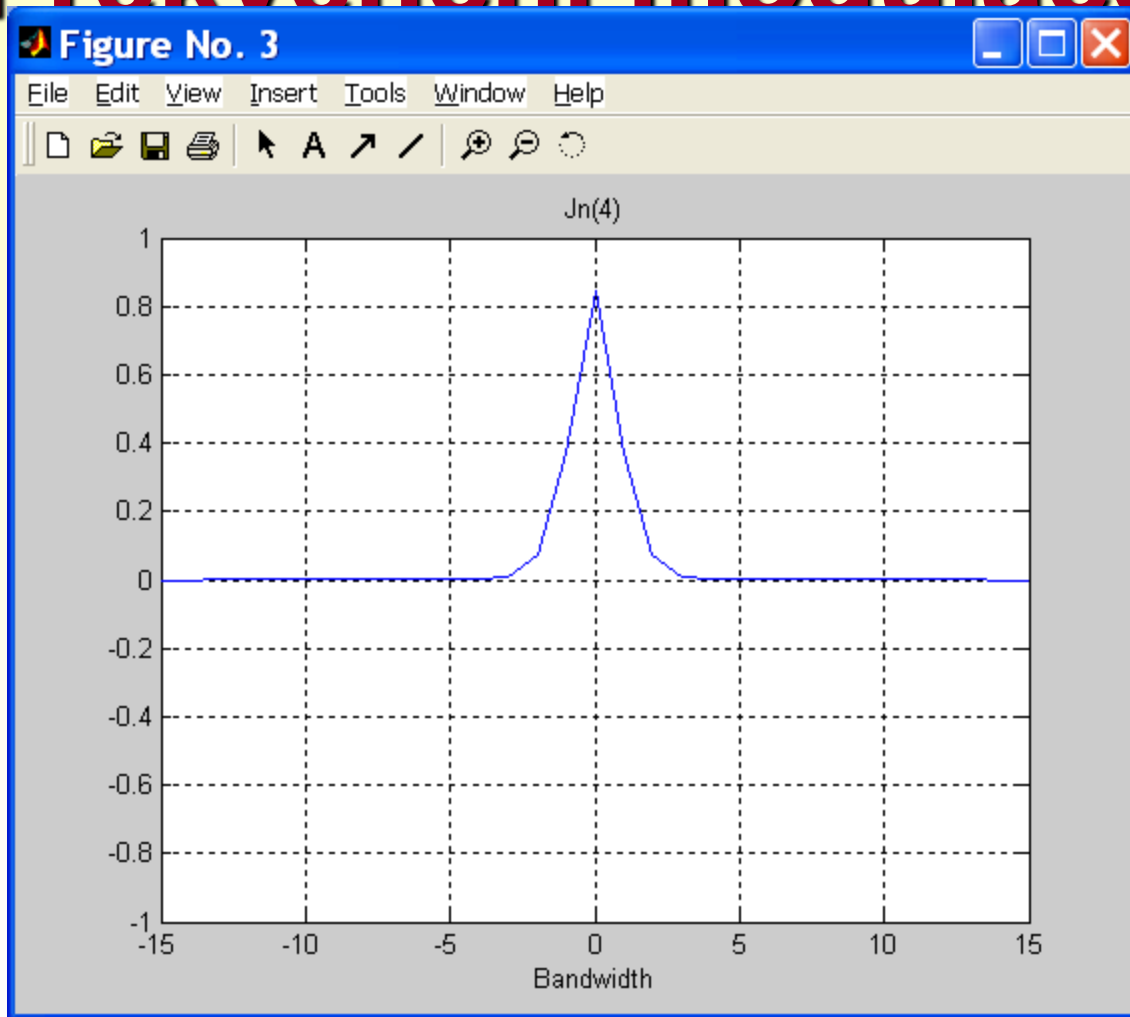
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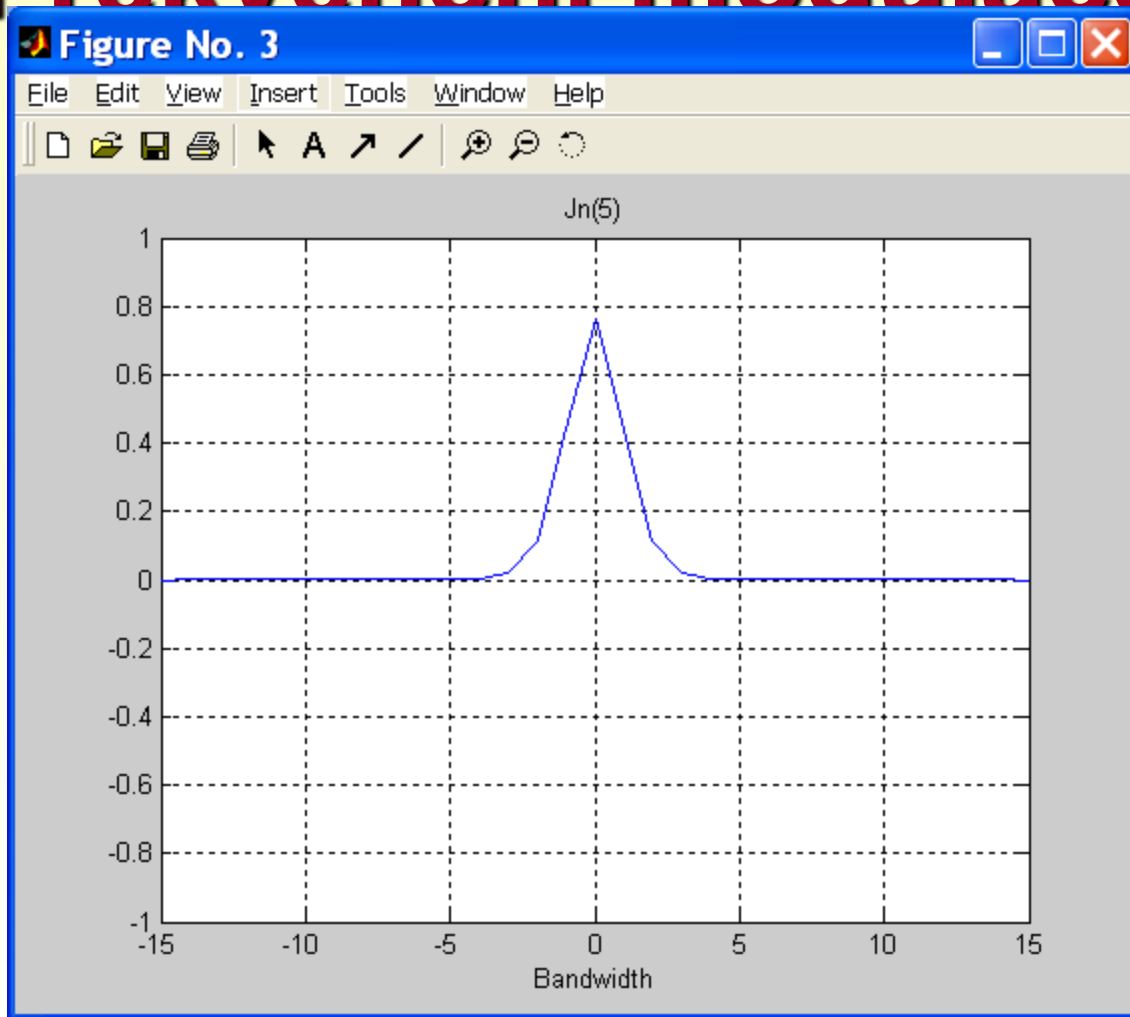
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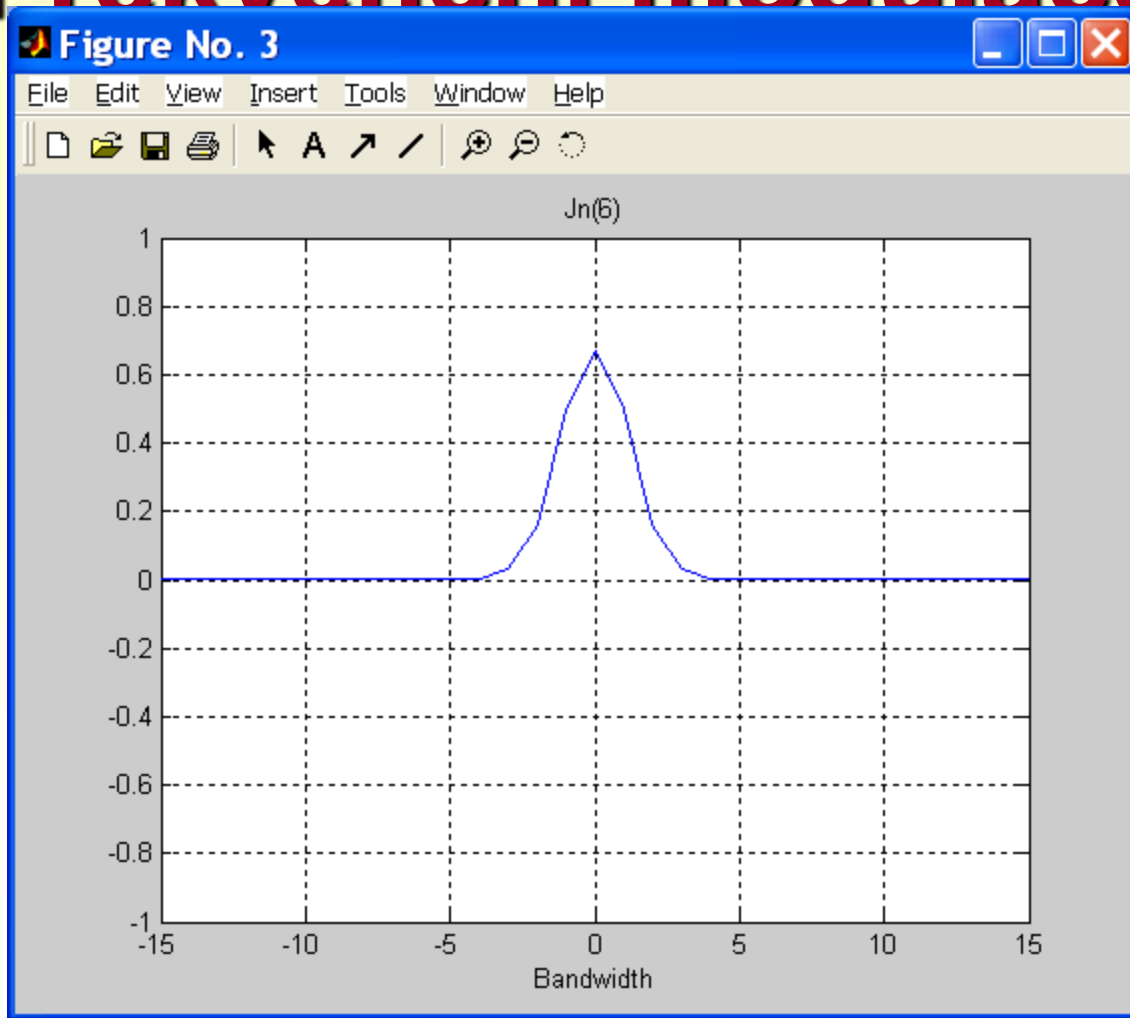
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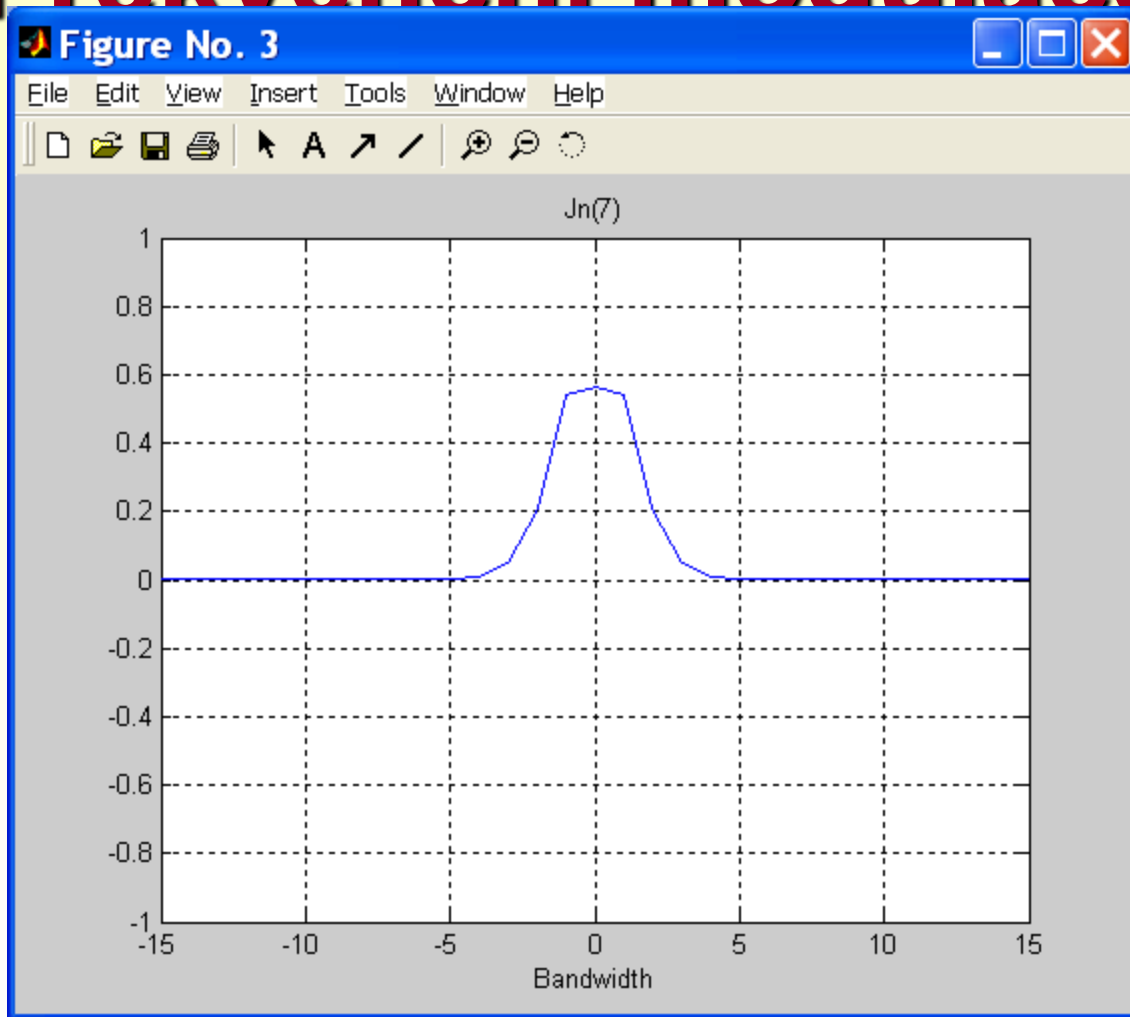
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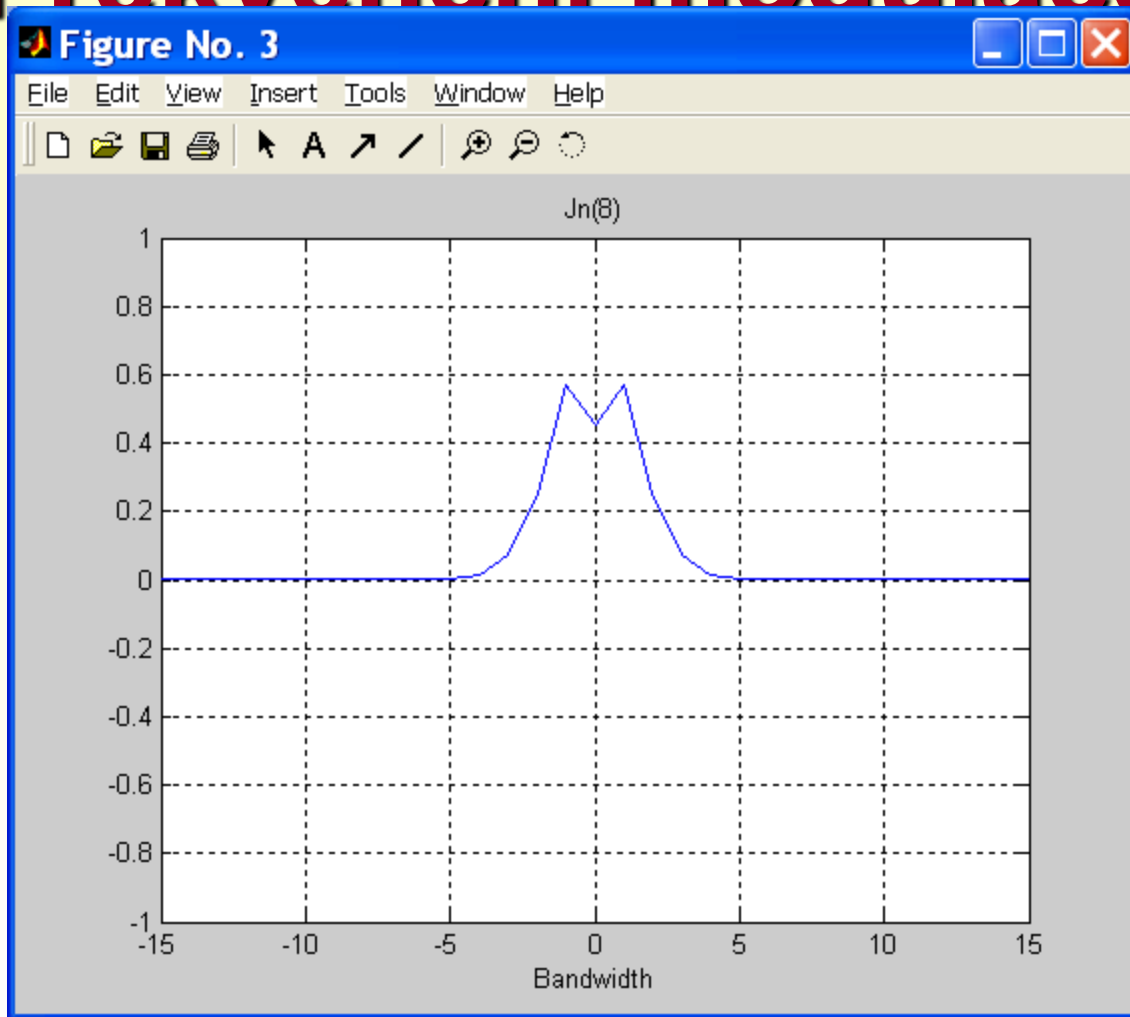
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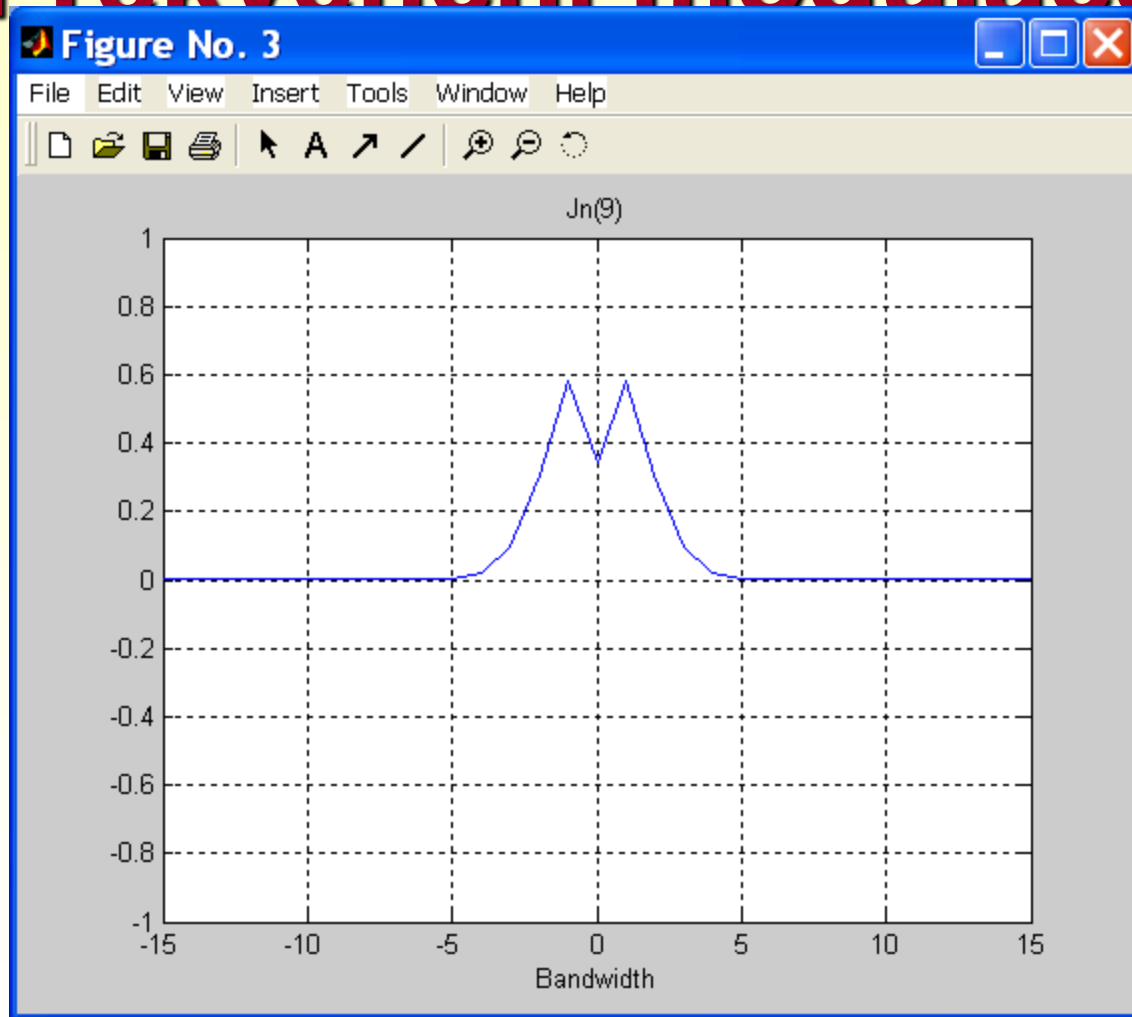
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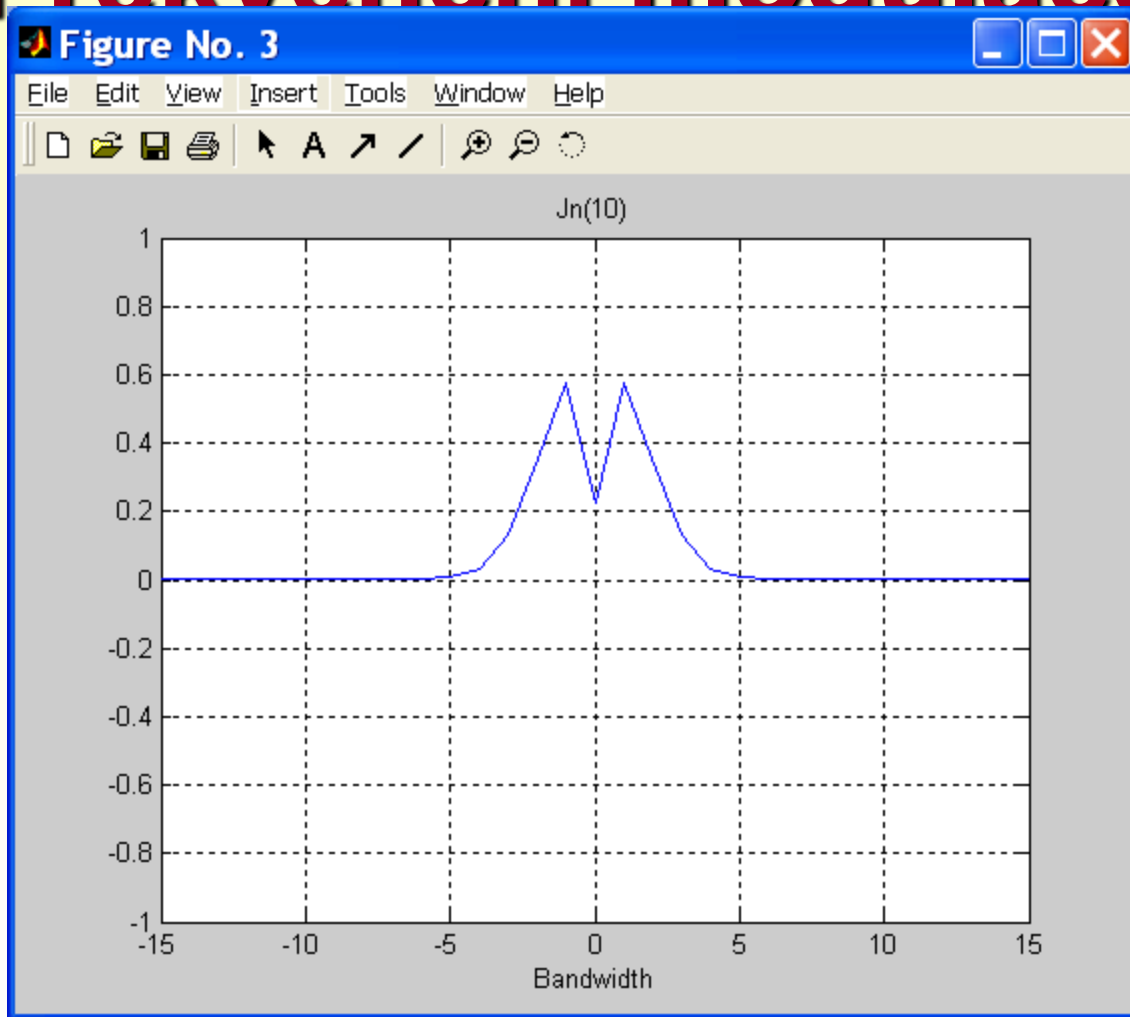
Frekvenční modulace



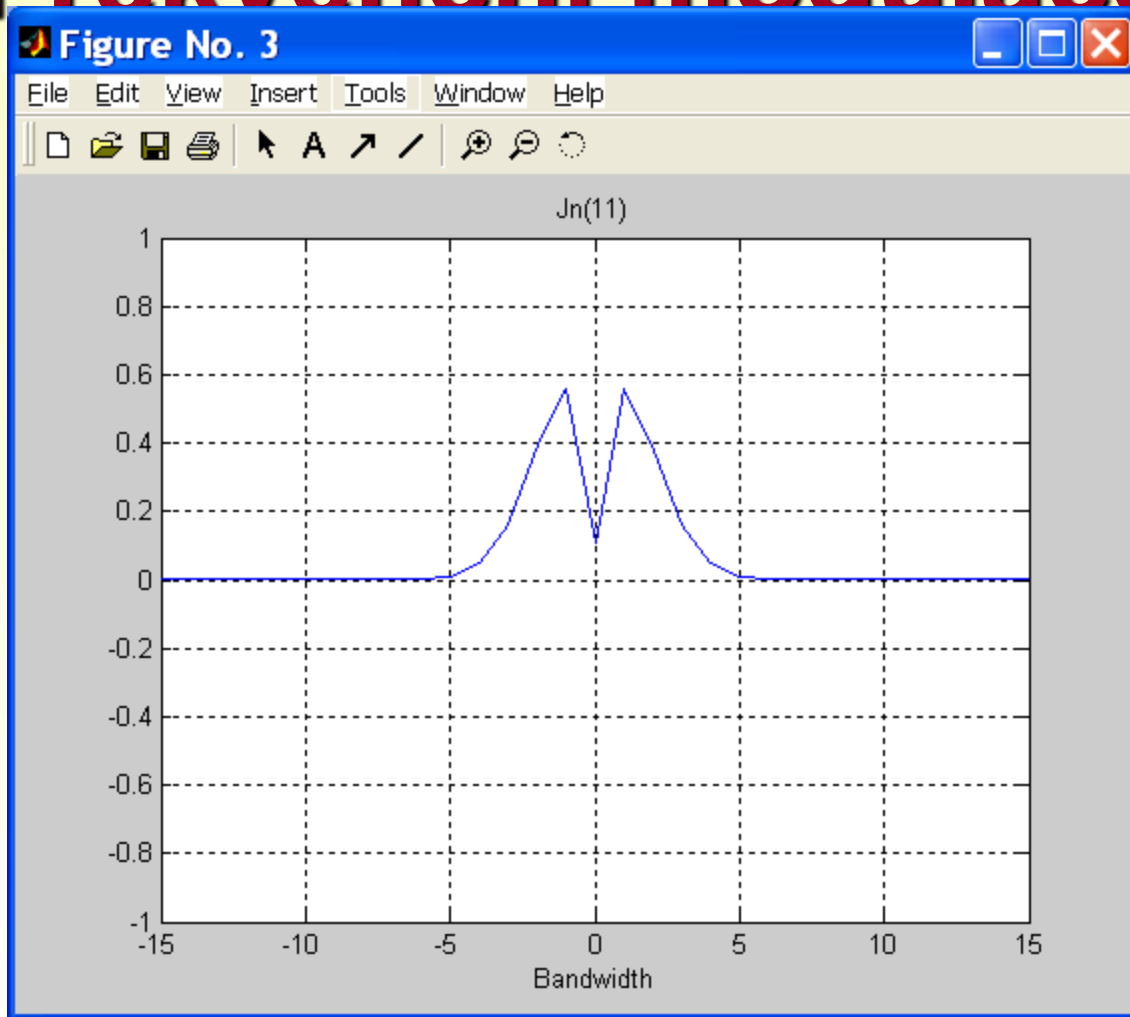
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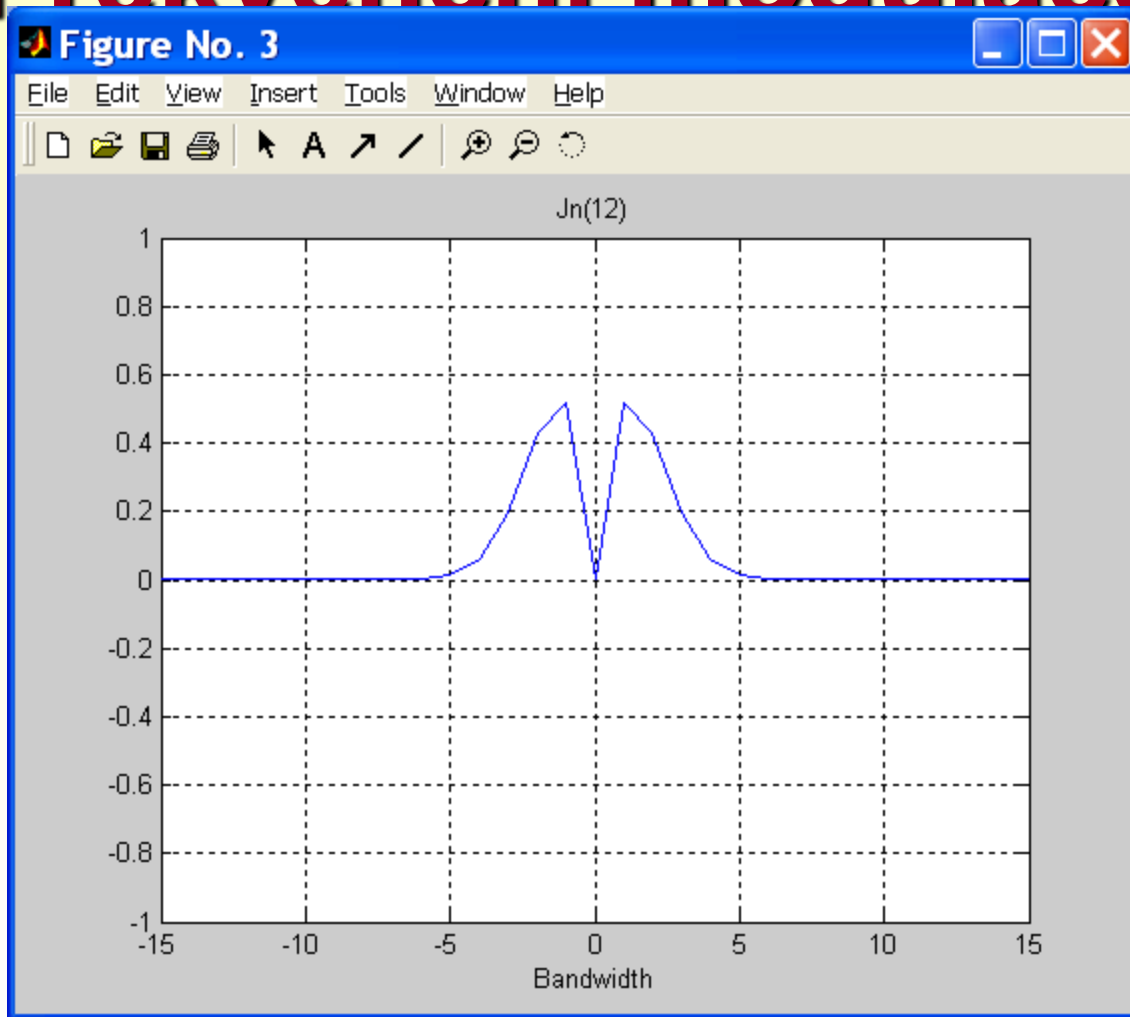
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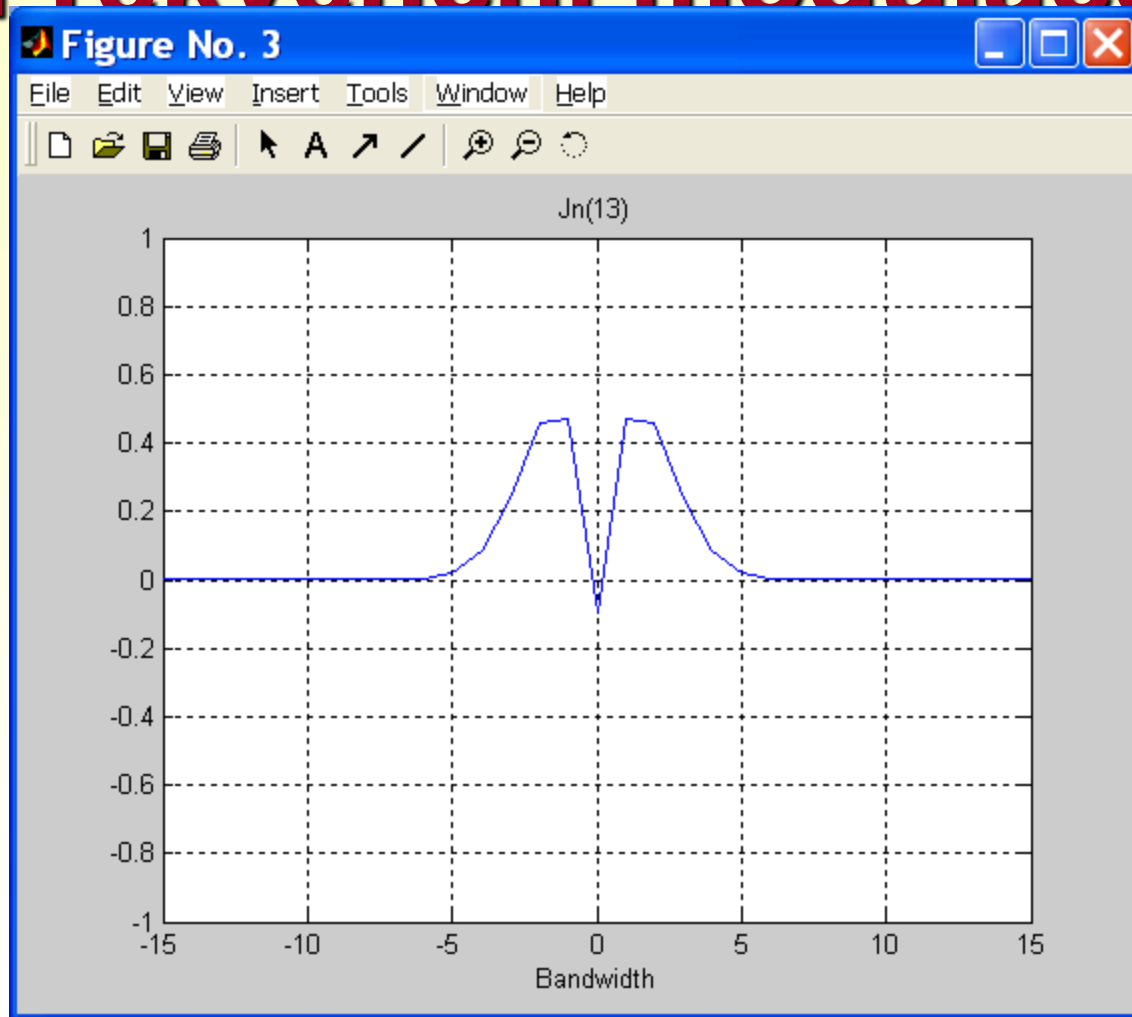
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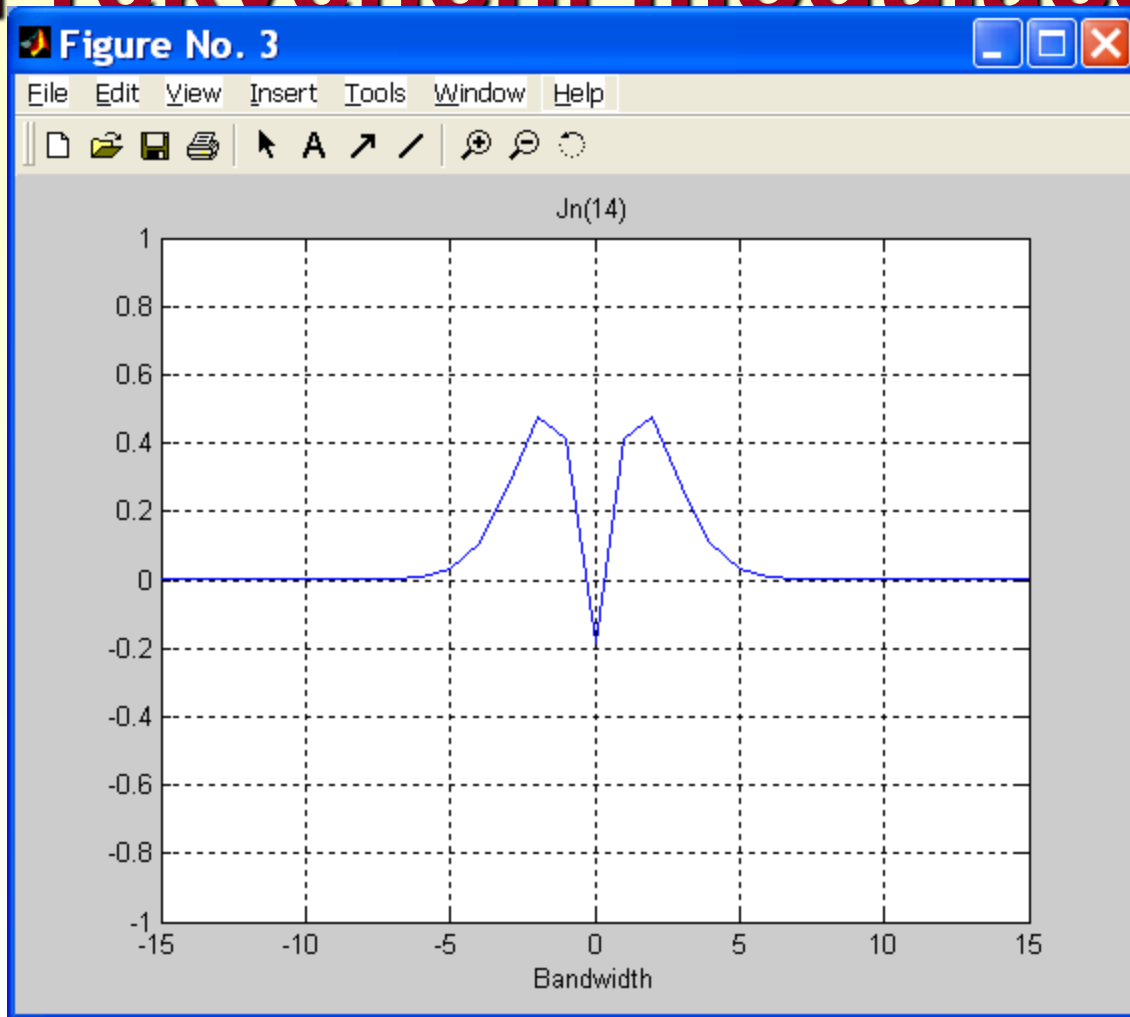
Frekvenční modulace



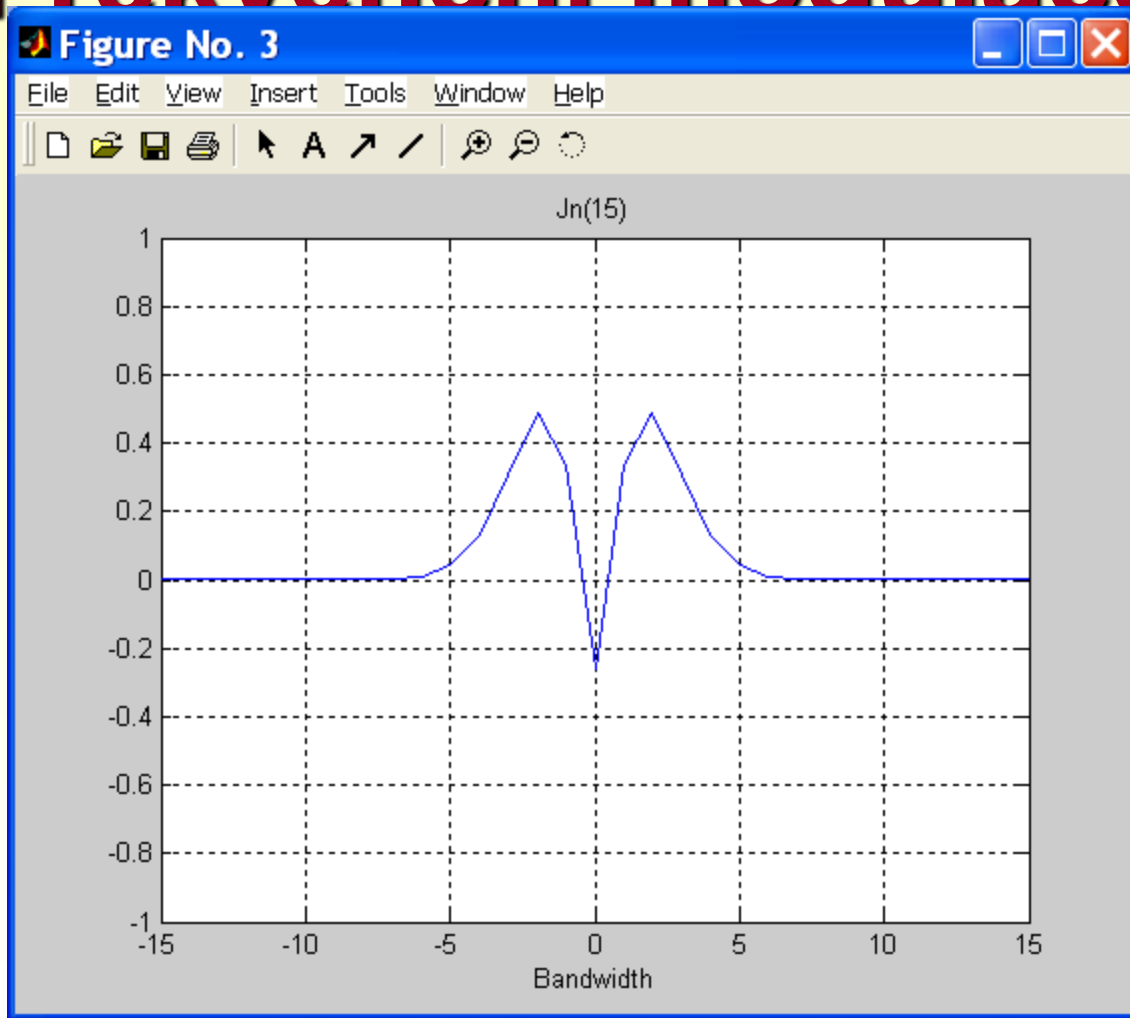
Frekvenční modulace



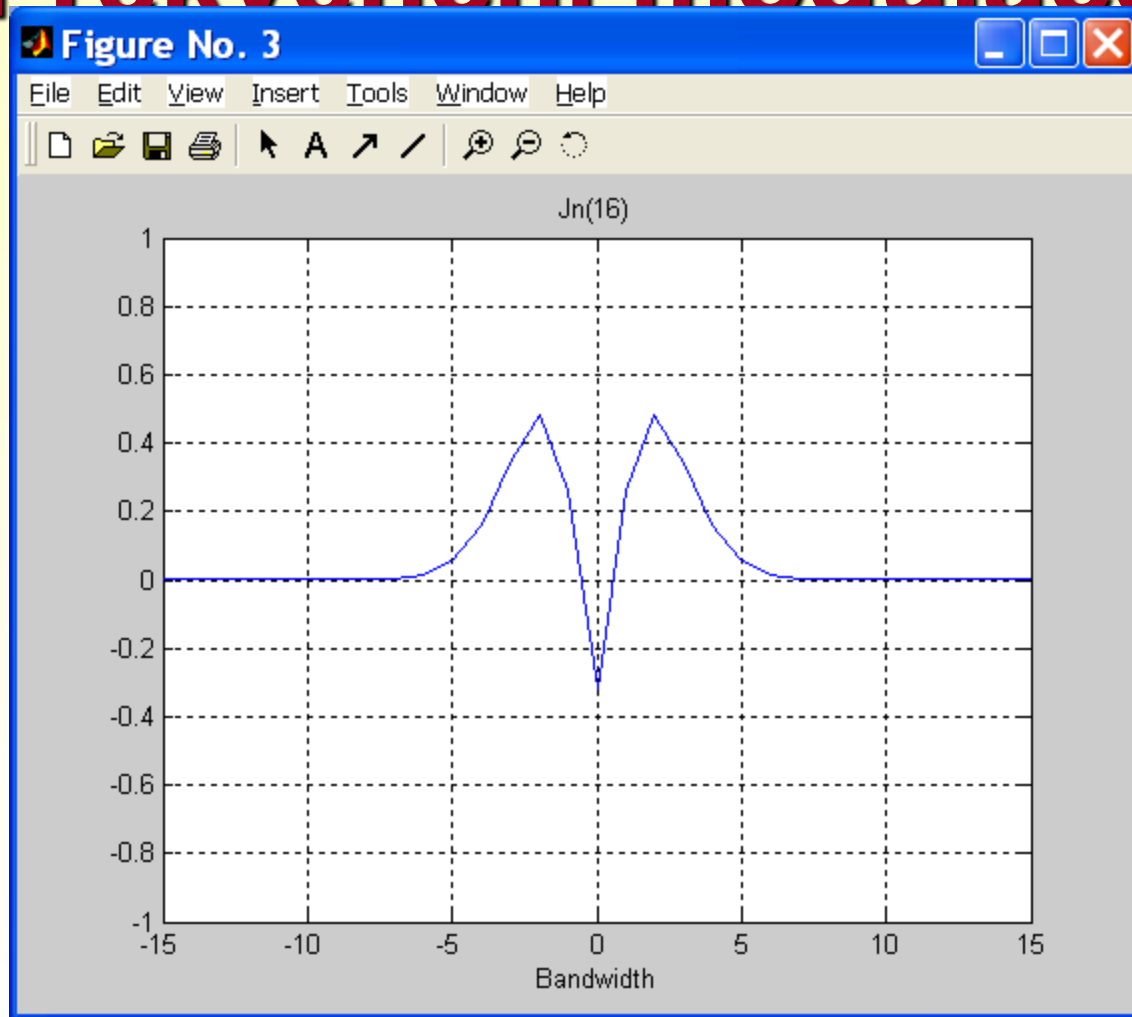
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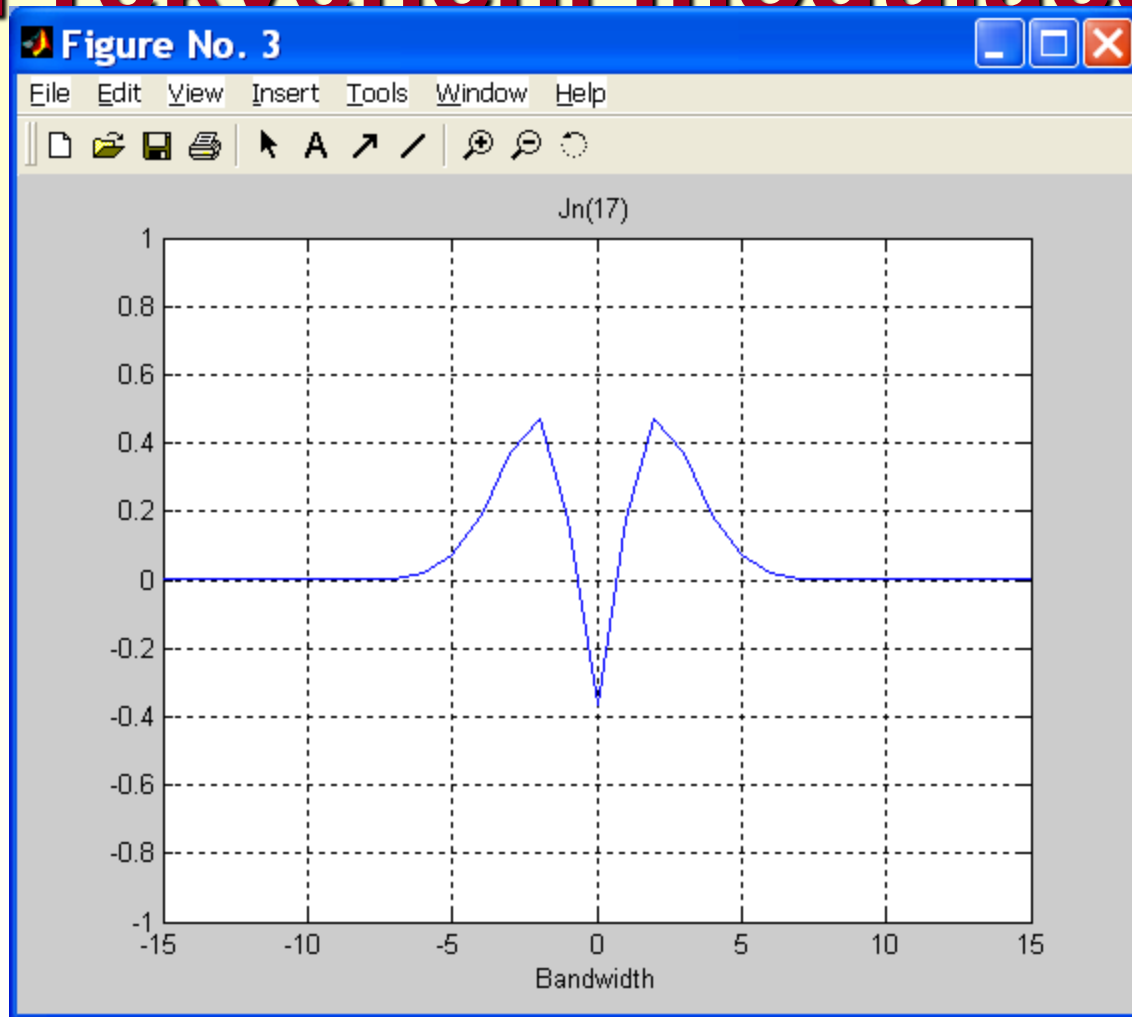
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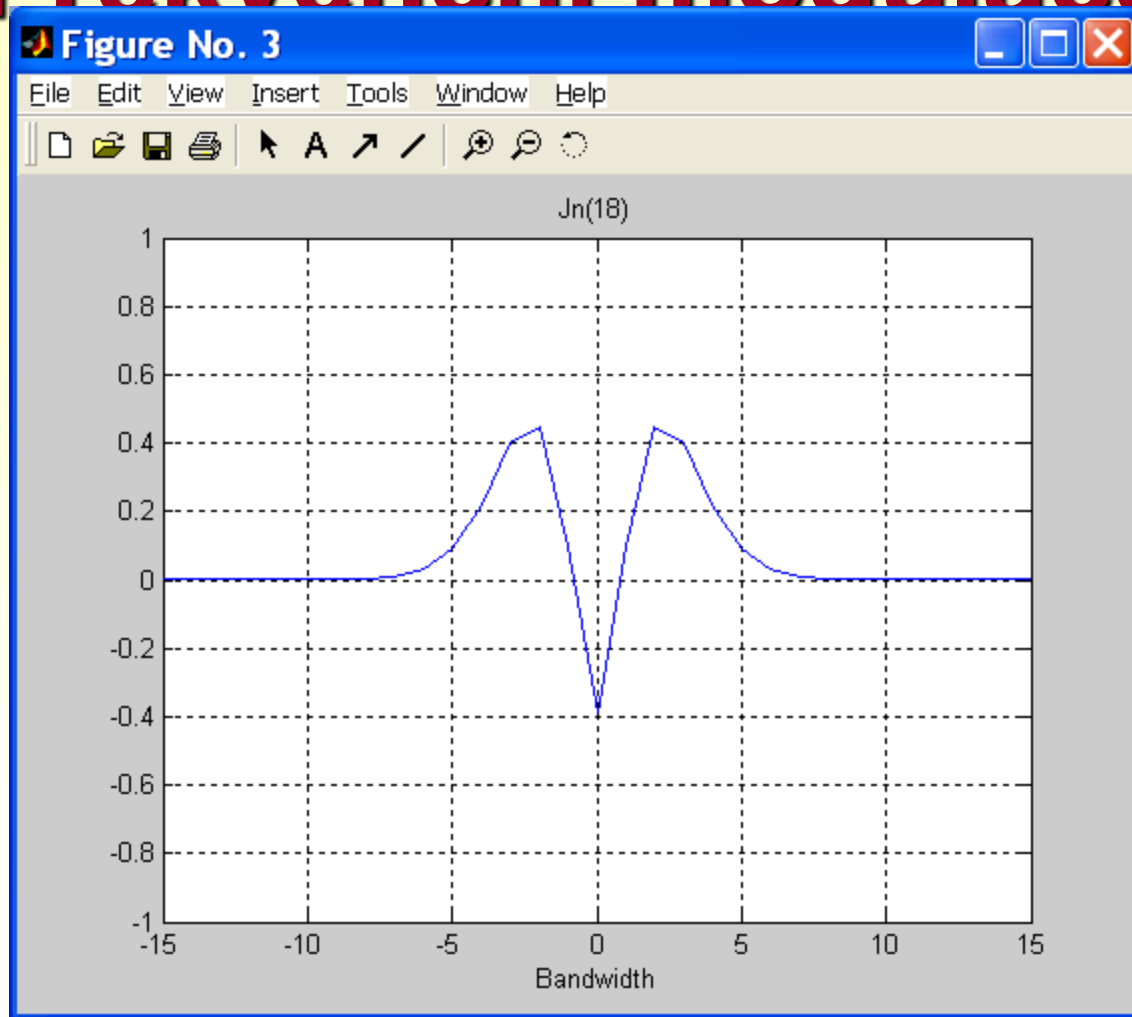
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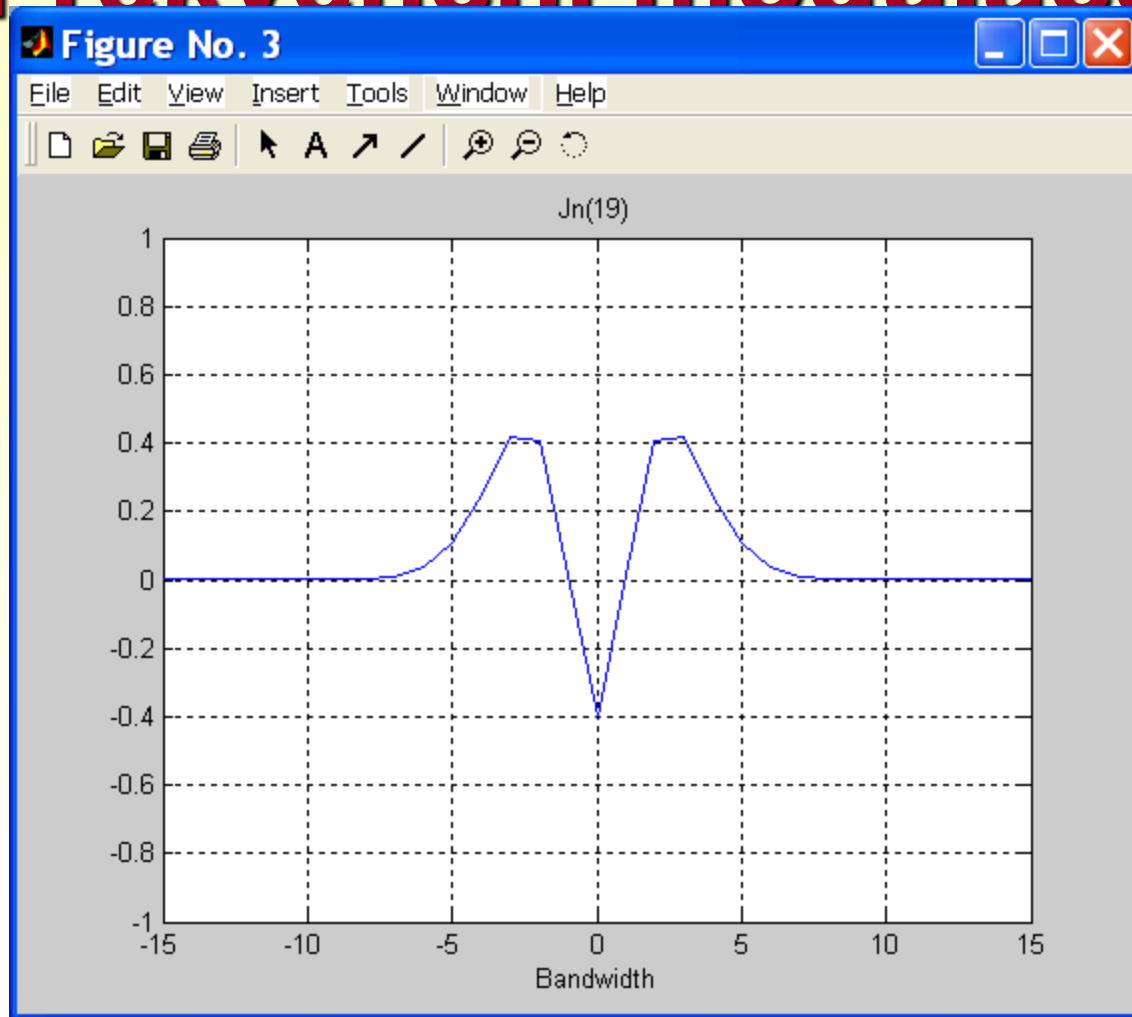
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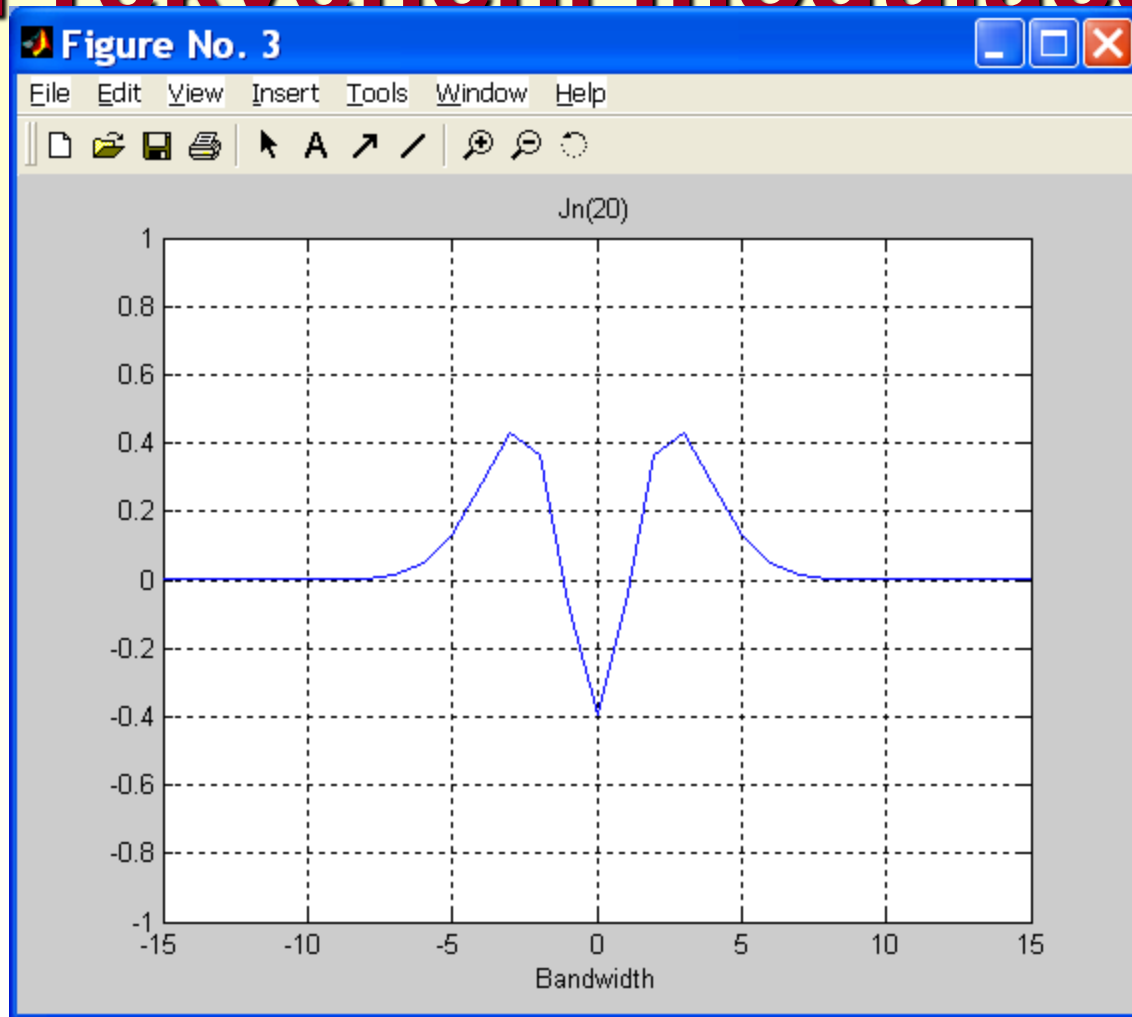
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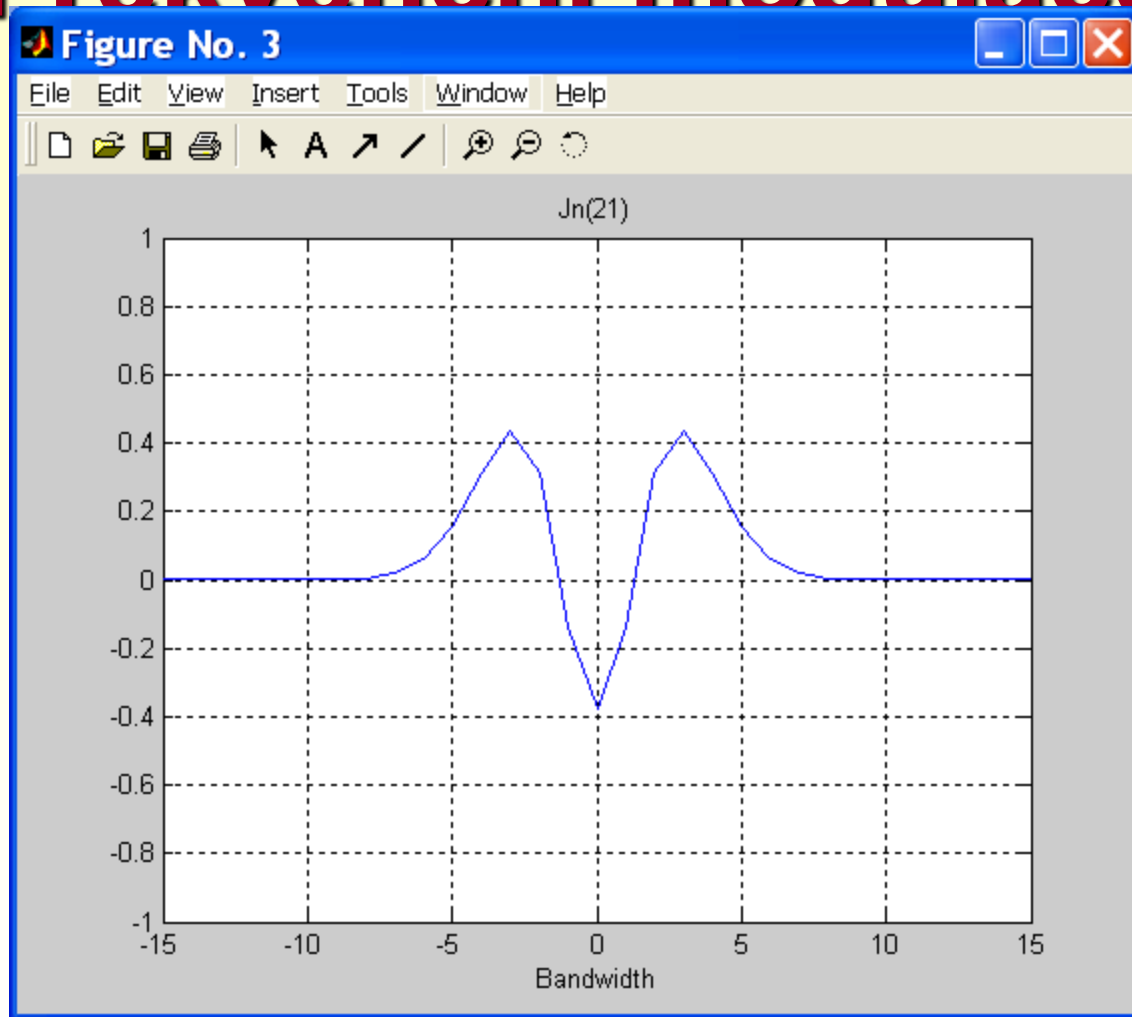
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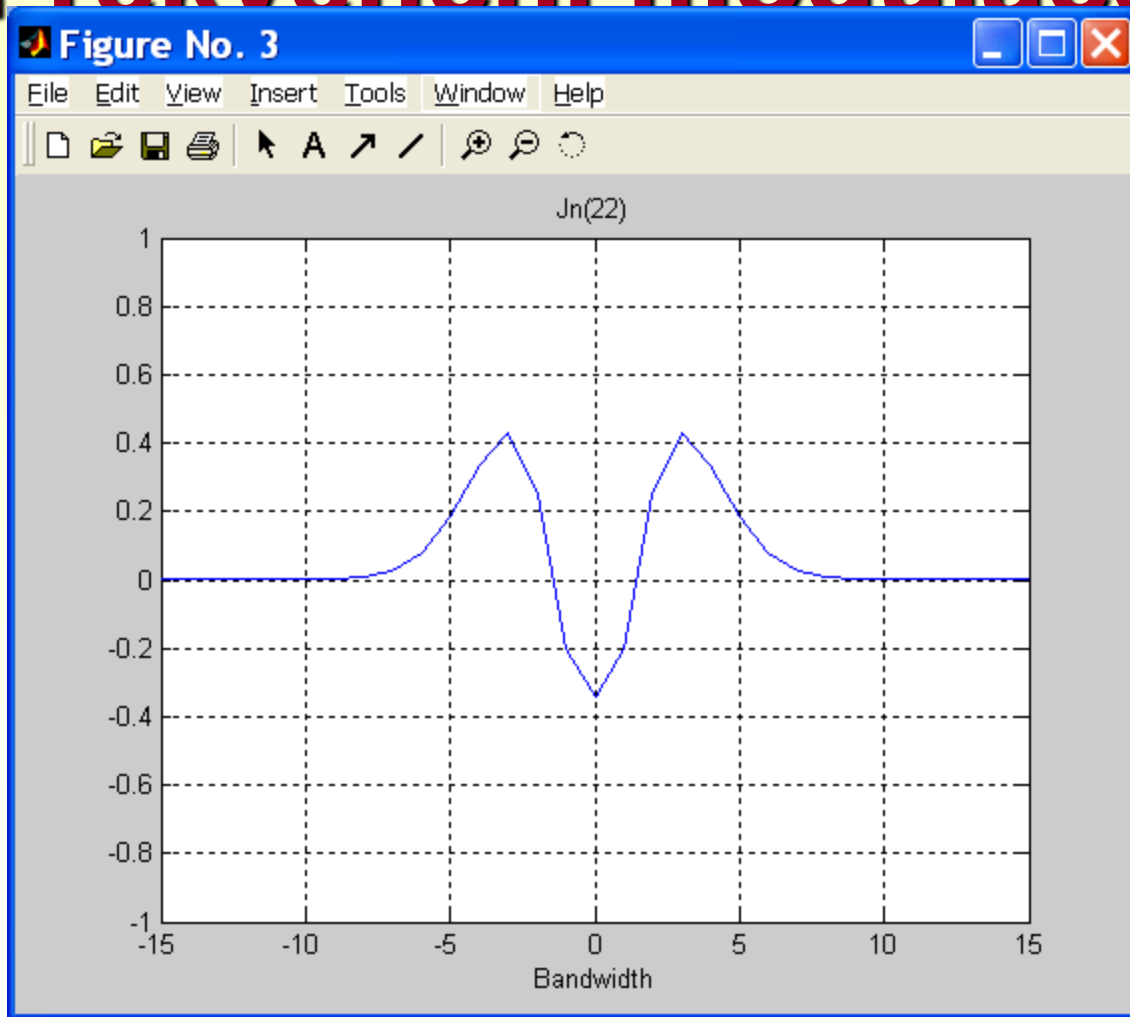
Frekvenční modulace



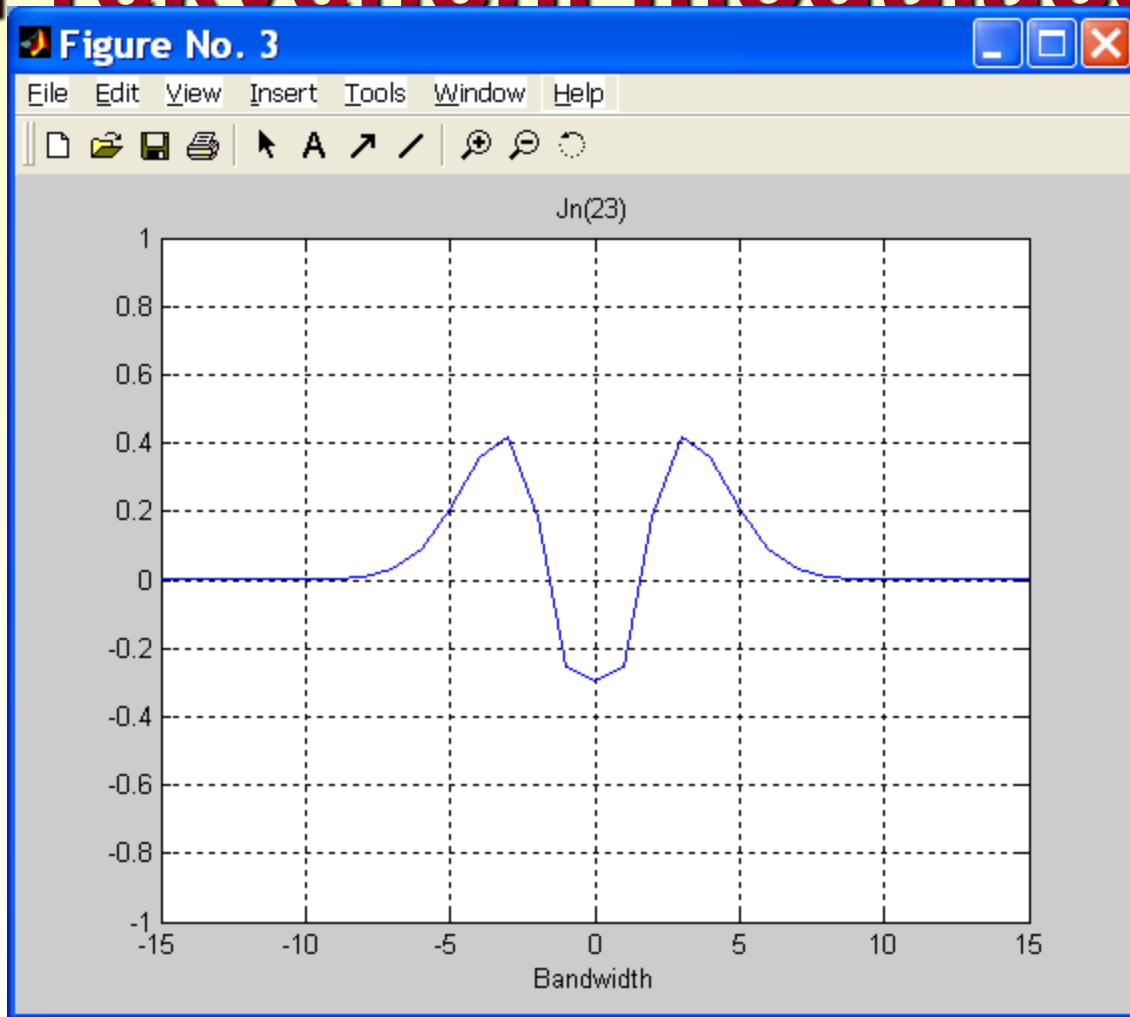
Frekvenční modulace



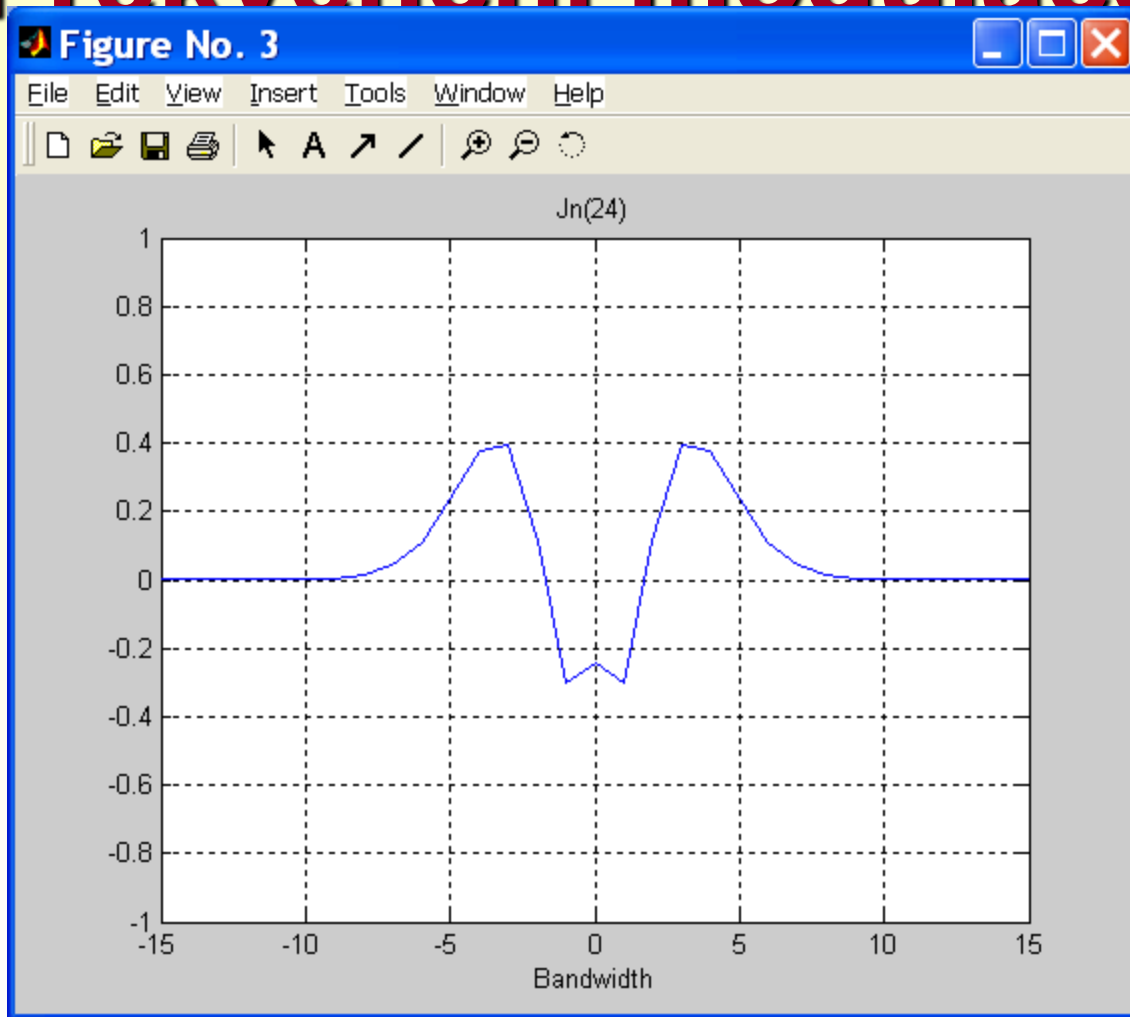
Frekvenční modulace



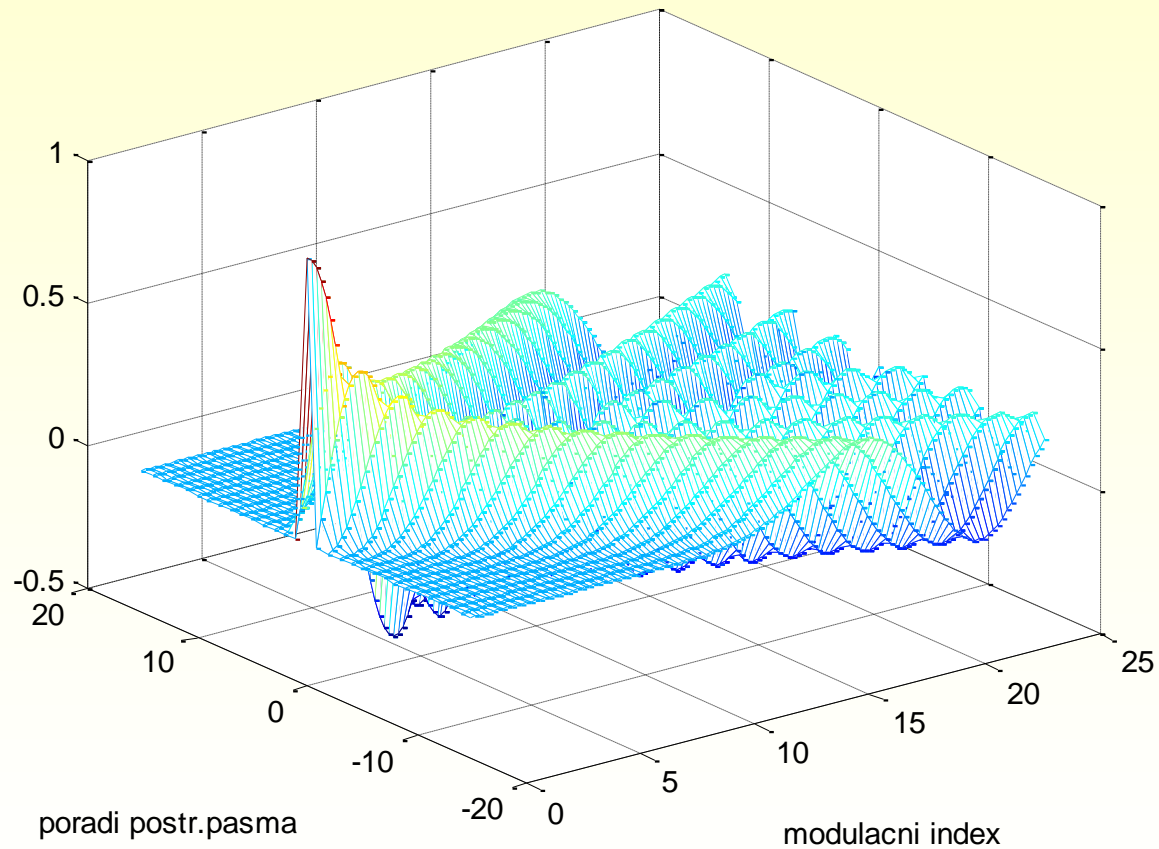
Frekvenční modulace



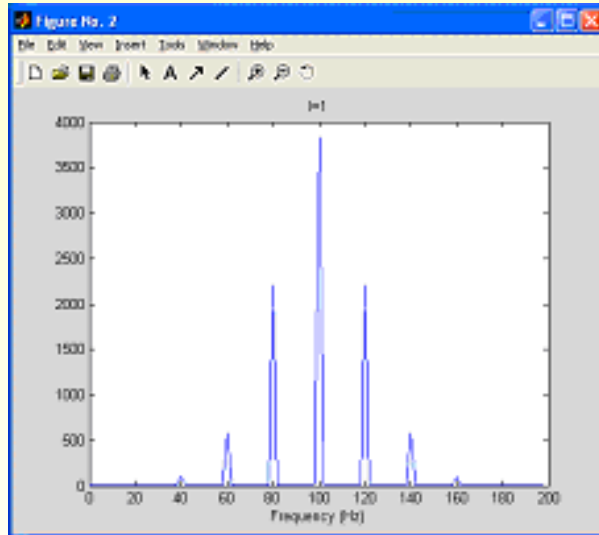
Frekvenční modulace



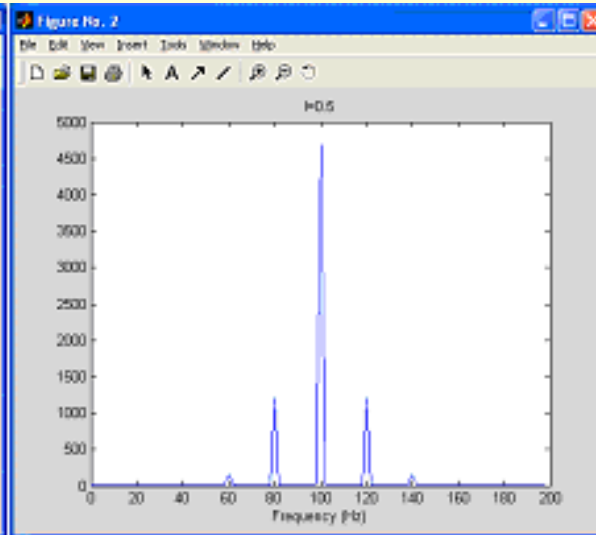
Frekvenční modulace



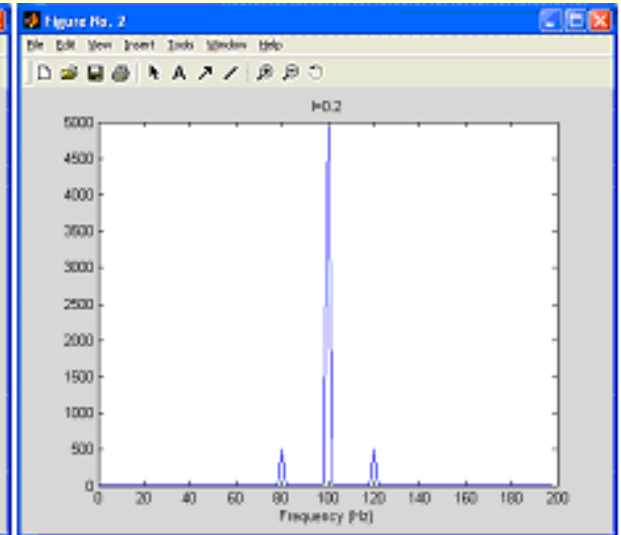
Frekvenční modulace



$I=1$

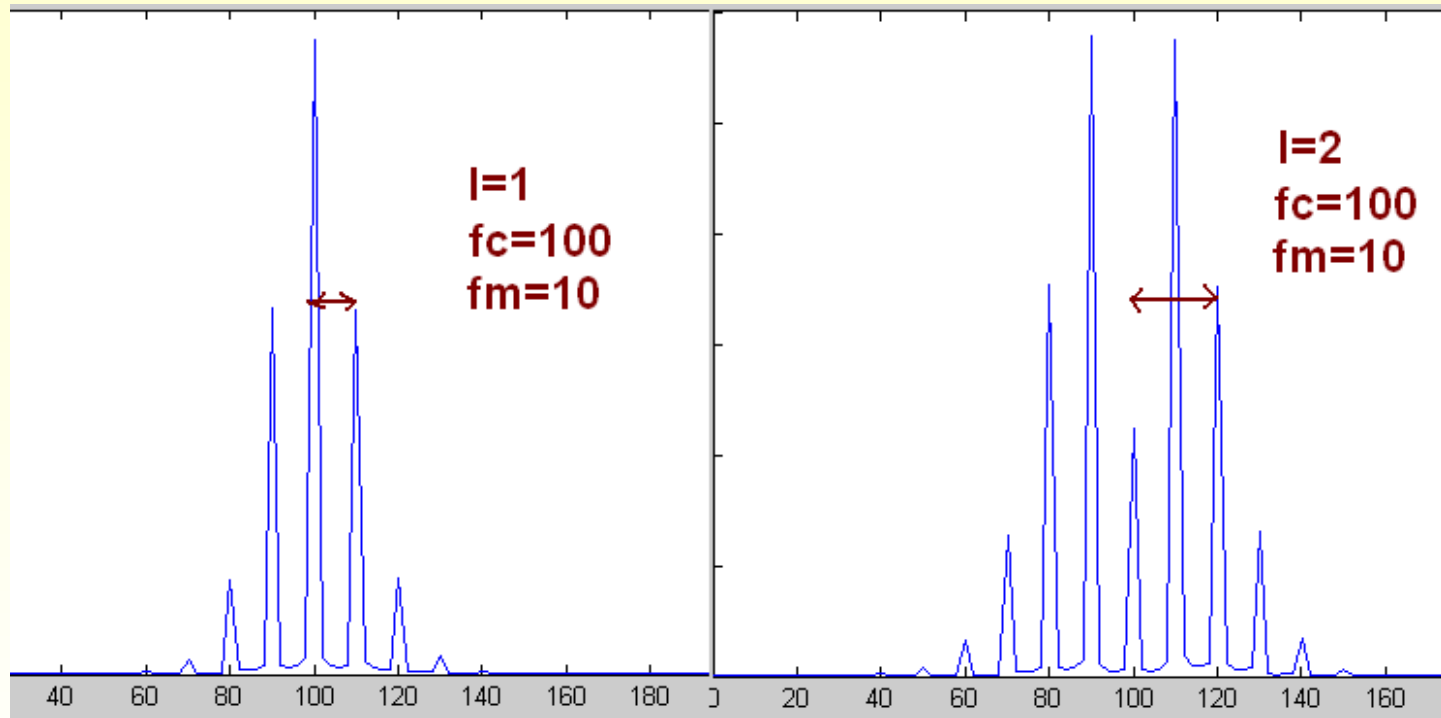


$I=0.5$

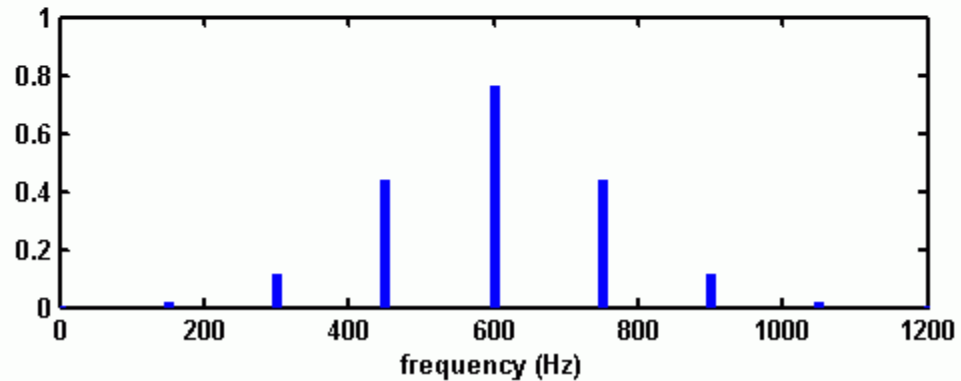
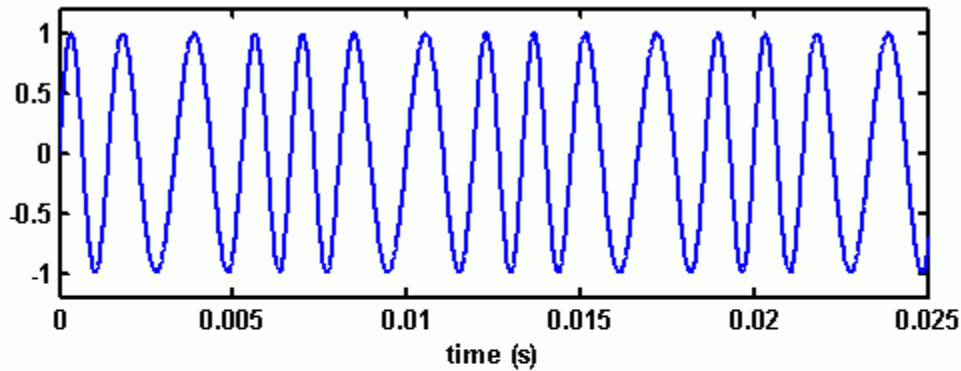


$I=0.1$

Frekvenční modulace



Frekvenční modulace



f_c f_m m_i

600

150

1



600

1

1



600

4

1



600

50

1



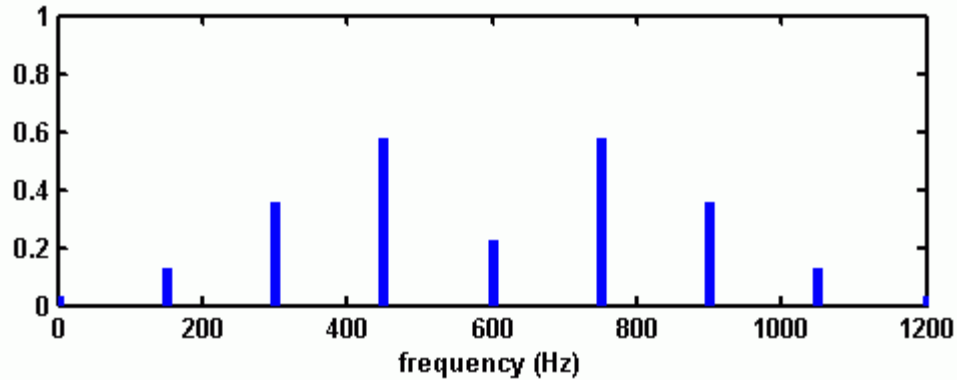
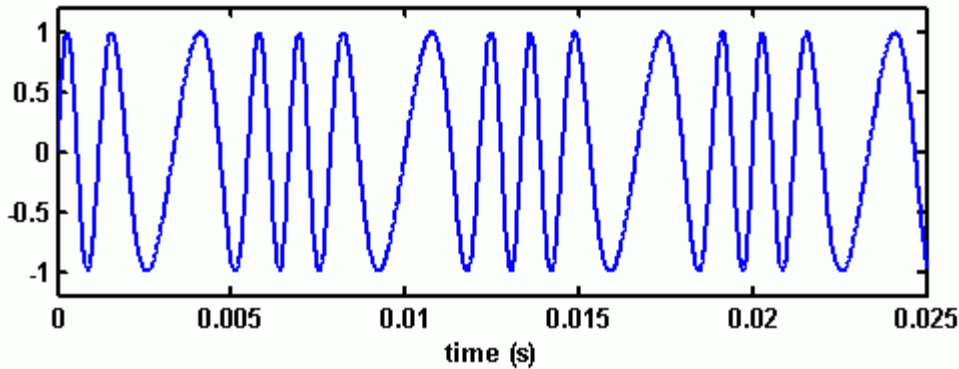
600

70

1

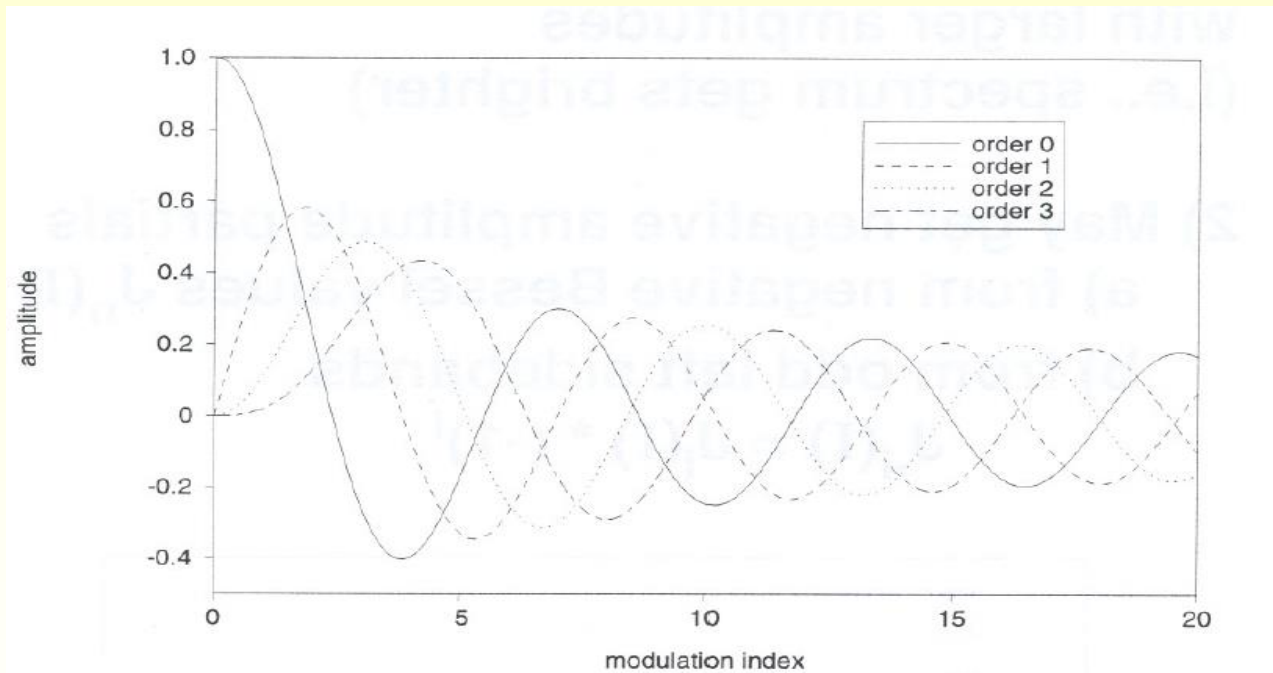


Frekvenční modulace



f_c	f_m	m_i	
600	150	2	🔊
600	170	2	🔊

Frekvenční modulace



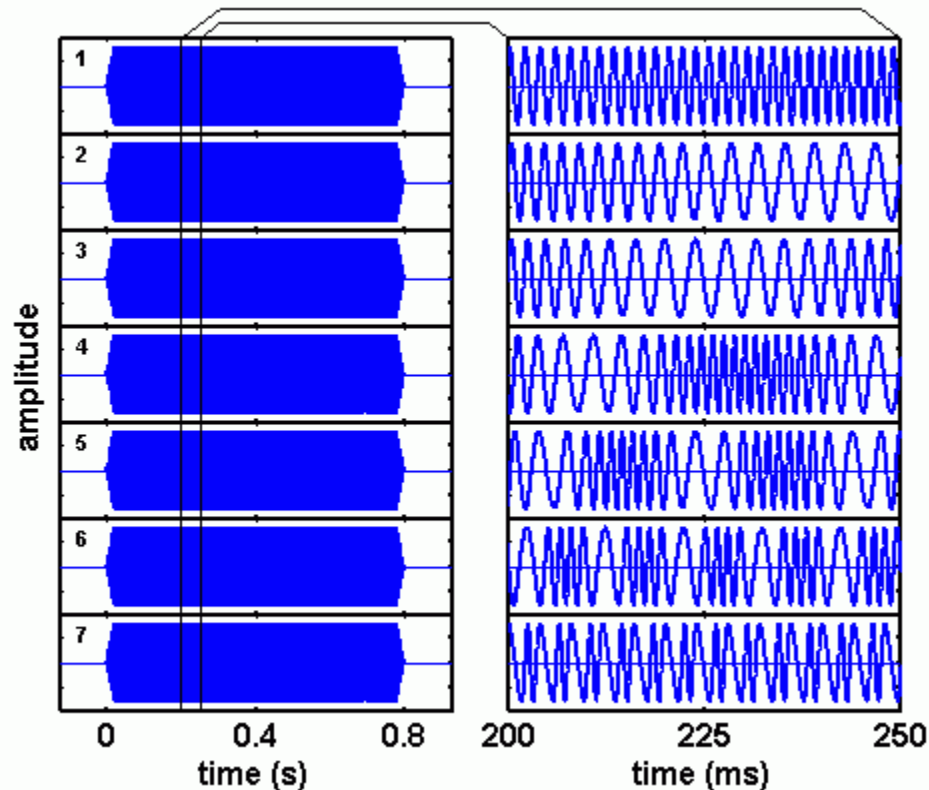
Frekvenční modulace

Harmonické a neharmonické modulační frekvence

$f_c = 500\text{Hz}$

$f_c = 500\text{Hz}$

$f_m = 2.5, 5, 10, 25, 50, 100, 250\text{ Hz}$ $f_m = 4.05, 8.09, 16.2, 40.5, 80.9, 162, 405\text{ Hz}$



Frekvenční modulace

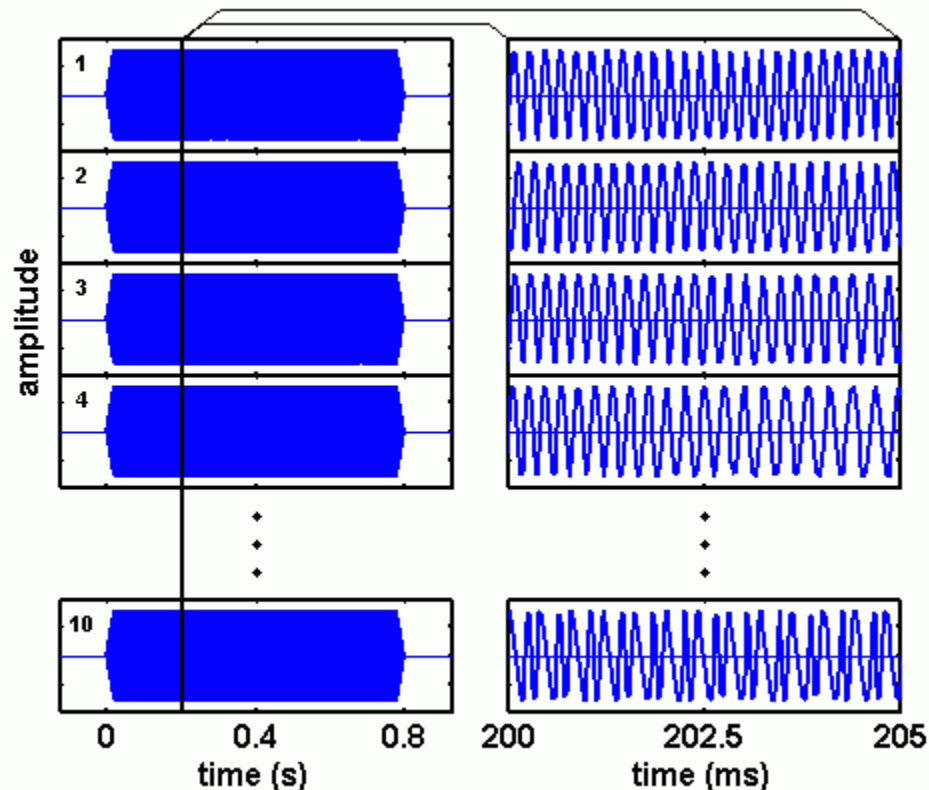
Harmonické a neharmonické modulační frekvence

$f_c = 5000\text{Hz}$

$f_m = 2.5, 5, 10, 25, 50, 100,$
 $250, 500, 1000, 2500\text{ Hz}$

$f_c = 5000\text{Hz}$

$f_m = 4.05, 8.09, 16.2, 40.5, 80.9,$
 $162, 405, 809, 1618, 4045\text{ Hz}$



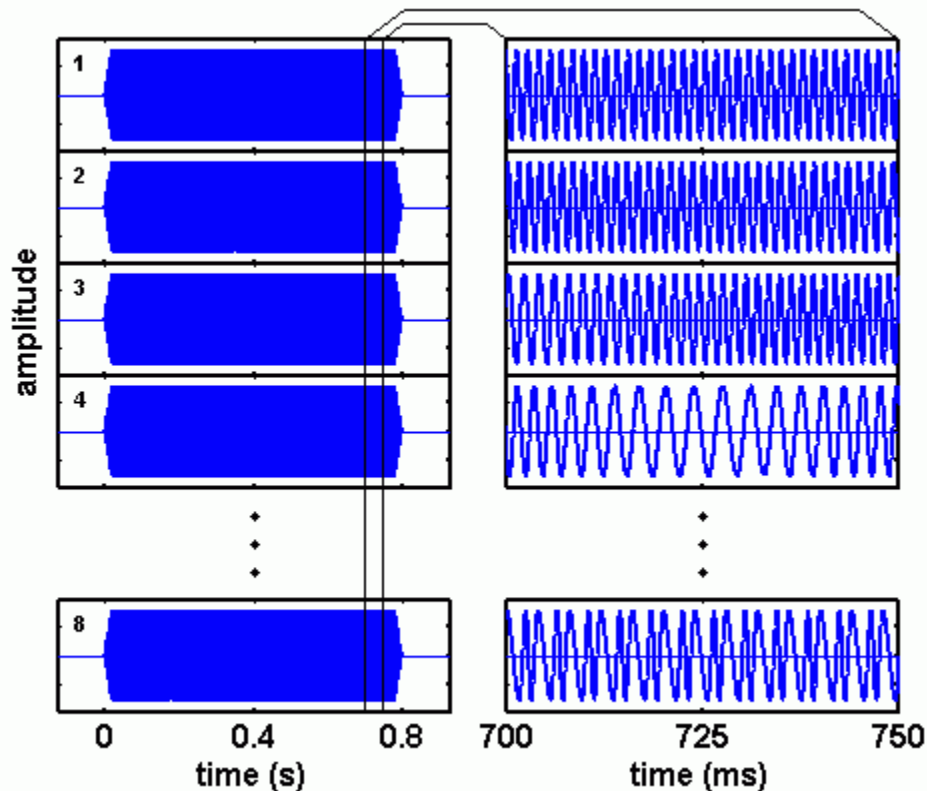
Frekvenční modulace

Zvětšení modulačního indexu

$f_c = 500\text{Hz}$

$f_c = 500\text{Hz}$

$f_m = 2.5, 5, 10, 25, 50, 100, 250\text{ Hz}$ $f_m = 4.05, 8.09, 16.2, 40.5, 80.9, 162, 405\text{ Hz}$

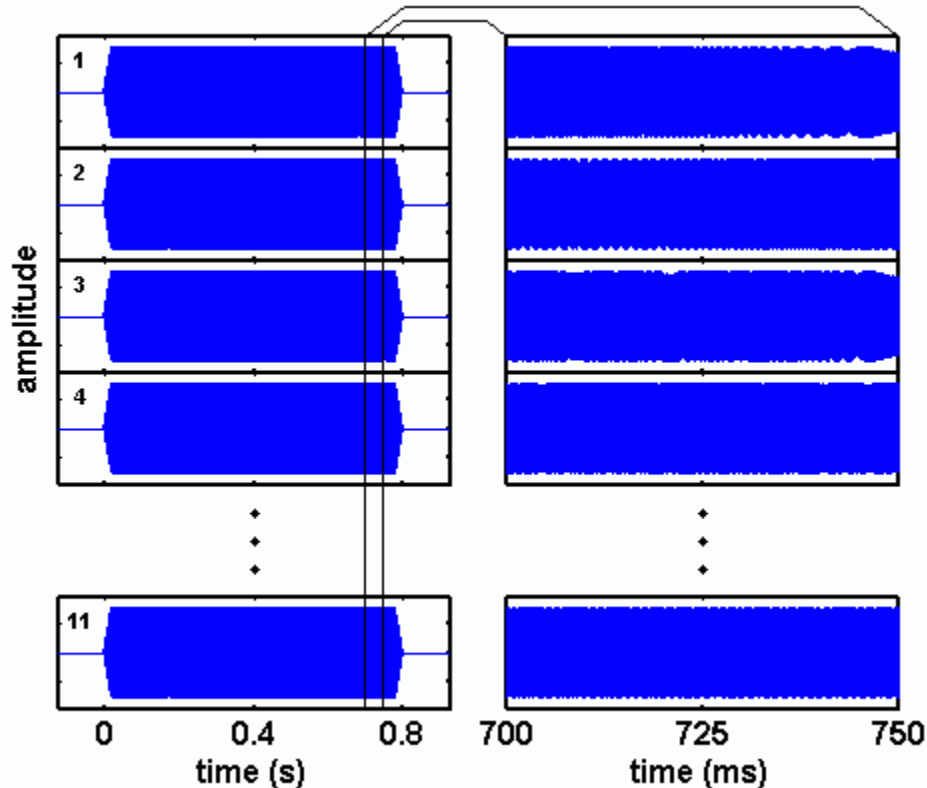


Frekvenční modulace

Zvětšení modulačního indexu

$f_c = 5000\text{Hz}$
 $f_m = 2.5, 5, 10, 25, 50, 100,$
 $250, 500, 1000, 2500\text{ Hz}$

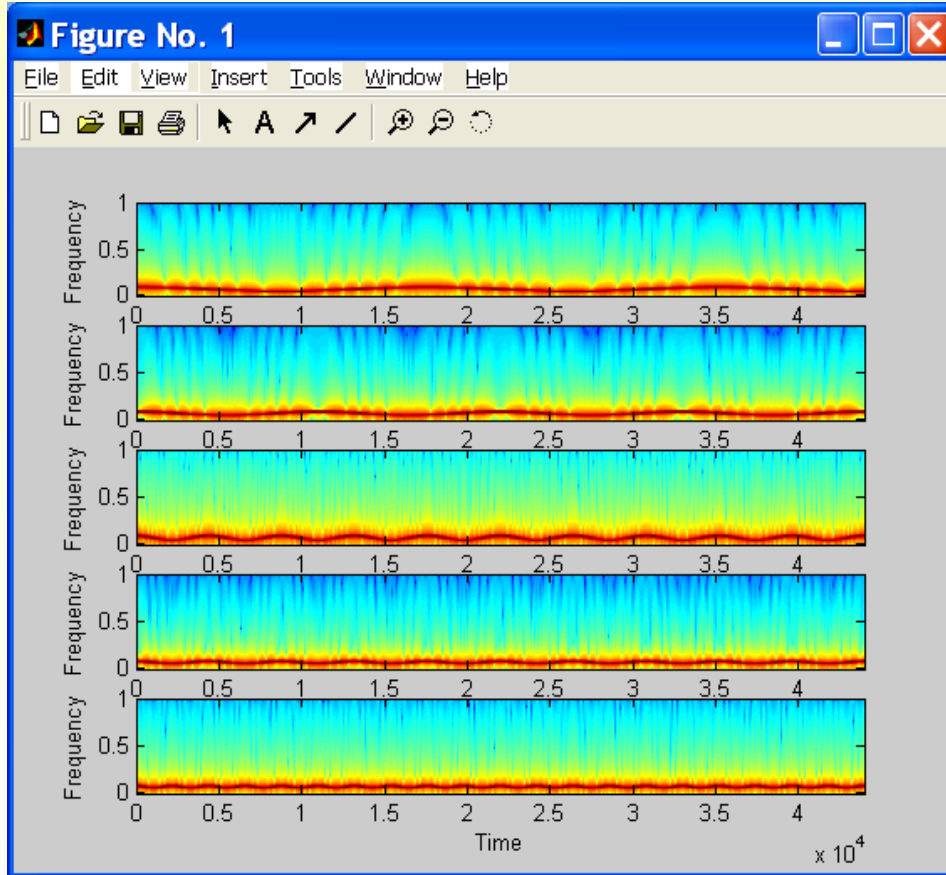
$f_c = 5000\text{Hz}$
 $f_m = 4.05, 8.09, 16.2, 40.5, 80.9,$
 $162, 405, 809, 1618, 4045\text{ Hz}$





(.wav)

Varovné signály



m_i	f_c	f_m
400	1500	1,25
200	1500	2
100	1500	5
50	1500	10
20	1500	25

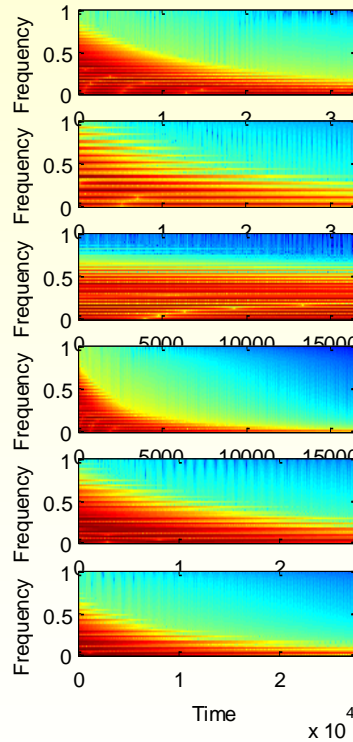
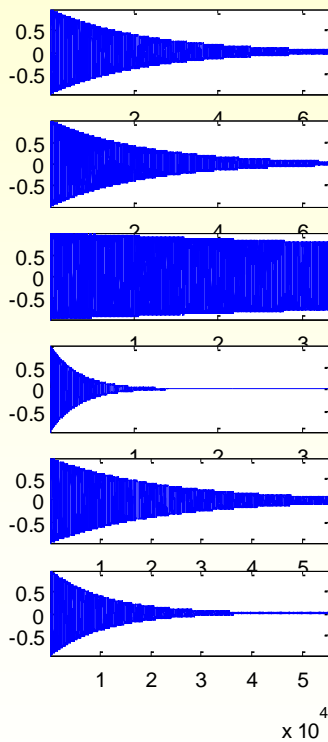
square

sawtooth

Syntetické zvony

obalka = $\exp(-t/\tau(k))$;

mi = $\ln(k) \cdot \exp(-t/\tau(k))$;

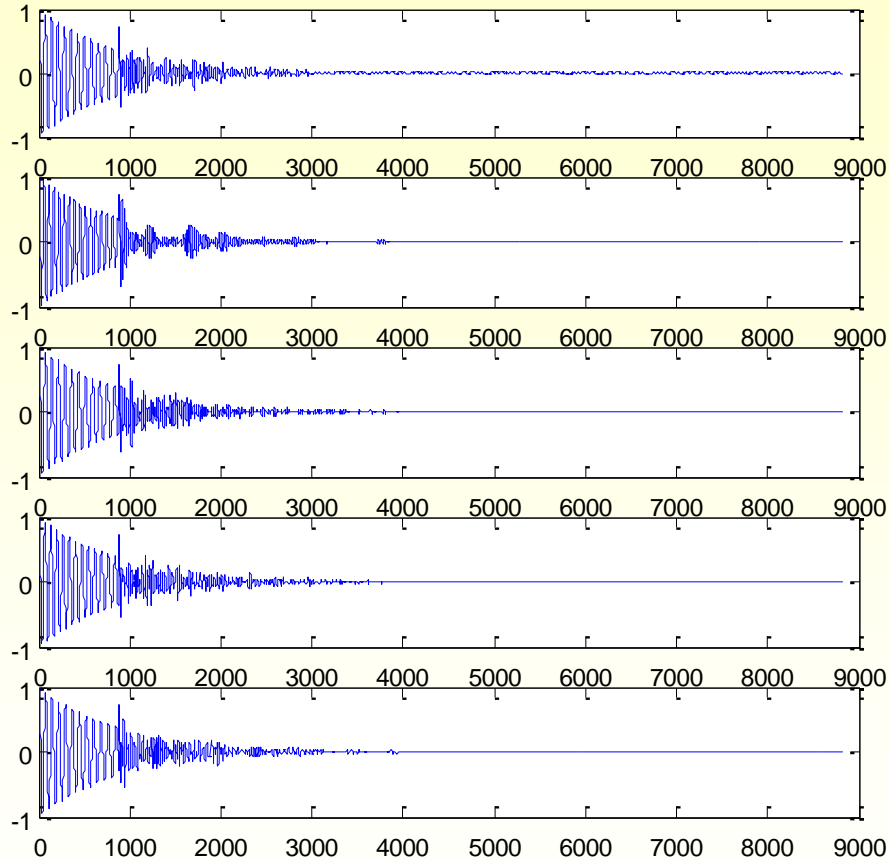


τ	l	f_c	f_m
2	10	110	220
2	5	220	440
12	10	110	220
0.3	10	110	220
2	5	250	350
1	3	250	350





Kapky vody



$$T_{obálky} = 20 \text{ ms}$$

$$m_i = 20$$

$$f_m = 7 \text{ Hz}$$

1. část 20 ms

$$f_c = 700 + 100 \text{randn}$$

2. část 180 ms

5 spektrálních složek

$$f_c = 1500 + 300 \text{randn}$$



Kapky vody

```
% synteticke kapky vody
% RC, 15.prosince 2008
clear, close all
fs      = 44100;
doba1   = 0.02;          % doba trvani prvni casti
doba2   = 0.18;          % doba trvani druhe casti
t1      = 0:1/fs:doba1-1/fs;
t2      = 0:1/fs:doba2-1/fs;
t       = 0:1/fs:doba1+doba2-1/fs;
fm      = 7;
mi      = 20;
tau     = 0.02;
pocet_kapek = 5;
y=[];
```



Kapky vody

```
for por_kapky      = 1:pocet_kapek,
    fc1            = 700+100*randn;
    cast1 = sin(2*pi*fc1*t1 + mi*cos(2*pi*fm*t1));
    A=0.4;
    cast2=zeros(1,length(t2));
    for h=1:5
        fc2      = 1500+300*randn;
        cast2 = cast2 + A*sin(2*pi*fc2*t2 +
                               mi*cos(2*pi*fm*t2));
    end;
    kapka(por_kapky,:)=[cast1 cast2].*exp(-t/tau);
    subplot(pocet_kapek,1,por_kapky),
        plot(kapka(por_kapky,:))
    sound(kapka(por_kapky,:),fs), pause(1)
    y=[y kapka(por_kapky,:) zeros(1,fs)];
end;
```

Jednoduché syntetické FM nástroje

ZVON

délka f_c

$H = f_m / f_c$

I_{max}

I_{min}

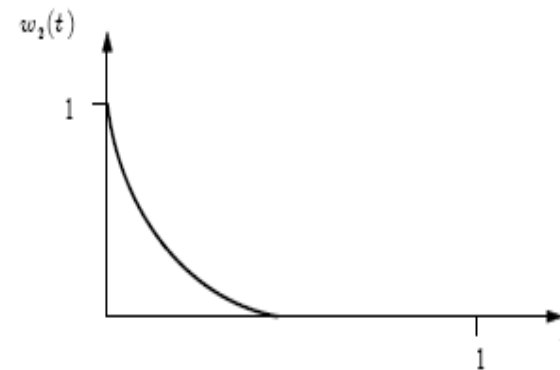
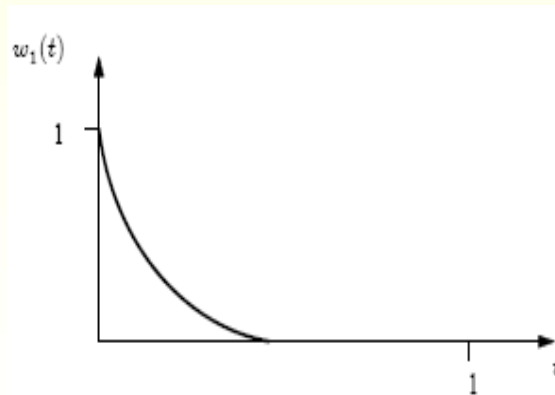
15

200

1.4

10

0



Amplitudová obálka

Obálka modulačního indexu

Jednoduché syntetické FM nástroje

BICÍ

délka f_c

$H = f_m/f_c$

I_{max}

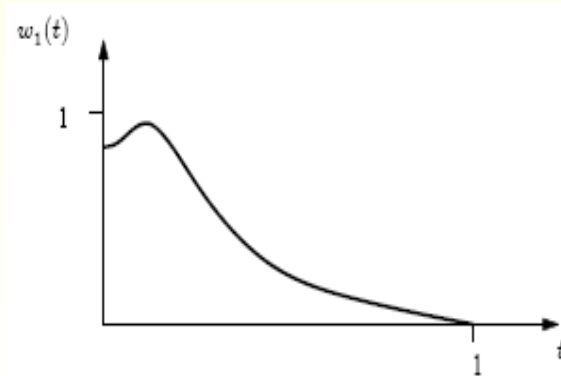
I_{min}

0.2 **80**

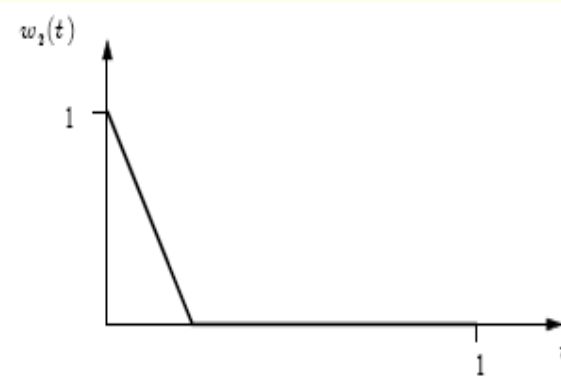
0.688

25

0



Amplitudová obálka



Obálka modulačního indexu

Jednoduché syntetické FM nástroje

ŽESTĚ

délka f_c

$H = f_m/f_c$

I_{max}

I_{min}

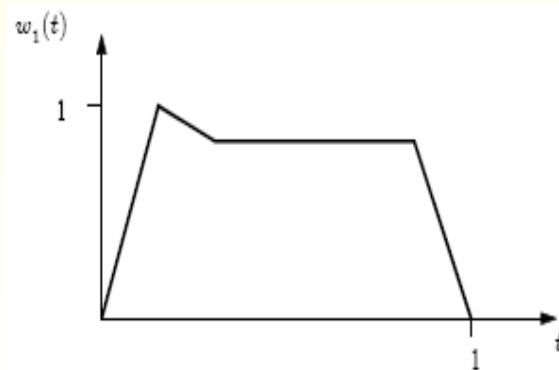
0.6

440

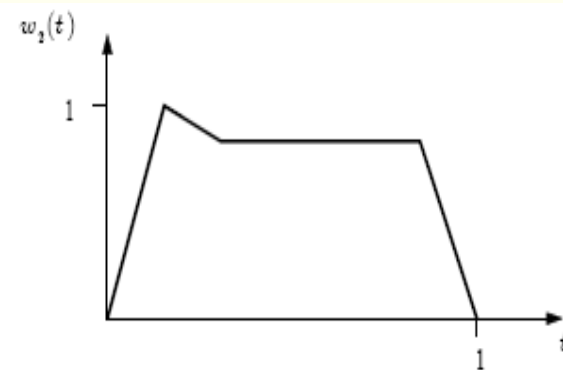
1.0

5

0



Amplitudová obálka

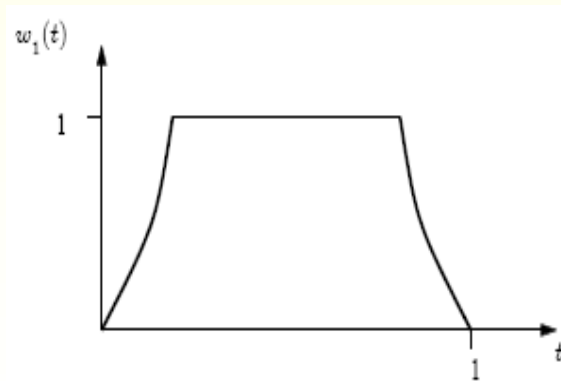


Obálka modulačního indexu

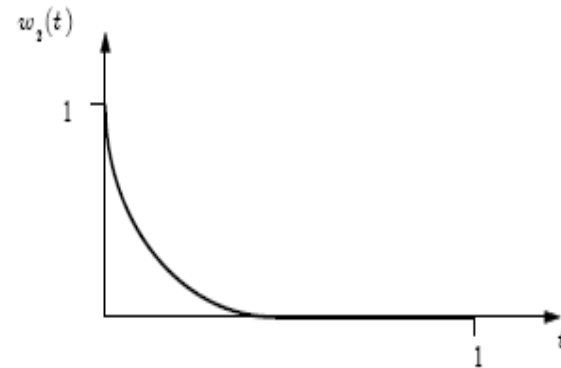
Jednoduché syntetické FM nástroje

KLARINET délka f_c $H = f_m/f_c$ I_{max} I_{min}

0.5 **900** **0.667** **4** **2**



Amplitudová obálka



Obálka modulačního indexu

Jednoduché syntetické FM nástroje

FAGOT

délka f_c

$H = f_m/f_c$

I_{max}

I_{min}

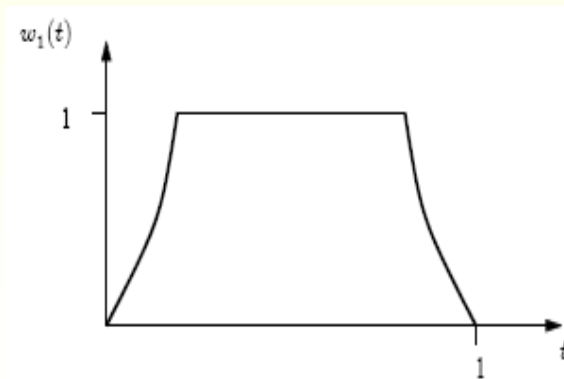
0.5

1100

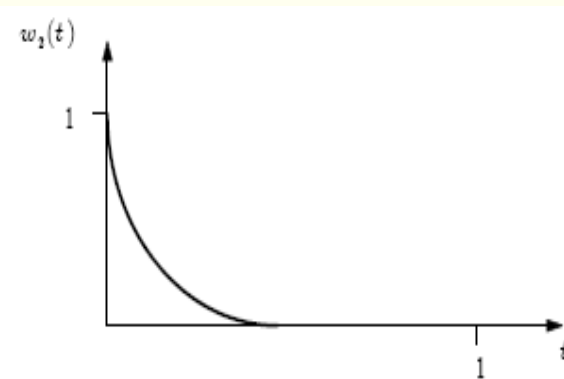
0.2

1.5

0

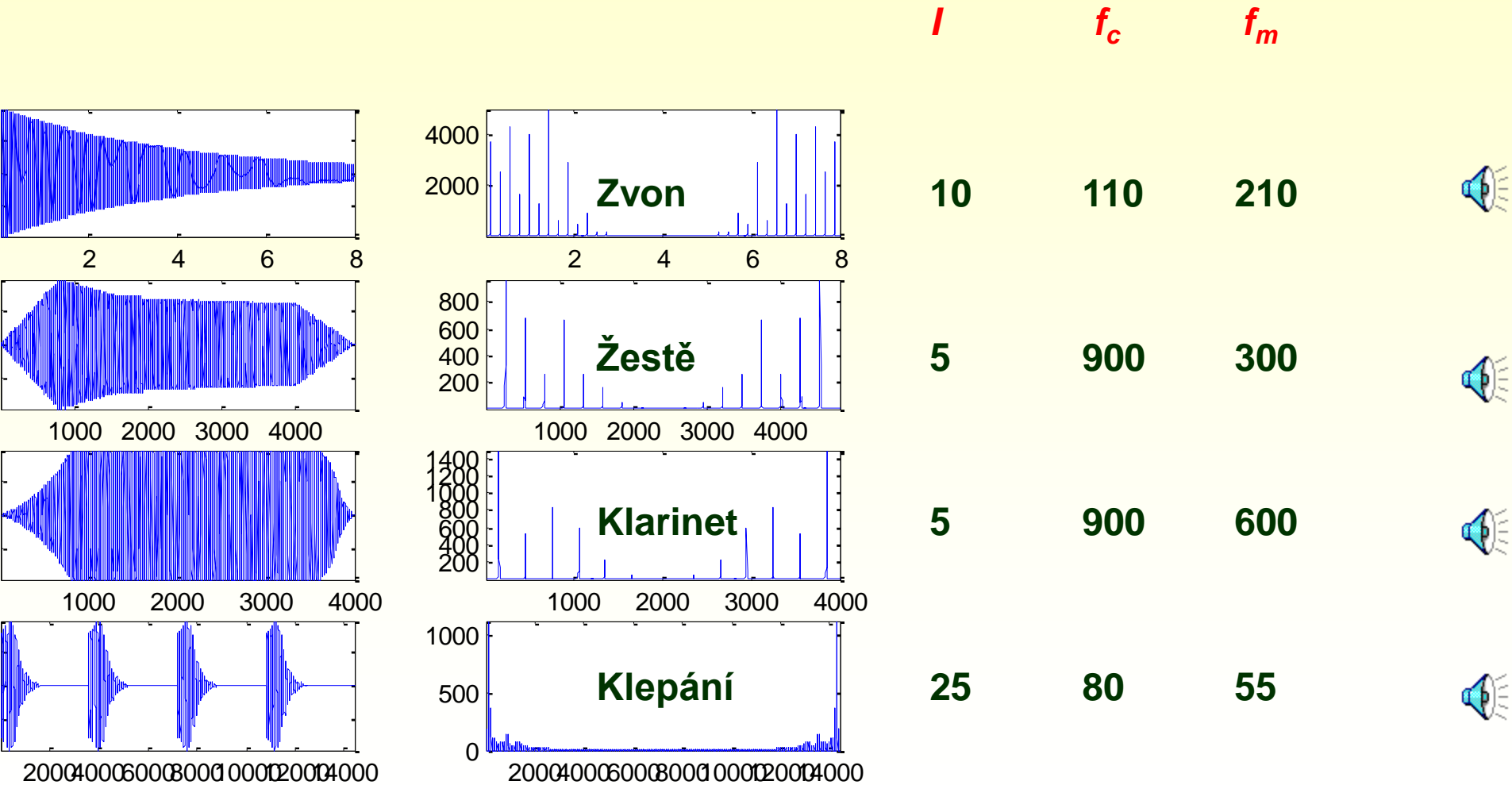


Amplitudová obálka



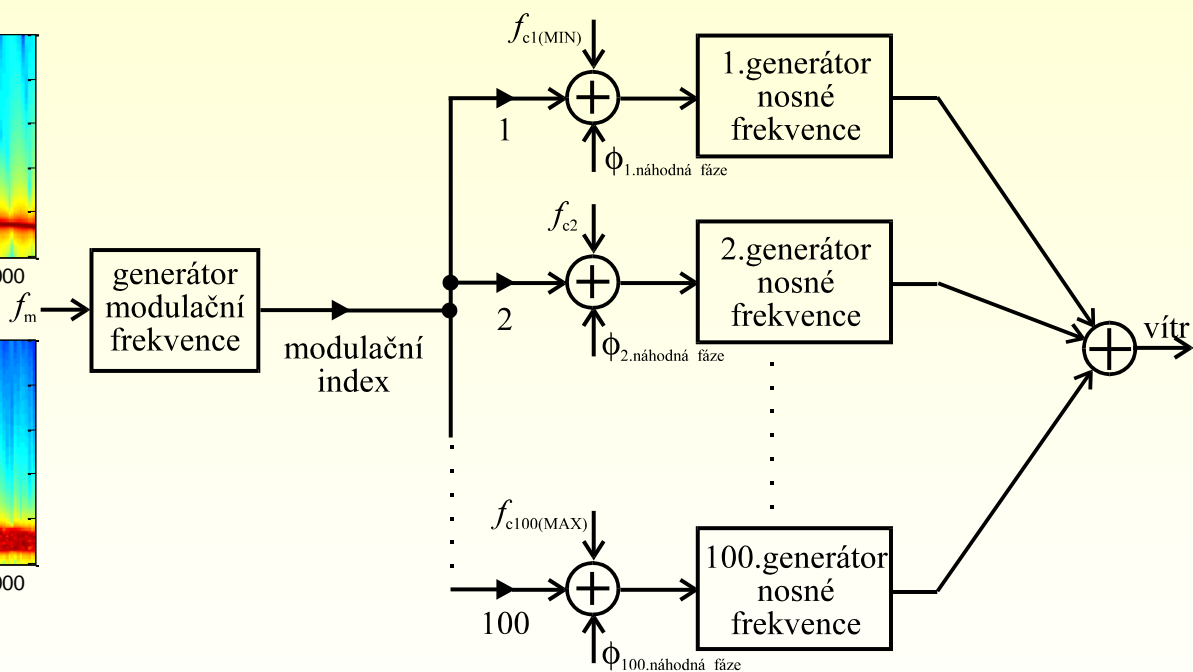
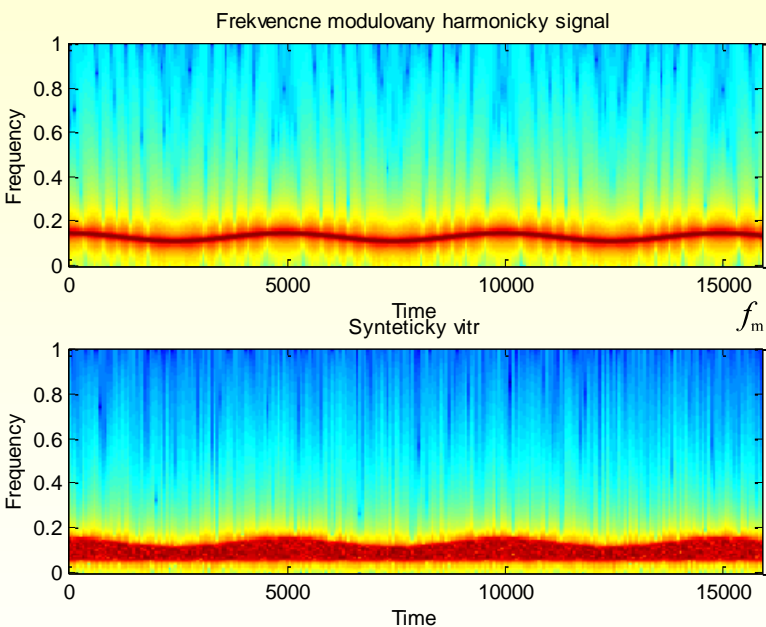
Obálka modulačního indexu

Jednoduché syntetické FM nástroje





Syntetické zvuky - vítr



Modulační syntéza

Ukázky semestrálních prací



Dvořák Jan

Syntéza zvuků telefonu (oznamovací tón, DTMF volba, 6x různé typy vyzvánění, oznámení o SMS zprávě)
AM, FM, aditivní a filtrační syntéza



Gregor Pavel

Kostel v horách
zvony vytvořené FM modulací, přidaná AM modulace + echo, vítr vytvořený filtrační syntézou



Chlumecký Martin

Policejní konvoj
FM, AM



Pazdera František

Hasičská siréna
FM + echo + dozvuk



Vibráto

$$x(t) = O.* \sum_{n=1}^9 \alpha_n \sin(2\pi n f_c t + 7\sqrt{n} \cdot \sin(2\pi f_m t))$$

$$f_c = 440\text{Hz}, f_m = 5\text{Hz}$$

$$\alpha_n = 1000, 300, 0.01, 0.01, 0.01, 3, 0.5, 1, 4$$

$$O \dots X = [0.2 \ 8.95 \ 1], Y = [0 \ 1 \ .3 \ 10]$$

Vibráto

```
% vibrato
```

```
clear all; close all;
```

```
fs = 22050; f0 = 440; fm = 5; doba = 5;
```

```
t = 0:1/fs:doba-1/fs;
```

```
alfa = [1000 300 .1 .1 .1 3 .5 1 4];
```

```
% vibrato s aditivni syntejou
```

```
x = zeros(1,length(t));
```

```
for n = 1:9
```

```
    x = x + alfa(n)*sin(2*pi*f0*n.*t + 7*sqrt(n)*sin(2*pi*fm.*t));
```

```
end
```

```
% obalka
```

```
X = [0 .2 .8 .95 1].*t(end); Y = [0 1 .3 .1 0]; O=interp1(X,Y,t);
```

```
x = x.*O; x = .98*x/(max(abs(x)));
```

```
sound(x,fs);
```

Zvuky

<http://www.soundsnap.com/>